

# Design and Analysis of Algorithms

## Course Information

- 1 Why Study Algorithm?
- 2 How to Study Algorithm?
- 3 Recap and Exams

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Two ideas changes the world!

# Typography

1448, German, Johann Guternberg: print books by putting together movable metallic pieces



- literacy spread ⇒ Dark Ages ended ⇒ human intellect was liberated ⇒ science and technology triumphed ⇒ Industrial Revolution happened

imagine a world in which only an elite could read lines

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But others insist that the key development was not typography,  
but *algorithm*

## Algorithm

Origin: decimal system

- 10 symbols  $\Rightarrow$  even large numbers can be expressed compactly (invented in India around AD 600)
- basic methods for add, mul, div, even square roots and  $\pi$  (9th century, Arabic, Baghdad, Al-Khwarizmi)



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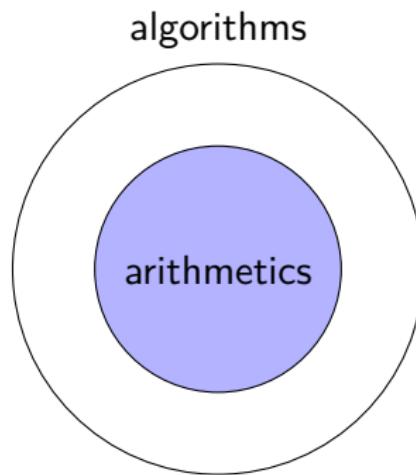
Back to 1448: imaging how to add/mul two Roman numbers:  
 $MCDXLVIII + DCCCXII$ ? fingers are not enough

## Algorithm Etymology

Spread to Europe around 12th century → plays an enormous role in Western civilization (science and technology, commerce and industry)

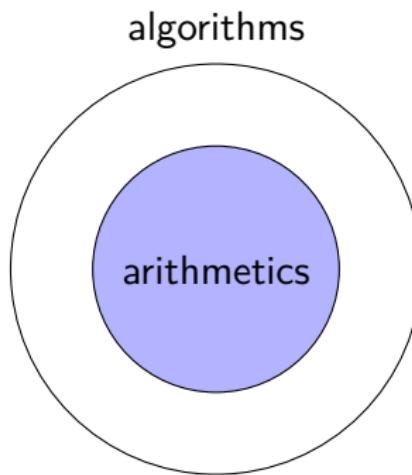
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Computer era: evolve to embody the positional system and arithmetic unit ↗ scientists develop algorithms for all kinds of problems — ultimately change the world

## Why Study Algorithms

**Internet.** Web search, packet routing, distributed file sharing, ...

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**Computer graphics.** movies, video games, virtual reality, ...

**Multimedia.** MP3, JPG, DivX, HDTV ...

**Artificial Intelligence.** face recognition, PS, more AI algorithms

**Social networks.** recommendations, news feeds, advertisements, ...

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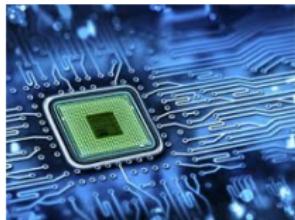
**Computers.** circuit layout, databases, caching, compilers, ...

**Biology.** human genome project, protein folding, ...

**Physics.**  $N$ -body simulation, particle collision simulation, ...

## Importance: Look around you

Google  
YAHOO!  
bing



Algorithms interesting and useful.  
We live in the algorithm world!

## Cryptographic Algorithms

Most algorithms focus on solving problems efficiently

- make us live in a better world

Good man and bad man live in the same world

- good man need *cryptographic algorithms* to protect them from bad man: enjoying the benefits in a secure manner

Cryptographic algorithms ensure there is no *efficient algorithms* against some problems



# Fundamental of Computer Sciences

## Algorithm design and analysis

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$\mathcal{P} = \mathcal{NP}$  is one of the most important questions in this century

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- data structure

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Advanced topics

- complexity theory
- randomized algorithms
- approximate algorithms

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Tips

- theory: think rigorously and keep ask yourself why
- practice: implement algorithms using your favorite programming languages

# Course Website

Syllabus

Office hours

Assignments

Lecture slides

...

[https://yuchen1024.github.io/teaching/SDU/2020\\_spring\\_algorithms/2020\\_spring\\_algorithms.html](https://yuchen1024.github.io/teaching/SDU/2020_spring_algorithms/2020_spring_algorithms.html)

## References and Resources

### Textbooks

- Algorithms. Sanjoy Dasgupta, Christos Papadimitriou, and Umesh Vazirani. The McGraw-Hill Companies, 2008.
- 算法设计与分析 (第二版). 屈婉玲, 刘田, 张立昂, 王捍贫. 清华大学出版社, 2016.2.

### Online resources

- leetcode
- online judging system: ZOJ, POJ

## Assignments

- electronic submission
- graded for correctness, clarity, conciseness, rigor, and efficiency
- recommendation: using  $\text{\LaTeX}$  template for writing solutions
- no collaboration, no Google

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### 算法的起源、发展与学习算法的意义

算法分析: 时、空复杂度为指标定量分析算法优劣

- 算法的伪码表示
- 最优、最坏、平均复杂度 (以排序算法为例)
- 函数的渐近复杂度
- 函数阶的计算: 递归方程求解技术 (迭代、递归树、主定理)
- 常见的函数阶

## 课程回顾 (2/4): 算法设计技术

### 分治

- 典型问题: 排序选择类、计算几何类、数值计算类 (快速幂、整数乘、矩阵乘、多项式乘)
- 设计: 子问题的划分与子问题解的合并
- 分析: 递归方程求解

### 贪心

- 典型问题 (最优子结构): 最优调度、最优装载、Huffman Coding、单源最短路径、最小生成树
- 设计: 选择贪心策略 (试错: 构造反例说明贪心策略非最优)
- 证明: 数学归纳法证明贪心解是最优解 (对问题的规模或算法的步骤进行归纳)

## 课程回顾 (3/4): 算法设计技术

### 动态规划

- 典型问题 (最优子结构 + 重叠子问题): 字符串类 (最长递增子序列、最大公共子序列、最小编辑距离)、矩阵链、最大子段和、背包类
- 设计: 找出 DAG, 列出递推方程, 设计备忘录和标记函数
- 分析: 根据递推方程或者备忘录分析时空复杂度

分治、贪心、动态规划设计范式的适用范围: 原始问题具有 (最优) 子结构性质  $\Rightarrow$  原始问题可分解为子问题

搜索技术: 求解优化类问题的通用技术 (将解空间建模为树)

- 暴力搜索
- 回溯 (Domino 性质: 根据优化类问题的约束条件及时停止局部搜索并回溯)
- 分支定界 (引入界和估计函数, 在约束条件的基础上加入更精细的判断)

### 复杂性理论

- 计算模型: Turing Machine (deterministic poly-time and non-deterministic poly-time)
- 重要的复杂性类:  $\mathcal{P}$ ,  $\mathcal{NP}$ ,  $\mathcal{NP}$ -hard,  $\mathcal{NP}$ -complete
- 更多的复杂性类:  $BPP$  (降低错误的方法和为什么能降低、衍生复杂性类、与其他复杂性类的关系)

### 随机算法初步

- 概率论初步: 期望线性性质的应用
- Miller-Rabin 素性检测算法
- Schwartz-Zippel 引理及其应用: 多项式恒等测试、矩阵运算结果测试

## Exams

总成绩 = 0.2 × 平时成绩 + 0.2 × 课后作业 + 0.6 × 考试成绩

考试日期: 2020.06.24 上午 8:30 ~ 10:30

考试形式: 线上闭卷 (不允许查阅资料和搜索)

- 考试开始前 5 分钟: 微信群中推送试卷电子版
- 腾讯会议打开摄像头进行答题
- 考试完成延长 5 分钟对试卷进行拍照, 将电子版发送至助教老师邮箱



Figure: 结合同学意见和学校要求

## 考试题型与范围

选择题 (送分题):  $5 \times 2 = 10$

- 考察渐近复杂度、经典算法和复杂性的常识

简答题 (又是送分题):  $15 \times 2 = 30$

- 渐近复杂度或递归方程求解
- 复杂性类的基本概念

算法设计与分析题 (还是送分题):  $20 \times 3 = 60$

- 分治、贪心、动态规划

评判标准: 根据算法的正确性和效率评分.

解答需包含以下四部分: (1) 算法思想; (2) 分治算法需写出递归方程, 贪心法需给出正确性证明, 动态规划算法需写出递推方程和标记函数; (3) 伪代码; (4) 时间复杂度分析

回溯和随机算法不做重点考察

逢考必过

