# Ablation Study of QRDQN

311551059 陳昱丞

#### Outline

- Background
- Experiments and Result Analysis
- Conclusion
- Appendix
- Reference

# Background

#### QRDQN

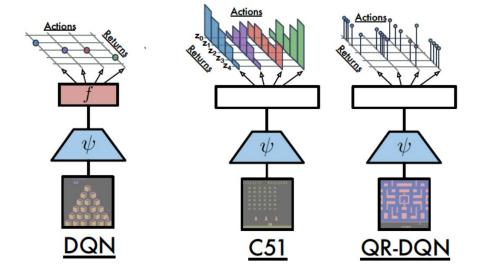
• Learn value distribution Z(s,a) and use E[Z(s,a)] as Q.

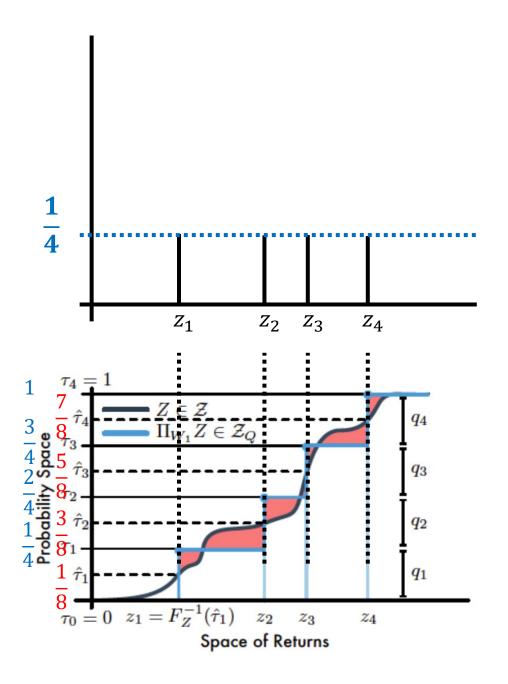
• 
$$Q^{\pi}(s, a) = E[Z^{\pi}(s, a)] = E[\sum_{t=0}^{\infty} \gamma^t r(s_t, a_t)]$$

Distributional Bellman Equation:

• 
$$Z^{\pi}(s,a) = r(s,a) + \gamma Z^{\pi}(s',a')$$

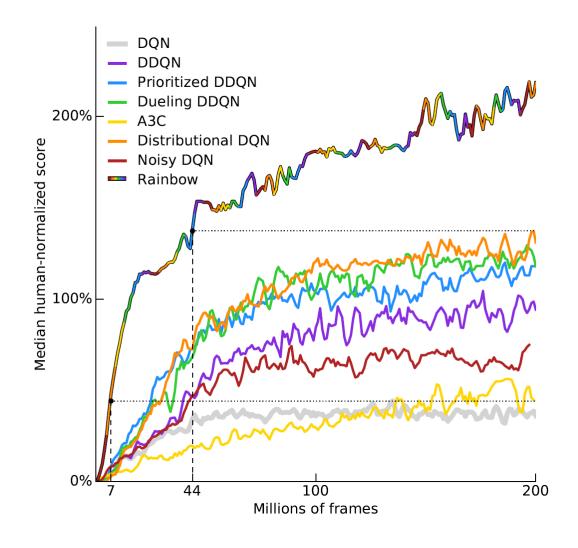
# QRDQN





#### Rainbow

- Double Q learning
- Prioritized Experience Replay
- Dueling networks
- Multi-step learning
- Noisy Nets
- Distributional RL
  - C51



## Double Q Learning

• DQN suffers from over-estimation.

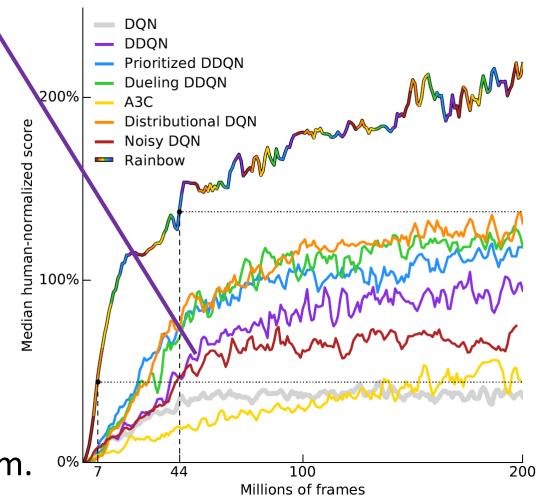


Behavior and Target network.

$$Y_t^{Q} = r_{t+1} + \gamma \max_{a} Q(S_{t+1}, a | \theta^{-})$$

$$Y_t^{DoubleQ} = r_{t+1} + \gamma Q\left(S_{t+1}, \arg\max_{a} Q(S_{t+1}, a | \theta) | \theta^{-}\right)$$

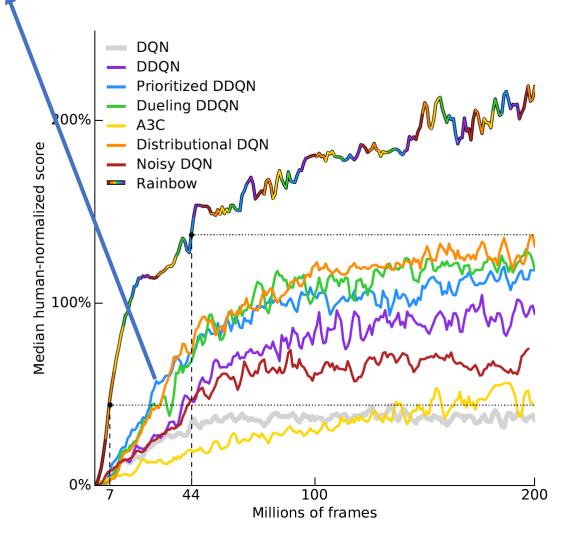
• Reduce the over-estimation problem.



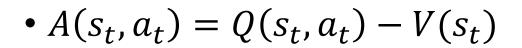
## Prioritized Experience Replay

 Sample important transitions from replay buffer more frequently.

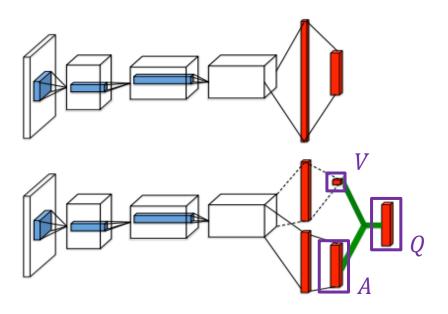
 Calculation of importance is based on TD-error.

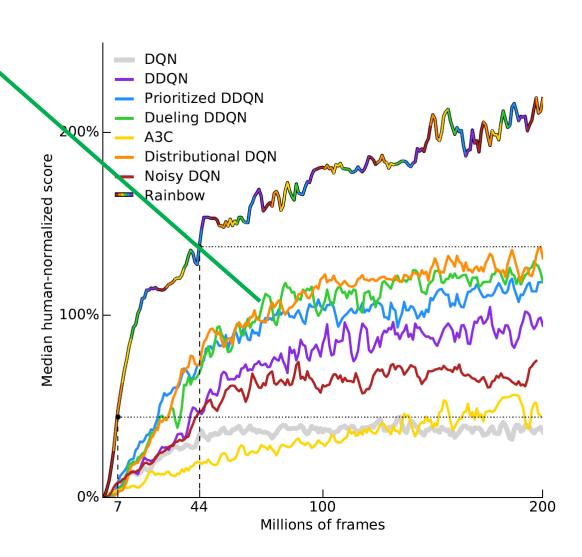


### **Dueling Networks**



$$\to Q(s_t, a_t) = A(s_t, a_t) + V(s)$$





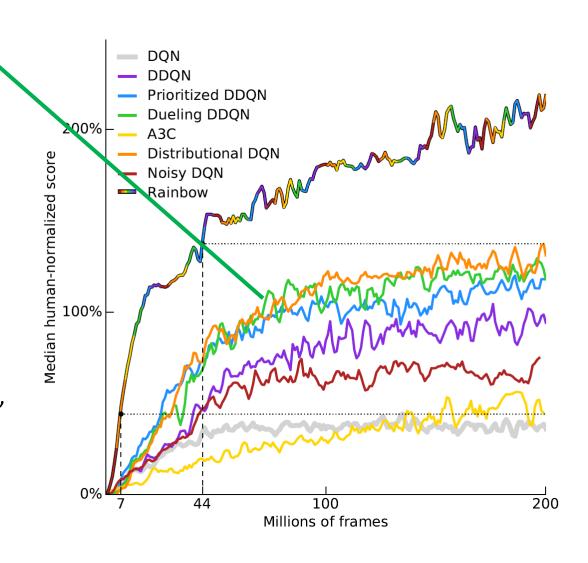
# **Dueling Networks**

• 
$$E_a[A(s_t, a_t)] = E_a[Q(s_t, a_t) - V(s_t)]$$
  
=  $V(s_t) - V(s_t) = 0$ 

Constrain the value of A:

$$Q(s_t, a_t) = V(s) + A(s_t, a_t) - \frac{1}{|A|} \sum_{a_t'} A(s_t, a_t')$$

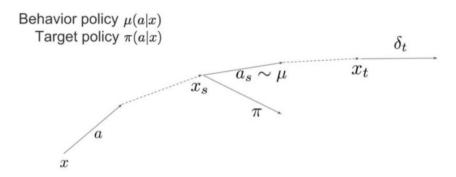
• Due to the relatively small numerical range of the value A, it is more sensitive to model updates, making it easier for the model to consider the relative changes in relation to other actions.



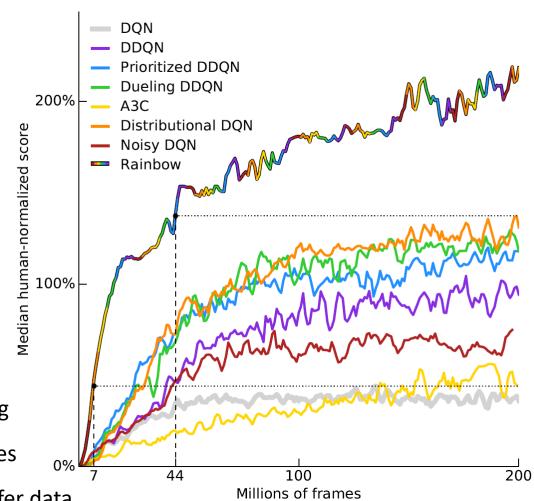
# Multi-step Learning

• 
$$R_t^{(n)} = \sum_{k=0}^{n-1} \gamma_t^{(k)} R_{t+k+1}$$

• 
$$R_t^{(n)} + \gamma_t^{(n)} \max_{a'} Q_{\theta}(S_{t+n}, a') - Q_{\theta}(S_t, A_t)$$



Under different policies, the probability of encountering
 a specific n-steps trajectory can vary. This discrepancy gives
 rise to the issue of distribution mismatch in off-policy buffer data.



### Noisy Nets

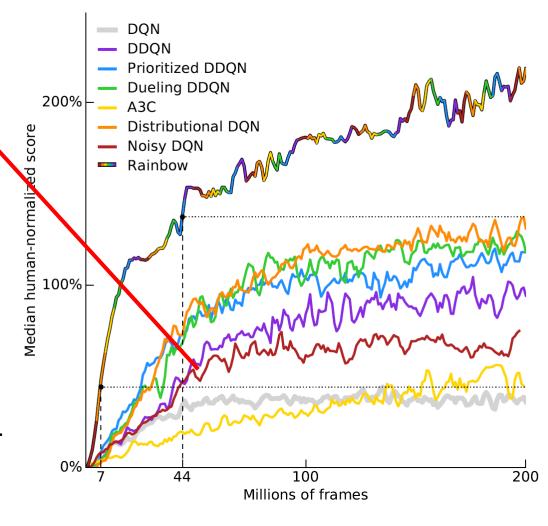
- Replace  $\epsilon$ -greedy.
- Noise on Parameters

$$a = arg \max_{a} \frac{\tilde{Q}}{Q}(s, a)$$

Inject noise into the parameters of Q-function at the beginning of each episode

$$Q(s,a) \longrightarrow \tilde{Q}(s,a)$$
Add noise

- $\epsilon$ -greedy
  - Action is randomly selected.
  - When encountering the same state again, it is possible to choose a completely different action.
- Noisy Nets
  - Noise remains the same within the same episode.
  - More systematic exploration method, the paper refer to it as "State-dependent Exploration".



How about Rainbow using QRDQN?

(QR-Rainbow)

# Experiments and Result Analysis

### Settings

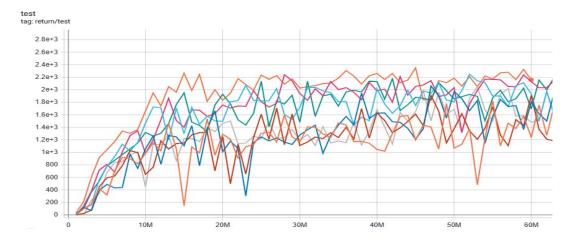
num steps: 50000000 batch size: 32 lr: 5e-5 memory\_size: 1000000 gamma: 0.99 multi\_step: 1 update interval: 4 target\_update\_interval: 10000 start steps: 50000 epsilon train: 0.1 epsilon eval: 0.01 epsilon\_decay\_steps: 250000 double\_q\_learning: False dueling\_net: False noisy net: False use per: False log interval: 100 eval interval: 250000 num\_eval\_steps: 125000

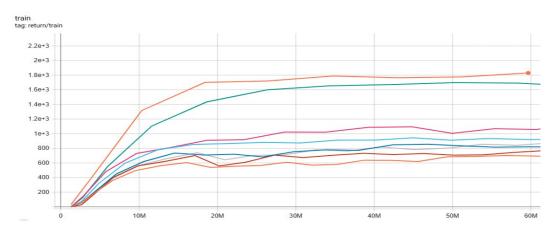
max episode steps: 27000

- Environment Atari games (with NoFrameskip-v4):
  - Breakout
  - Enduro (following slides)
  - MsPacman
- Number of frames:
  - 60M to 80M
- Comparison:
  - DQN
  - QRDQN (N = 200, kappa = 1)
    - QR origin
    - QR + Double Q
    - QR + PER
    - QR + Dueling
    - QR + Noisy
    - QR + Multistep (step=3)
    - QR Rainbow

### **QRDQN** Rainbow

- DQN
- **☑** QRDQN
- QRDQN Double-Q
- QRDQN Dueling Network
- QRDQN Multistep Return
- QRDQN Noisy Network
- QRDQN Prioritize Experience Replay
- QRDQN Rainbow

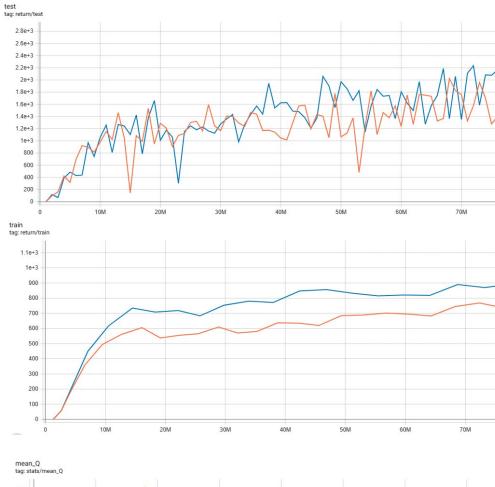


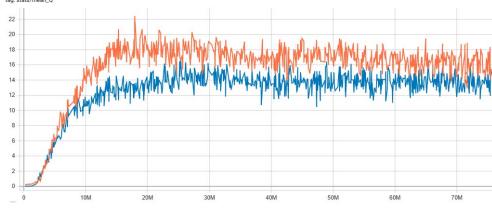




# QRDQN vs DQN

- Training:
  - QRDQN > DQN
- Testing:
  - QRDQN > DQN
- Estimation of Q:
  - QRDQN < DQN

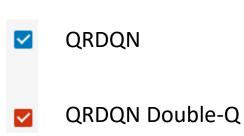


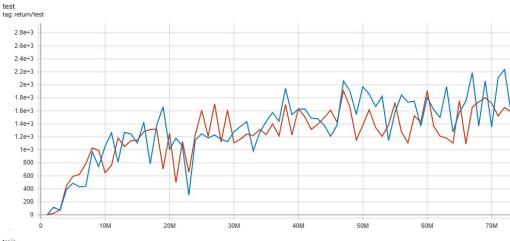


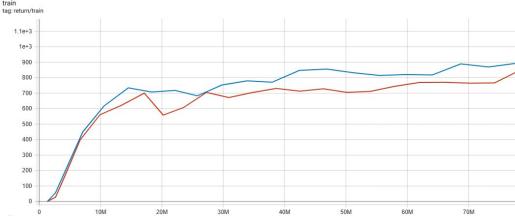


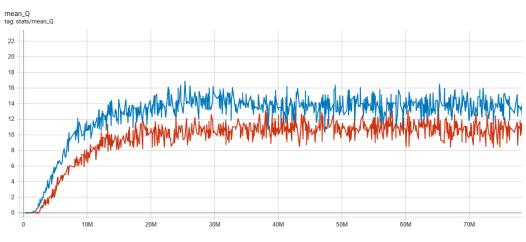
### QR vs QR Double-Q

- Training:
  - QRDQN > QR Double-Q
- Testing:
  - QRDQN >= QR Double-Q
- Estimation of Q:
  - QRDQN > QR Double-Q
- Reduce over-estimation (?)





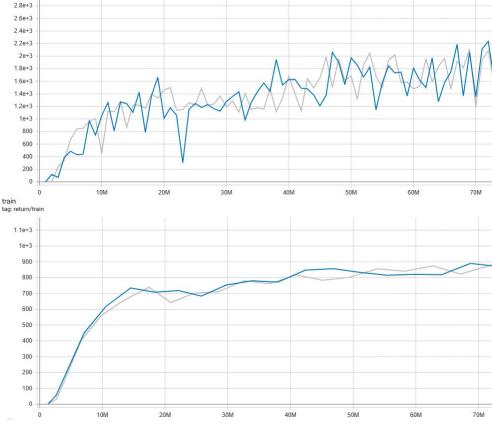


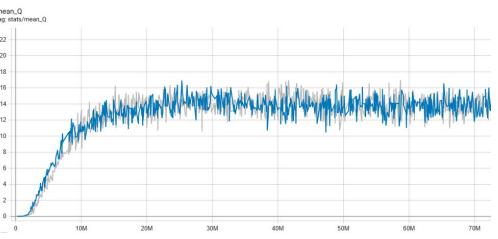


#### QR vs QR PER

- Training:
  - QRDQN = QR PER
- Testing:
  - QRDQN = QR PER
- Estimation of Q:
  - QRDQN = QR PER
- PER is not so effective in dense reward environment.







### QR vs QR Dueling Network

- Training:
  - QRDQN < QR Dueling</li>
- Testing:
  - QRDQN < QR Dueling</li>
- Estimation of Q:
  - QRDQN > QR Dueling
- Great performance against QR in early

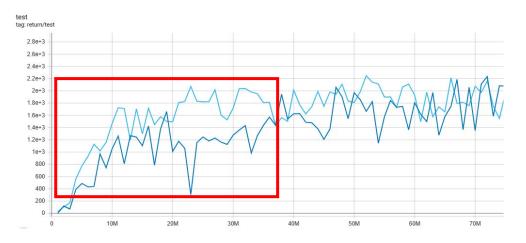
stage while testing.

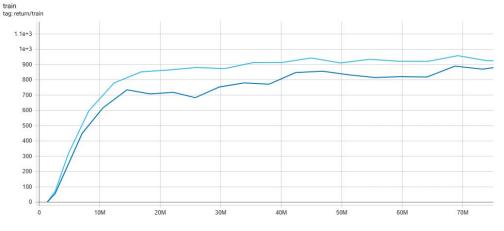


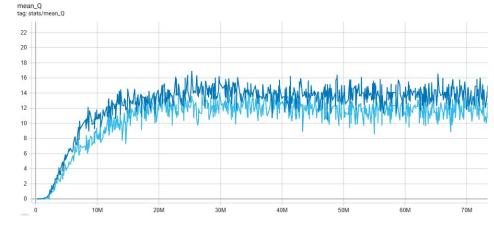
**QRDQN** 



**QRDQN** Dueling





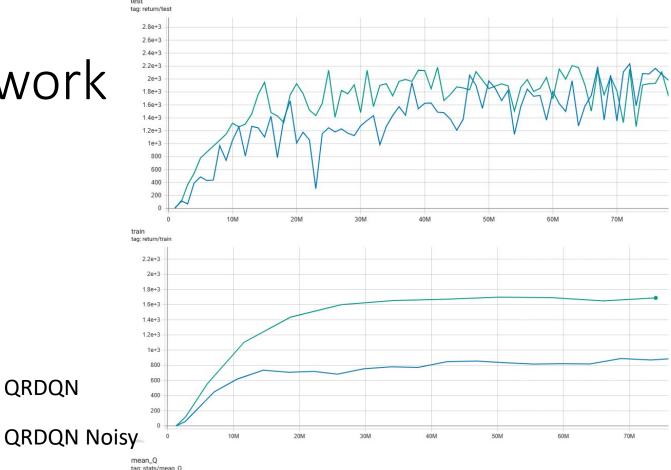


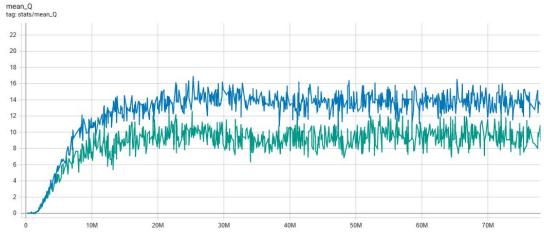
### QR vs QR Noisy Network

- Training:
  - QRDQN << QR Noisy</li>
- Testing:
  - QRDQN < QR Noisy</li>
- Estimation of Q:
  - QRDQN > QR Noisy
- Excellent performance on training return, but seems not translating into testing.

**QRDQN** 

Sample noise while testing?





### QR vs QR Multistep

 $\checkmark$ 

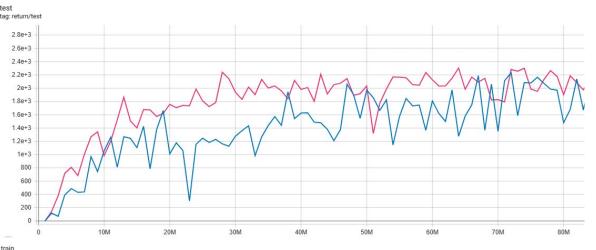
**QRDQN** 

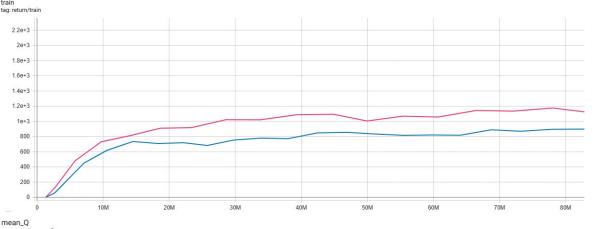
• Training:

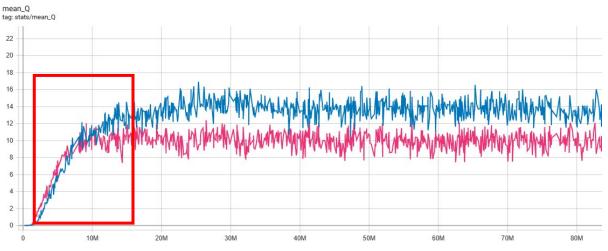


**QRDQN** Multistep

- QRDQN < QR Multistep</li>
- Testing:
  - QRDQN < QR Multistep</li>
- Estimation of Q:
  - QRDQN > QR Multistep
- High Q-value initially, but as training progress, Q-value tends to be lower.



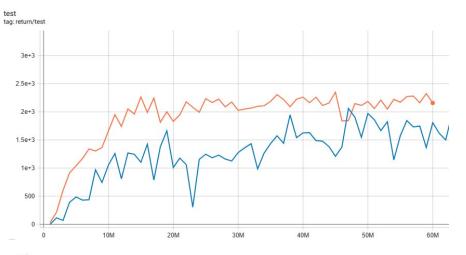


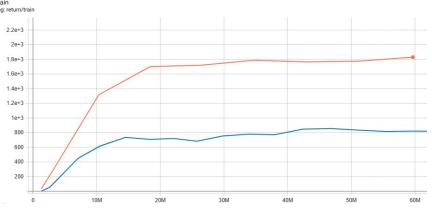


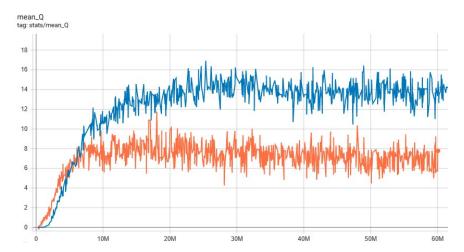
#### QR vs QR Rainbow

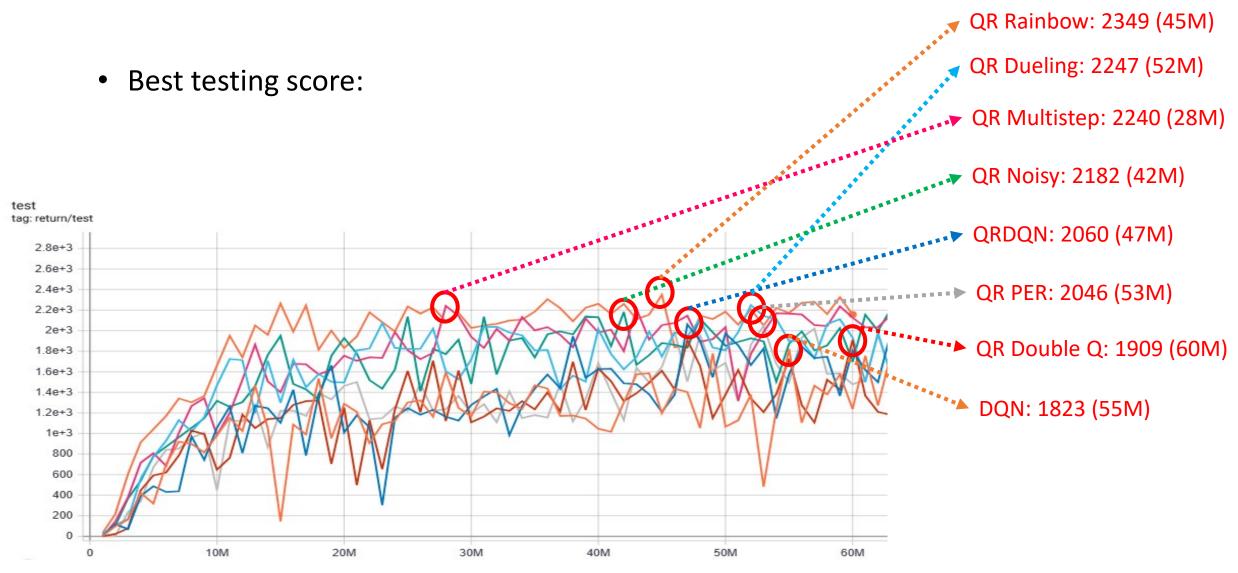
- Training:
  - QRDQN << QR Rainbow</li>
- Testing:
  - QRDQN << QR Rainbow</li>
- Estimation of Q:
  - QRDQN >> QR Rainbow
- Best performance.



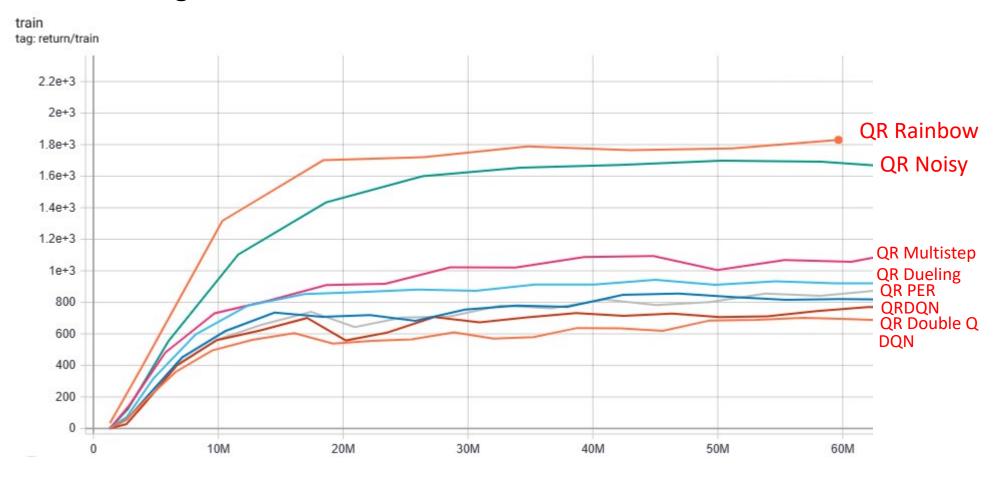




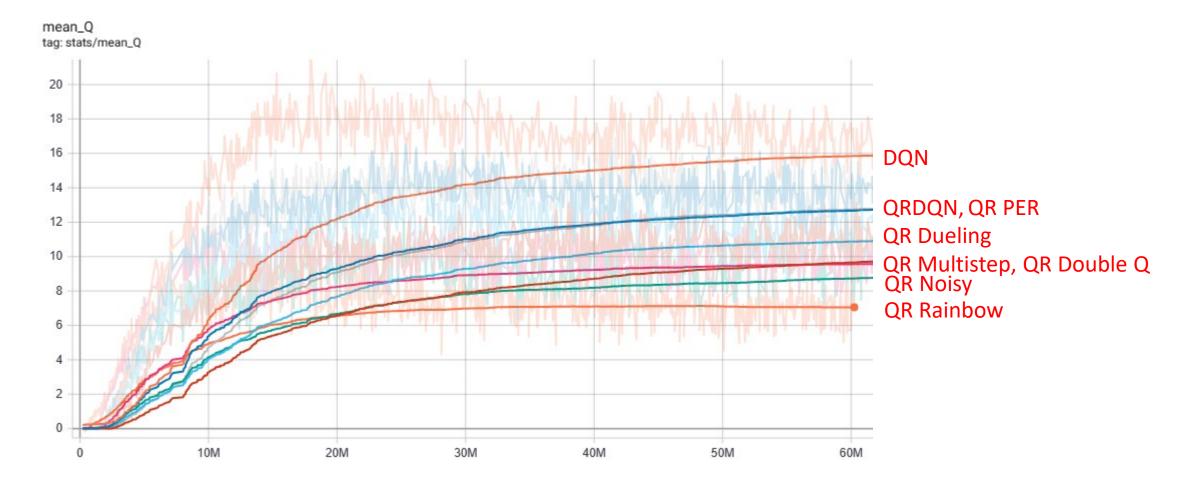




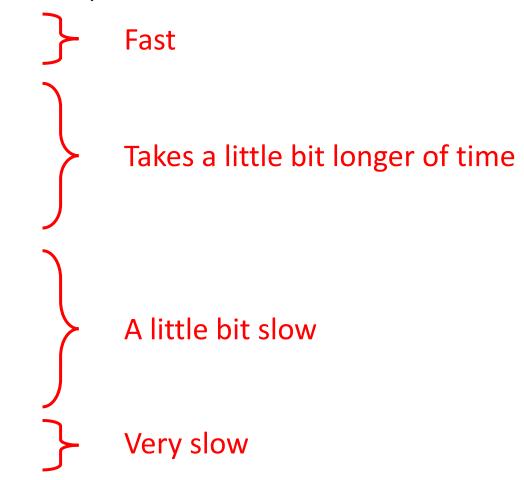
#### • Training score:



• Estimation of Q-value:

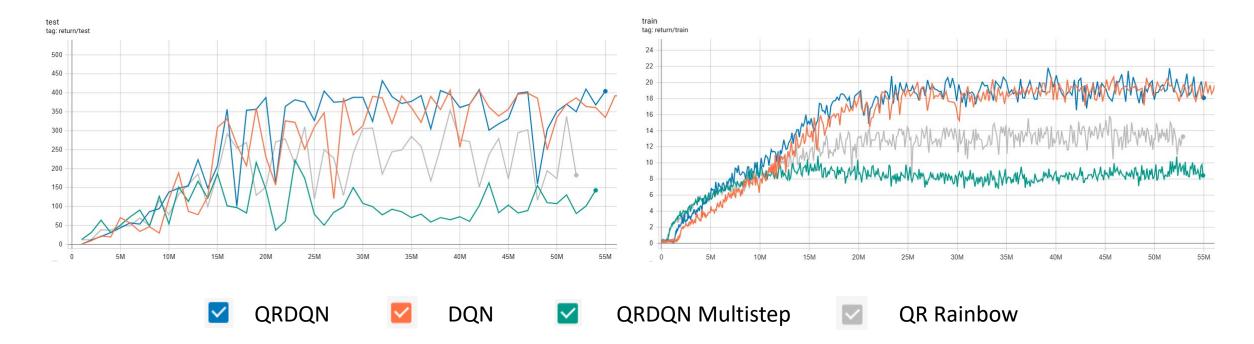


- Training speed (0 to 60M) (may not be accurate):
  - DQN (2d11h)
  - QR Multistep (2d13h18m)
  - QR Double-Q (2d13h24m)
  - QRDQN (2d14h)
  - QR Dueling (2d16h)
  - QR Noisy (2d21h)
  - QR PER (2d22h)
  - QR Rainbow (3d20h)



### Other Issue – Multistep Return

- Some environments may not be suitable for multistep return.
- May need some off-policy corrections. Like Retrace or ACER...
- Breakout:



## Other Issue – Noise while Testing

- Load the best model of QR Noisy.
- Run 1M frames and record the mean return:

	With Noise	Without Noise
Enduro	2143.3	2114.6
MsPacman	3005.95	3180.75

Sample noise while testing doesn't have much impact.

## Other Research – IQN, FQF

QR Rainbow

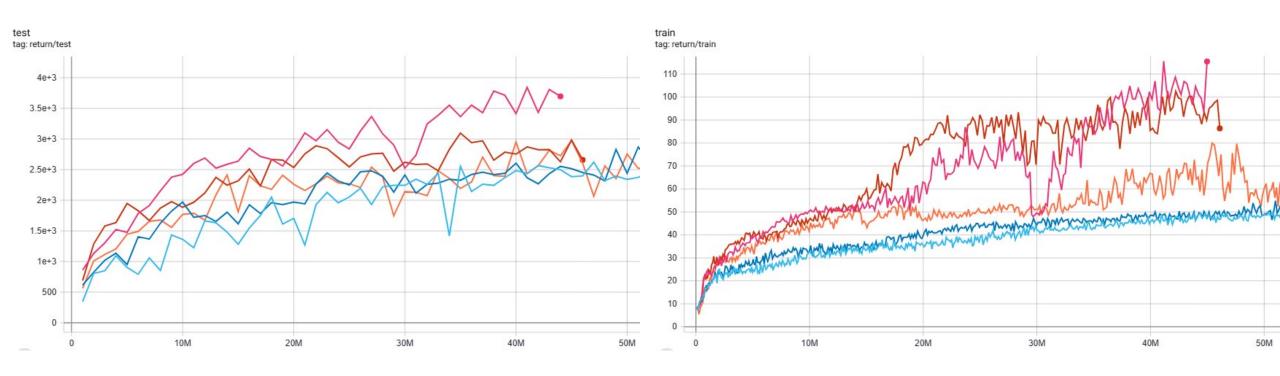
IQN

✓ IQN Rainbow

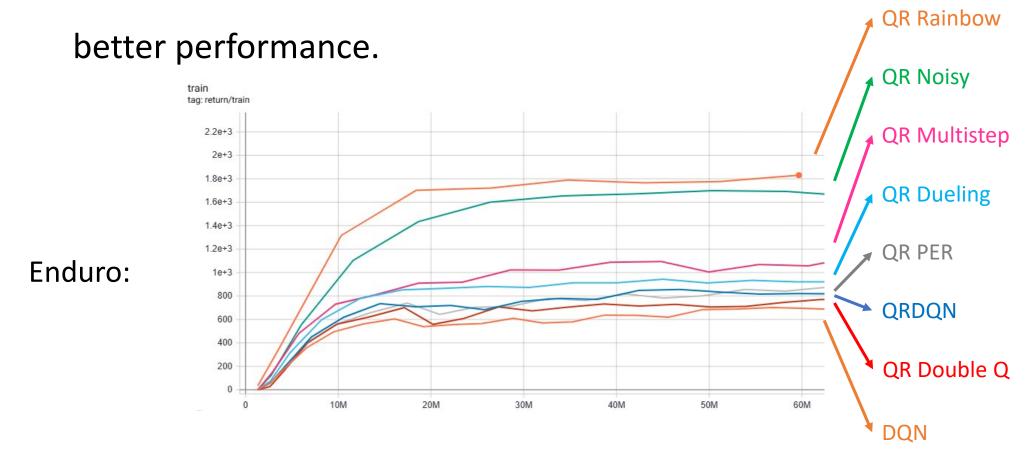
FQF

FQF Rainbow

#### MsPacman:

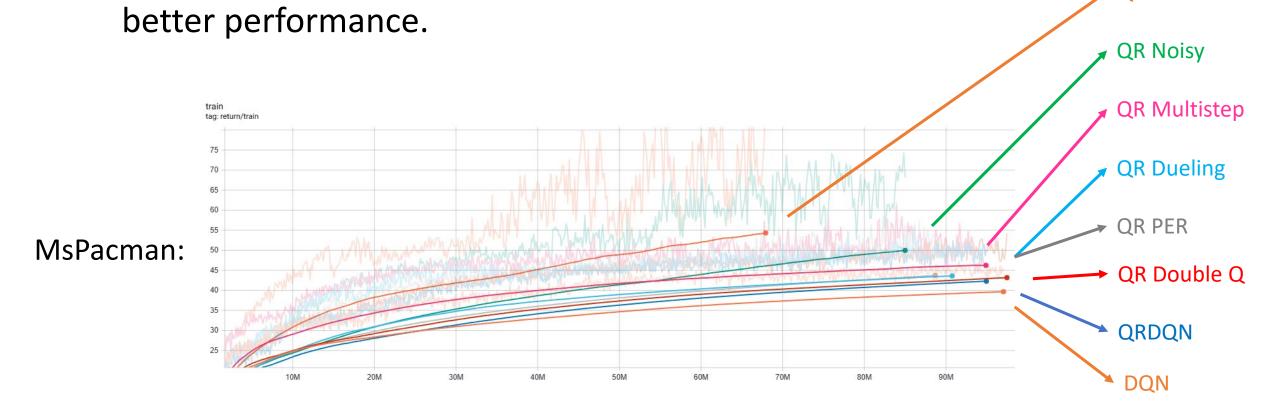


Combining QRDQN with most of the non-distributional methods gets



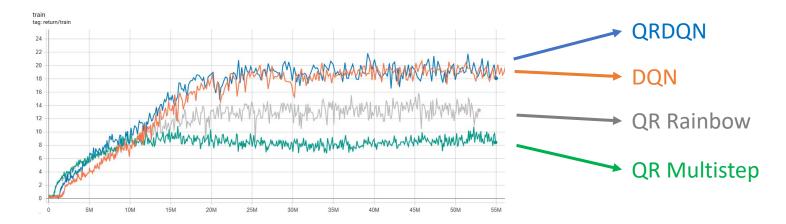
Combining QRDQN with most of the non-distributional methods gets

**QR** Rainbow



- Some environments are not suitable for all methods, so blindly using Rainbow is risky.
- It is important to test and confirm the effectiveness of a method in improving performance before incorporating it.

**Breakout:** 



#### **Further Studies**

- More games, more environments.
- Different kappa (0 or 1) in QRDQN.
- Different N in QRDQN.
- Compare Rainbow with QR Rainbow.
- Add intrinsic motivation (e.g. RND) in QRDQN.
- Risk Sensitive QRDQN.

# Appendix

#### Video

- QR Rainbow plays Enduro:
  - https://youtu.be/yWZy-niGd6U
- QR Rainbow plays MsPacman:
  - https://youtube.com/shorts/Tbbh0zdfwRE?feature=share
- QRDQN plays Breakout:
  - https://youtu.be/TA4eBbyK8Mw

QR Rainbow in Breakout 400

QRDQN Prioritize Experience Replay

✓ QRDQN

QRDQN Double-Q

QRDQN Dueling Network

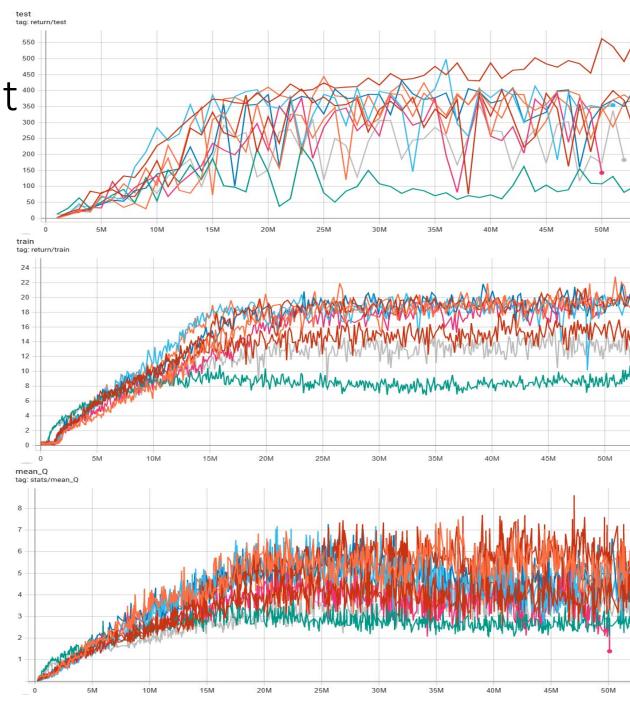
QRDQN Noisy Network

QRDQN Multistep Return

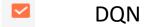
QRDQN Rainbow

DQN

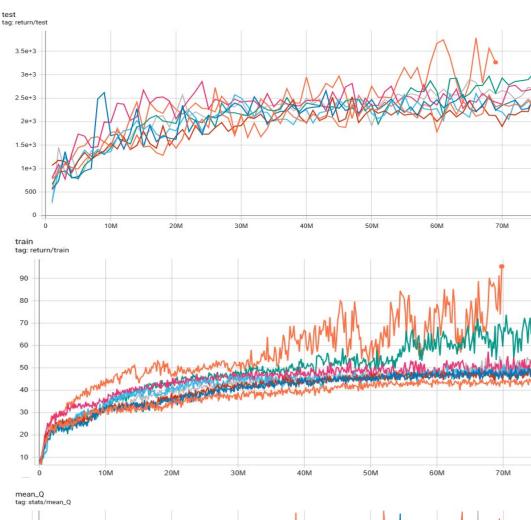
■ QRDQN PER + Double + Dueling

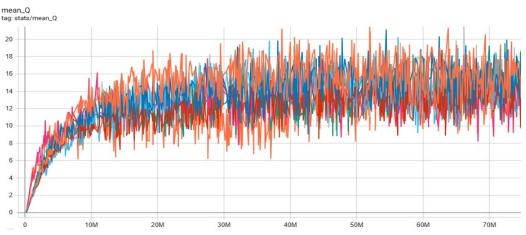


#### QR Rainbow in MsPacman



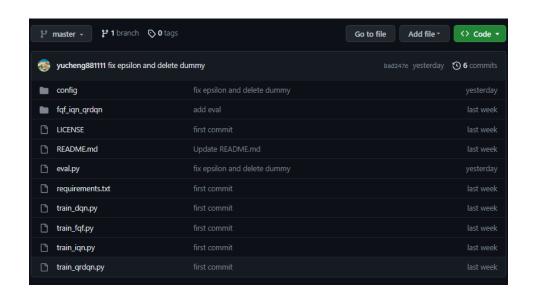
- QRDQN
- QRDQN Double-Q
- QRDQN Dueling Network
- ☑ QRDQN Multistep Return
- QRDQN Noisy Network
  - QRDQN Prioritize Experience Replay
- QRDQN Rainbow

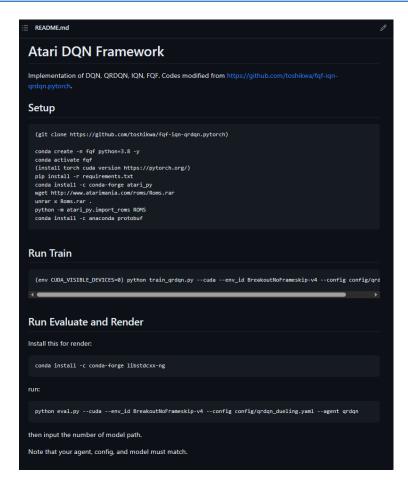




## My GitHub Link

https://github.com/yucheng881111/Atari\_DQN\_Framework





- Codes modified from:
  - https://github.com/toshikwa/fqf-iqn-qrdqn.pytorch
  - Distributional Reinforcement Learning with Quantile Regression | Papers With Code

Code		' Edit
C) DLR-RM/stable-baselines3 Ly Quickstart in	<b>★</b> 5,861	<mark>⊙</mark> PyTorch
facebookresearch/Horizon	<b>★</b> 3,400	○ PyTorch
	<b>★</b> 3,400	O PyTorch
opendilab/DI-engine	<b>★</b> 2,605	O PyTorch
<b>○</b> Kchu/DeepRL_CK	<b>★</b> 165	O PyTorch
🗘 ku2482/fqf-iqn-qrdqn.pytorch	<b>★</b> 135	<b>○</b> PyTorch
ars-ashuha/quantile-regression-dqn	★ 81	<b>○</b> PyTorch
senya-ashukha/quantile-regression-d  • Quickstart in CO Colab	★ 81	O PyTorch

#### Rainbow:

• Hessel, Matteo, et al. "Rainbow: Combining improvements in deep reinforcement learning." Proceedings of the AAAI conference on artificial intelligence. Vol. 32. No. 1. 2018.

#### • QRDQN:

• Dabney, Will, et al. "Distributional reinforcement learning with quantile regression." Proceedings of the AAAI Conference on Artificial Intelligence. Vol. 32. No. 1. 2018.

#### • Multistep Return:

• Hernandez-Garcia, J. Fernando, and Richard S. Sutton. "Understanding multi-step deep reinforcement learning: A systematic study of the DQN target." arXiv preprint arXiv:1901.07510 (2019).

#### Prioritized Experience Replay:

• Schaul, Tom, et al. "Prioritized experience replay." arXiv preprint arXiv:1511.05952 (2015).

#### Double Q-learning:

- Hasselt, Hado. "Double Q-learning." Advances in neural information processing systems 23 (2010).
- Van Hasselt, Hado, Arthur Guez, and David Silver. "Deep reinforcement learning with double q-learning." Proceedings of the AAAI conference on artificial intelligence. Vol. 30. No. 1. 2016.

#### • Dueling Network:

• Wang, Ziyu, et al. "Dueling network architectures for deep reinforcement learning." International conference on machine learning. PMLR, 2016.

#### Noisy Network:

• Fortunato, Meire, et al. "Noisy networks for exploration." arXiv preprint arXiv:1706.10295 (2017).

#### • IQN:

 Dabney, Will, et al. "Implicit quantile networks for distributional reinforcement learning." International conference on machine learning. PMLR, 2018.

#### FQF:

Yang, Derek, et al. "Fully parameterized quantile function for distributional reinforcement learning."
 Advances in neural information processing systems 32 (2019).

#### Risk Sensitive QRDQN:

• Lim, Shiau Hong, and Ilyas Malik. "Distributional Reinforcement Learning for Risk-Sensitive Policies." Advances in Neural Information Processing Systems. 2022.