A Gradient-based Adaptive Learning Framework for Efficient Personal Recommendation

Yue Ning¹ Yue Shi² Liangjie Hong² Huzefa Rangwala³ Naren Ramakrishnan¹

August 27, 2017

¹Virginia Tech

²Yahoo Research. Yue Shi is now with Facebook, Liangjie Hong is now with Etsy.

³George Mason University

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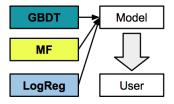
Challenges in Personalized Recommender Systems

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- ► Alleviate "average" experiences for users.
- ► Lack of generic empirical frameworks for different models.
- ▶ Distributed model learning and less access of data.



Example of Personal Models

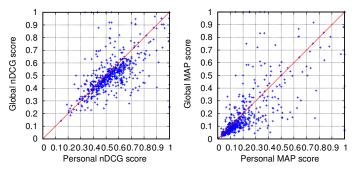


Figure: An example of global and personal models. Left figure showcases the nDCG score of users from global (y-axis) and personal (x-axis) models. (Right: MAP score).

System Framework

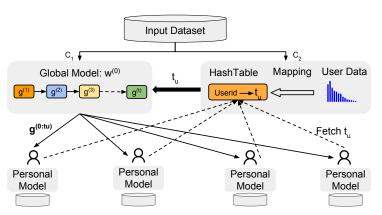


Figure: System Framework. Component C_1 trains a global model. Component C_2 generates a hashtable based on users' data distribution. Users request t_u from C_2 and C_1 returns a subsequence of gradients $g^{(0:t_u)}$ to users.

Adaptation Mechanism

Global update \rightarrow

$$\boldsymbol{\theta}^{(T)} = \boldsymbol{\theta}^{(0)} - \eta \sum_{t=1}^{T} g^{(t)}(\boldsymbol{\theta})$$

Local update \rightarrow

$$\widetilde{\boldsymbol{\theta}}_u = \boldsymbol{\theta}^{(0)} - \eta_1 \sum_{t=1}^{t_u-1} g^{(t)}(\boldsymbol{\theta}) - \eta_2 \sum_{t=t_u}^T g^{(t)}(\boldsymbol{\theta}_u)$$

- ightharpoonup heta: the global model parameter.
- \triangleright θ_{u} : the personal model parameter.
- ▶ *u*: the index for one user.
- ightharpoonup the index of global gradients for user u.
- $ightharpoonup g^{(t)}(\theta)$: global gradients
- $ightharpoonup g^{(t)}(\theta_u)$: personal gradients



How do we decide t_u ?

- Group users into C groups based on their data sizes in descending order.
- ▶ Decide the position $p_u = \frac{i}{C}$,
 - ► C is # groups.
 - \blacktriangleright *i* is the group assignment for user *u*.
 - ▶ the first group (i=1) of users has the most data.
- ▶ Set $t_u = \lfloor T * p_u \rfloor$
 - ► T: total iterations in the global SGD algorithm
 - ► Users with the most data have the earliest stop for global gradients.

Adaptive Logistic Regression

Objective:

$$\min_{\mathbf{w}} L(\mathbf{w}) = f(\mathbf{w}) + \lambda r(\mathbf{w}) \tag{1}$$

- ▶ $f(\mathbf{w})$ is the negative log-likelihood.
- $ightharpoonup r(\mathbf{w})$ is a regularization function.

Adaptation Procedure:

▶ Global update →

$$\widetilde{\mathbf{w}}_{u}^{(0)} = \mathbf{w}^{(0)} - \eta_{1} \sum_{t=1}^{t_{u}-1} g^{(t)}(\mathbf{w})$$
 (2)

▶ Local update →

$$\widetilde{\mathbf{w}}_{u}^{(T)} = \widetilde{\mathbf{w}}_{u}^{(0)} - \eta_{2} \sum_{t=1}^{T-t_{u}} g^{(t)}(\mathbf{w}_{u})$$
(3)

Adaptive Gradient Boosting Decision Tree

Objective:

$$L^{(t)} = \sum_{d}^{N} I(y_d, F_d^{(t-1)} + \rho h^{(t)}) + \Omega(h^{(t)})$$

$$= \sum_{d}^{N} I(y_d, F_d^{(0)} + \rho h^{(0:t)}) + \Omega(h^{(t)})$$
(4)

Adaptation Procedure:

$$\widetilde{F}_{u}^{(0)} = F^{(0)} + \rho h^{(0:t_{u})} \tag{5}$$

$$\widetilde{F}_{u}^{(T)} = \widetilde{F}_{u}^{(0)} + \rho h_{u}^{(t_{u}:T)} \tag{6}$$

Adaptive Matrix Factorization

Objective:

$$\min_{\mathbf{q}_{*}, p_{*}, b_{*}} \sum_{u,i} (r_{ui} - \mu - b_{u} - b_{i} - \mathbf{q}_{u}^{T} \mathbf{p}_{i})
+ \lambda (||\mathbf{q}_{u}||^{2} + ||\mathbf{p}_{i}||^{2} + b_{u}^{2} + b_{i}^{2})$$
(7)

Adaptation Procedure:

$$\widetilde{\mathbf{q}}_{u}^{(0)} = \mathbf{q}_{u}^{(0)} - \eta_{1} \sum_{t=0}^{t_{u}} g^{(t)}(\mathbf{q}_{u}), \widetilde{\mathbf{q}}_{u}^{(T)} = \widetilde{\mathbf{q}}_{u}^{(0)} - \eta_{2} \sum_{t=0}^{T-t_{u}} g^{(t)}(\widetilde{\mathbf{q}}_{u}) \quad (8)$$

$$\widetilde{b}_{u}^{(0)} = b_{u}^{(0)} - \eta_{1} \sum_{k=0}^{t_{u}} g^{(t)}(b_{u}), \widetilde{b}_{u}^{(T)} = \widetilde{b}_{u}^{(0)} - \eta_{2} \sum_{t=0}^{T-t_{u}} g^{(t)}(\widetilde{b}_{u}) \quad (9)$$

Properties

- Generality: The framework is generic to a variety of machine learning models that can be optimized by gradient-based approaches.
- Extensibility: The framework is extensible to be used for more sophisticated use cases.
- ► Scalability: In this framework, the training process of a personal model for one user is independent of all the other users.

Datasets

Table: Dataset Statistics

News Portal				
# users	54845			
# features	351	Movie Ratings		
# click events	2,378,918		Netflix	Movielens
# view events	26,916,620	# users	478920	1721
avg # click events per user	43	# items	17766	3331
avg # events per user	534	sparsity	0.00942	0.039

- ► For LogReg and GBDT: News Portal dataset
- ► For Matrix Factorization: Movie rating datasets (Netflix, Movielens)

Metrics

- ► MAP: Mean Average Precision.
- MRR: Mean Reciprocal Rank.
- ► AUC: Area Under (ROC) Curve.
- ▶ nDCG: Normalized Discounted Cumulative Gain.
- ► RMSE: Root Mean Square Error
- ► MAE: Mean Absolute Error

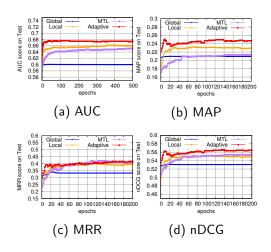
Comparison Methods

Table: Objective functions for different methods.

Model	LogReg				
Global	$\frac{\sum_{d=1}^{N} f(\mathbf{w}) + \lambda \mathbf{w} _2^2}{\sum_{j=1}^{N_u} f(\mathbf{w}_u) + \lambda \mathbf{w}_u _2^2}$				
Local	$\sum_{i=1}^{N_u} f(\mathbf{w}_u) + \lambda \mathbf{w}_u _2^2$				
MTL	$\sum_{j}^{N_{u}} f(\mathbf{w}_{u}) + \frac{\lambda_{1}}{2} \mathbf{w}_{u} - \mathbf{w} ^{2} + \frac{\lambda_{2}}{2} \mathbf{w}_{u} ^{2}$				
Model	GBDT				
Global	$\frac{\sum_{d}^{N} I(y_{d}, F_{d}^{(0)} + \rho h^{(0:t)}) + \Omega(h^{(t)})}{\sum_{i}^{N_{u}} I(y_{i}, F_{i}^{(0)} + \rho h^{(0:t)}) + \Omega(h^{(t)})}$				
Local	$\sum_{j}^{N_u} I(y_j, F_j^{(0)} + \rho h^{(0:t)}) + \Omega(h^{(t)})$				
MTL	-				
Model	MF				
Global	$\sum_{u,i} (r_{ui} - \mu - b_u - b_i - \mathbf{q}_u^T \mathbf{p}_i) + \lambda (\mathbf{q}_u ^2 + \mathbf{p}_i ^2 + b_u^2 + b_i^2)$				
Local	$\left \sum_{i \in N_u} (r_{ui} - \mu - \widetilde{b}_u - \widetilde{b}_i - \widetilde{\mathbf{q}}_u^T \widetilde{\mathbf{p}}_i) + \lambda(\widetilde{\mathbf{q}}_u ^2 + \widetilde{\mathbf{p}}_i ^2 + \widetilde{b}_u^2 + \widetilde{b}_i^2) \right $				
MTL	global + $\lambda_2[(\mathbf{q}_u - \mathbf{q})^2 + (\mathbf{p}_i - \mathbf{p})^2 + (b_u - A_u)^2 + (b_i - A_i)^2]$				

- ► Global: models are trained on all users' data
- ► Local: models are learned locally on per user's data
- ► MTL: users models are averaged by a global parameter.

Ranking Performance - LogReg



- ► AUC, MAP, MRR and nDCG scores on the test dataset with varying training epochs.
- ► The proposed adaptive LogReg models achieve higher scores with fewer epochs.
- Global models perform the worst.

Ranking Performance - GBDT

Table: Performance comparison based on MAP, MRR, AUC and nDCG for GBDT. Each value is calculated from the average of 10 runs with standard deviation.

	Global -GBDT					
#Trees	MAP	MRR	AUC	nDCG		
20	0.2094(1e-3)	0.3617(2e-3)	0.6290(1e-3)	0.5329(6e-4)		
50	0.2137(1e-3)	0.3726(1e-3)	0.6341(1e-3)	0.5372(6e-4)		
100	0.2150(8e-3)	0.3769(1e-3)	0.6356(8e-4)	0.5392(6e-4)		
200	0.2161(5e-4)	0.3848(1e-3)	0.6412(6e-4)	0.5415(5e-4)		
	Local-GBDT					
#Trees	MAP	MRR	AUC	nDCG		
20	0.2262(2e-3)	0.4510(5e-3)	0.6344(3e-3)	0.5604(2e-3)		
50	0.2319(2e-3)	0.4446(4e-3)	0.6505(2e-3)	0.5651(2e-3)		
100	0.2328(1e-3)	0.4465(5e-3)	0.6558(2e-3)	0.5651(2e-3)		
200	0.2322(2e-3)	0.4431(2e-3)	0.6566(1e-3)	0.5649(1e-3)		
	Adaptive-GBDT					
#Trees	MAP	MRR	AUC	nDCG		
20 + 50	0.2343 (2e-3)	0.4474(4e-3)	0.6555(2e-3)	0.5661(2e-3)		
50 + 50	0.2325(2e-3)	0.4472(1e-4)	0.6561(8e-4)	0.5666 (6e-4)		
10 + 100	0.2329(2e-3)	0.4423(3e-3)	0.6587 (1e-3)	0.5650(3e-3)		

Ranking Performance - GBDT

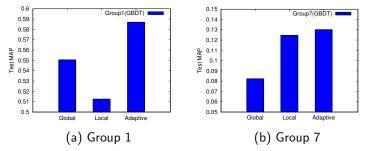
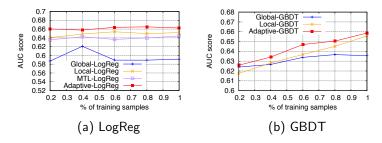


Figure: MAP Comparison of Group 1 (least) and Group 7 (most) for GBDT methods.

- ► MAP score for the groups of users with least data (Group 1) and most data (Group 7) for GBDT models.
- Adaptive-GBDT outperform both global and local GBDT models in terms of MAP for all groups of users.

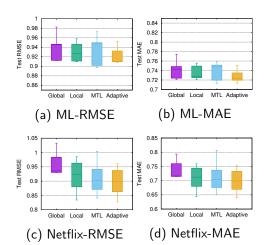
Ranking Performance - LogReg vs GBDT



- ► AUC score for Global-GBDT, Local-GBDT, and Adaptive-GBDT with # of training samples from 20% to 100%.
- ► On average of AUC, Adaptive-GBDT performs better than other methods.
- With the increase of training samples, GBDT based methods tend to perform better while LogReg methods achieve relatively stable scores.



Results - MF



- ► RMSE and MAE on MovieLens(ML) and Netflix datasets.
- The quartile analysis of the group level RMSE and MAE for different MF models.
- ► Gold: Adaptive-MF

Summary

- ► Effectively and efficiently build personal models that lead to improved recommendation performance over either the global model or the local model.
- ► Adaptively learn personal models by **exploiting the global gradients** according to **individuals characteristic**.
- Our experiments demonstrate the usefulness of our framework across a wide scope, in terms of both model classes and application domains.

Thank you! Q&A