

## Part 1: Gaussian Filtering

1.boxfilter(n)

(1) n = 3

```
[[0.33333333 0.33333333 0.33333333]
 [0.33333333 0.33333333 0.33333333]
 [0.33333333 0.33333333 0.33333333]]
```

(2) n= 4

```
Traceback (most recent call last):
  File "A1final.py", line 18, in <module>
    print(boxfilter(n))
  File "A1final.py", line 10, in boxfilter
    assert mod != 0, "Dimension must be odd."
AssertionError: Dimension must be odd.
```

(3) n = 5

```
[[0.2 0.2 0.2 0.2 0.2]
 [0.2 0.2 0.2 0.2 0.2]
 [0.2 0.2 0.2 0.2 0.2]
 [0.2 0.2 0.2 0.2 0.2]
 [0.2 0.2 0.2 0.2 0.2]]
```

2.gauss1d(sigma)

(1)sigma = 0.3

```
[0.00141816 0.99716368 0.00141816]
```

(2)sigma = 0.5

```
[4.99999916e-01 7.61498859e-09 1.52951135e-07 7.61498859e-09
 4.99999916e-01]
```

(3)sigma = 1

```
[0.12388227 0.1321298 0.07528529 0.33740527 0.07528529 0.1321298
 0.12388227]
```

(4)  $\sigma = 2$

```
[0.06904283 0.06904283 0.06904283 0.06904283 0.06905968 0.06093008
 0.18767786 0.06093008 0.06905968 0.06904283 0.06904283 0.06904283
 0.06904283]
```

```
3.sigam = 3
```



5. Since the expression can be write to the form of two identical function for x and for y multiply together.

$$G_{\sigma}(x, y) = \frac{1}{2\pi\sigma^2} \exp^{-\frac{x^2+y^2}{2\sigma^2}}$$

$$= \left( \frac{1}{\sqrt{2\pi}\sigma} \exp^{-\frac{x^2}{2\sigma^2}} \right) \left( \frac{1}{\sqrt{2\pi}\sigma} \exp^{-\frac{y^2}{2\sigma^2}} \right)$$

function of x

function of y

We can simply just implement a `gauss1d(sigma)` function and for each pixel(x,y), apply it to x and y separately, then multiply the result together to get the 2d gaussian filter. By doing this our runtime original from  $m^2 \cdot n^2$ , improve to  $2 \cdot m \cdot n^2$  (where m stand for the height of filter, n stand for the height of pixel)

Part 2:  
1.sigam = 3



2.sigam = 3



3.sigam = 3



sigam = 2



sigam = 3

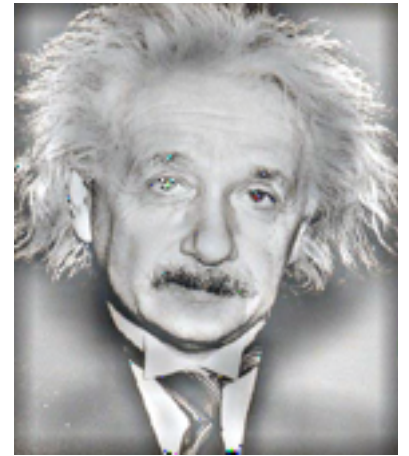
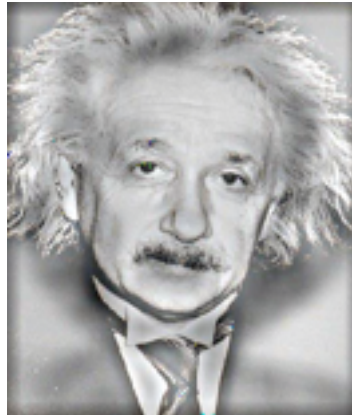
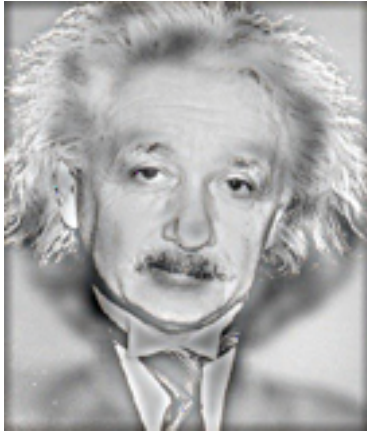


sigam = 4





$\sigma = 2,3,4$



$\sigma = 2,3,4$



sigam = 4, 5,6









