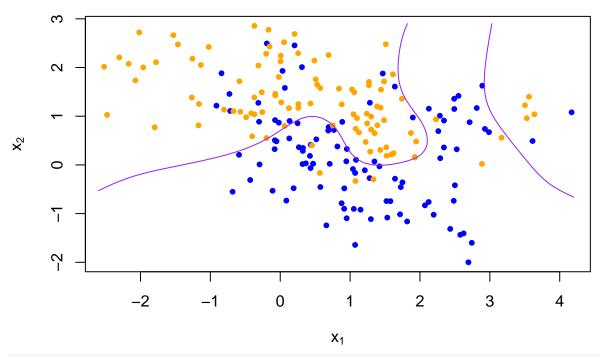
Homework 1

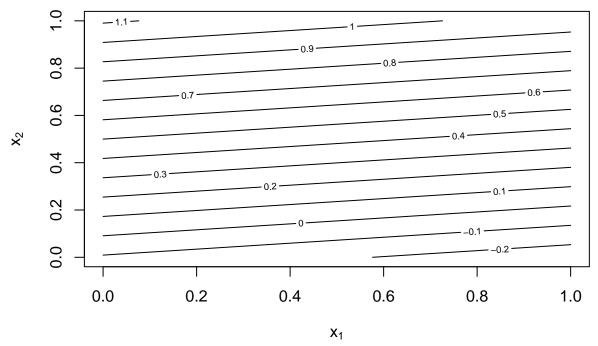
Yue Guo

January 22, 2020

Rewrite code with lm()

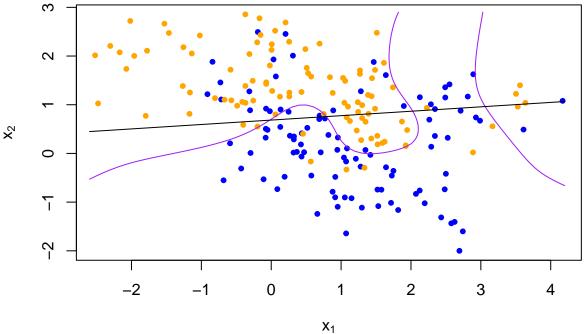
```
library('class')
library('dplyr')
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
## load binary classification example data from author website
## 'ElemStatLearn' package no longer available
load(url('https://web.stanford.edu/~hastie/ElemStatLearn/datasets/ESL.mixture.rda'))
dat <- ESL.mixture
plot_mix_data <- expression({</pre>
  plot(dat$x[,1], dat$x[,2],
       col=ifelse(dat$y==0, 'blue', 'orange'),
       pch=20,
       xlab=expression(x[1]),
       ylab=expression(x[2]))
  ## draw Bayes (True) classification boundary
  prob <- matrix(dat$prob, length(dat$px1), length(dat$px2))</pre>
  cont <- contourLines(dat$px1, dat$px2, prob, levels=0.5)</pre>
  rslt <- sapply(cont, lines, col='purple')</pre>
})
eval(plot_mix_data)
```



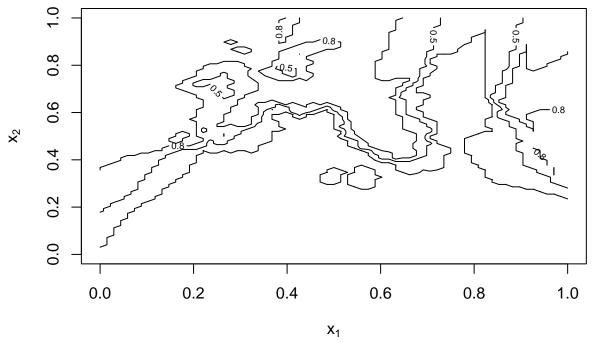


find the contours in 2D space such that lc_pred == 0.5
lc_cont <- contourLines(dat\$px1, dat\$px2, lc_pred, levels=0.5)

plot data and decision surface
eval(plot_mix_data)
sapply(lc_cont, lines)</pre>

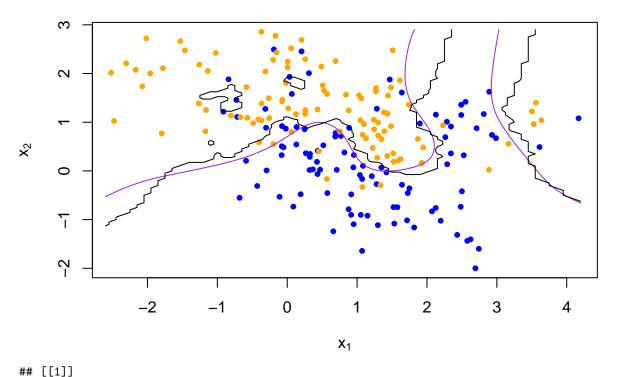


[[1]]
NULL
fit knn classifier
use 5-NN to estimate probability of class assignment



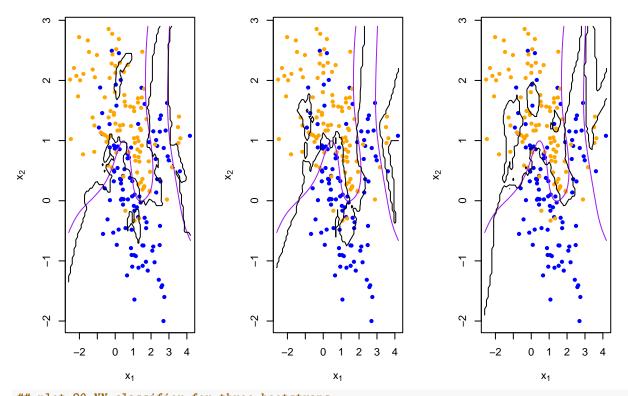
```
## find the contours in 2D space such that knn_pred == 0.5
knn_cont <- contourLines(dat$px1, dat$px2, knn_pred, levels=0.5)

## plot data and decision surface
eval(plot_mix_data)
sapply(knn_cont, lines)</pre>
```



```
## NULL
## [[2]]
## NULL
##
## [[3]]
## NULL
##
## [[4]]
## NULL
##
## [[5]]
## NULL
\hbox{\it \#\# do bootstrap to get a sense of variance in decision surface}\\
resample <- function(dat) {</pre>
  idx <- sample(1:length(dat$y), replace = T)</pre>
  dat$y <- dat$y[idx]</pre>
  dat$x <- dat$x[idx,]</pre>
  return(dat)
}
## plot linear classifier for three bootstraps
par(mfrow=c(1,3))
for(b in 1:3) {
  datb <- resample(dat)</pre>
  ## fit model to mixture data and make predictions
  lc_beta <- fit_lc(datb$y, datb$x)</pre>
  lc_pred <- predict_lc(datb$xnew, lc_beta)</pre>
  ## reshape predictions as a matrix
  lc_pred <- matrix(lc_pred, length(datb$px1), length(datb$px2))</pre>
```

```
## find the contours in 2D space such that lc_pred == 0.5
  lc_cont <- contourLines(datb$px1, datb$px2, lc_pred, levels=0.5)</pre>
  ## plot data and decision surface
  eval(plot_mix_data)
  sapply(lc_cont, lines)
}
×2
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               0
                1
                    2
                      3
                                         -2
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                                                                               0
                                                                                 1
                                                                                     2 3
                                                                                 X<sub>1</sub>
                                                 x_1
## plot 5-NN classifier for three bootstraps
par(mfrow=c(1,3))
for(b in 1:3) {
  datb <- resample(dat)</pre>
  knn_fit <- knn(train=datb$x, test=datb$xnew, cl=datb$y, k=5, prob=TRUE)</pre>
  knn_pred <- attr(knn_fit, 'prob')</pre>
  knn_pred <- ifelse(knn_fit == 1, knn_pred, 1-knn_pred)</pre>
  ## reshape predictions as a matrix
  knn_pred <- matrix(knn_pred, length(datb$px1), length(datb$px2))</pre>
  ## find the contours in 2D space such that knn_pred == 0.5
  knn_cont <- contourLines(datb$px1, datb$px2, knn_pred, levels=0.5)</pre>
  ## plot data and decision surface
  eval(plot_mix_data)
  sapply(knn_cont, lines)
}
```



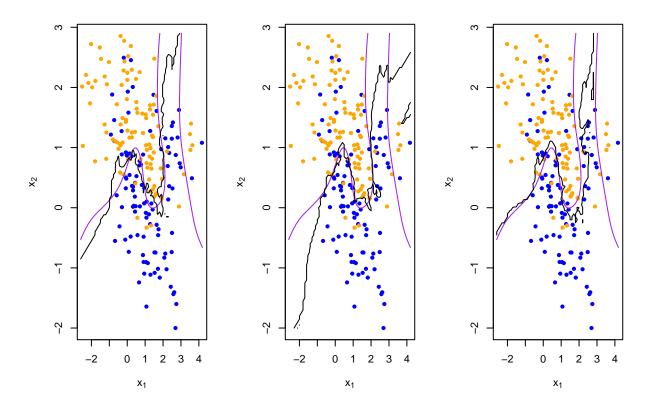
```
## plot 20-NN classifier for three bootstraps
par(mfrow=c(1,3))
for(b in 1:3) {
    datb <- resample(dat)

    knn_fit <- knn(train=datb$x, test=datb$xnew, cl=datb$y, k=20, prob=TRUE)
    knn_pred <- attr(knn_fit, 'prob')
    knn_pred <- ifelse(knn_fit == 1, knn_pred, 1-knn_pred)

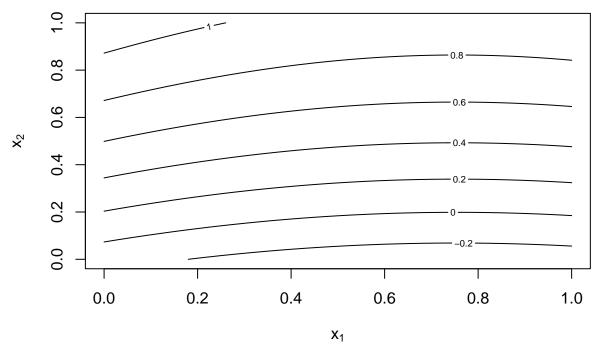
## reshape predictions as a matrix
    knn_pred <- matrix(knn_pred, length(datb$px1), length(datb$px2))

## find the contours in 2D space such that knn_pred == 0.5
    knn_cont <- contourLines(datb$px1, datb$px2, knn_pred, levels=0.5)

## plot data and decision surface
eval(plot_mix_data)
sapply(knn_cont, lines)
}</pre>
```

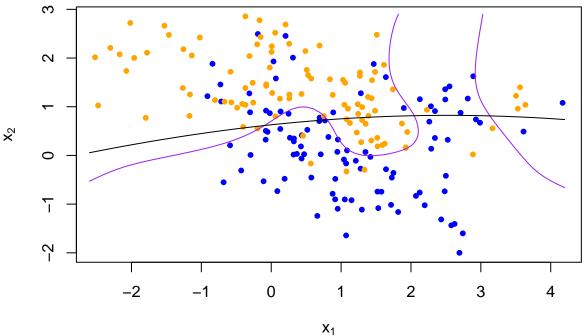


Use squared x to fit the data



```
## find the contours in 2D space such that lc_pred == 0.5
lc_cont_new <- contourLines(dat$px1, dat$px2, lc_pred_new, levels=0.5)

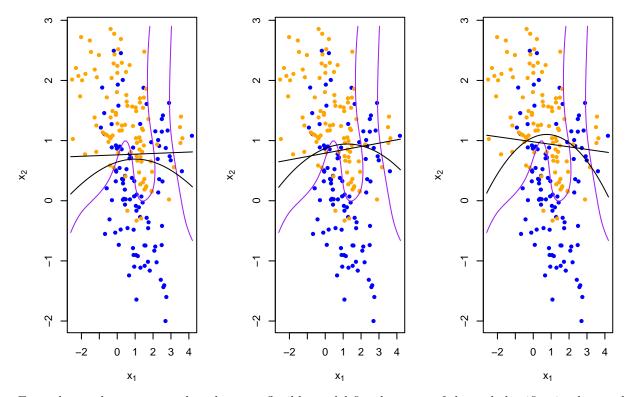
## plot data and decision surface
eval(plot_mix_data)
sapply(lc_cont_new, lines)</pre>
```



```
## NULL
## do bootstrap to get a sense of variance in decision surface
resample <- function(dat) {</pre>
```

[[1]]

```
idx <- sample(1:length(dat$y), replace = T)</pre>
  dat$y <- dat$y[idx]</pre>
  dat$x <- dat$x[idx,]</pre>
  return(dat)
}
## plot linear classifier for three bootstraps
par(mfrow=c(1,3))
for(b in 1:3) {
  datb <- resample(dat)</pre>
  ## fit model to mixture data and make predictions
  lc_beta_new <- fit_lc_new(datb$y, datb$x)</pre>
  lc_pred_new <- predict_lc_new(datb$xnew, lc_beta_new)</pre>
  ## reshape predictions as a matrix
  lc_pred_new <- matrix(lc_pred_new, length(datb$px1), length(datb$px2))</pre>
  ## find the contours in 2D space such that lc_pred == 0.5
  lc_cont_new <- contourLines(datb$px1, datb$px2, lc_pred_new, levels=0.5)</pre>
  lc_beta <- fit_lc(datb$y, datb$x)</pre>
  lc_pred <- predict_lc(datb$xnew, lc_beta)</pre>
  ## reshape predictions as a matrix
  lc_pred <- matrix(lc_pred, length(datb$px1), length(datb$px2))</pre>
  ## find the contours in 2D space such that lc_pred == 0.5
  lc_cont <- contourLines(datb$px1, datb$px2, lc_pred, levels=0.5)</pre>
  ## plot data and decision surface
  eval(plot_mix_data)
  sapply(lc_cont_new, lines)
  sapply(lc_cont, lines)
```



From the result we can see that the more flexible model fits the curve of the real classification better, but from the results of bootstrap, the curvature of different training sets varies greatly, more unstable. Therefore, it has smaller bias and larger variance.