

# Foundations of Reinforcement Learning

## Introduction

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# **Outline**

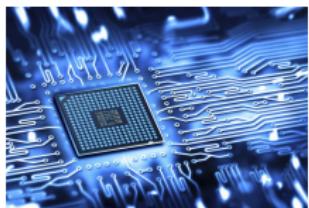
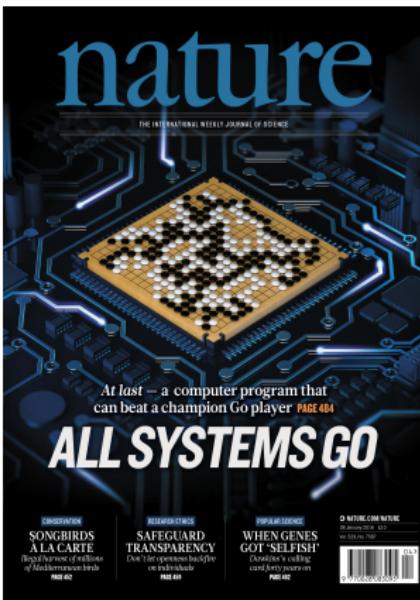
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Introduction

Logistics

# Recent successes in reinforcement learning (RL)

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*RL holds great promise in the next era of artificial intelligence.*

# Supervised learning

Given training data, make prediction on unseen data:



Primarily deal with **pattern recognition**

# Reinforcement learning

In RL, an agent learns by interacting with an environment.

- no training data
- maximize total rewards
- trial-and-error
- sequential and online



Deal with **decision making**, sometimes with constraints

# Sequential decision making

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*“Those who cannot remember the past are condemned to repeat it.”*

—George Santayana

- Games
- Robotics navigation and control
- Pricing and supply chain management
- Recommendation systems
- Portfolio optimization

Learn from past to predict and optimize future performance

# Challenges of RL

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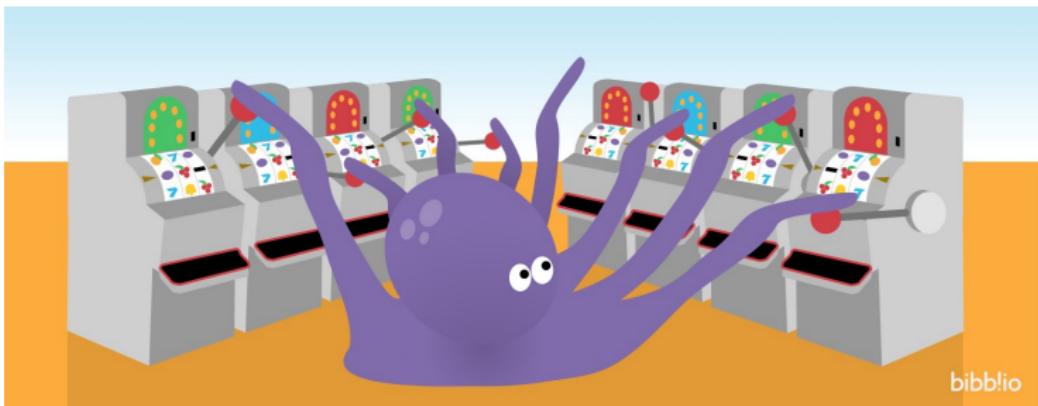
- explore or exploit: unknown or changing environments
- credit assignment problem: delayed rewards or feedback
- enormous state and action space
- nonconvex optimization



# Multi-arm bandit

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Which slot machine will give me the most money?



# Learning the best arm

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Can we **learn** which slot machine gives the most money?



\$1  
\$0  
\$0



\$1  
\$4  
\$0  
\$2  
\$1  
\$3  
\$5



\$1  
\$0  
\$1  
\$2

# Learning the best arm via trial-and-error

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Which arm do I pick next, so that I maximize my reward over time?



\$1  
\$0  
\$0

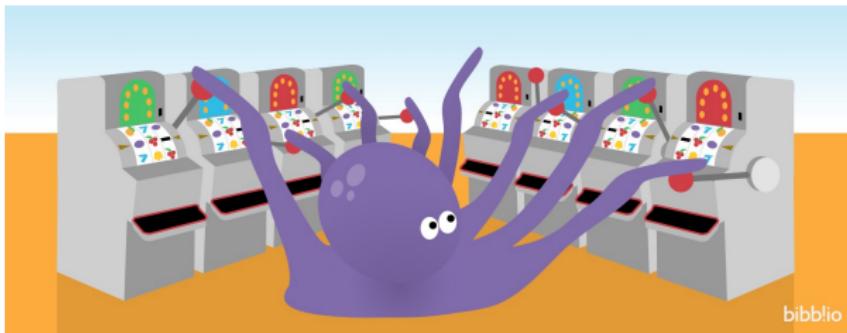


\$1  
\$4  
\$0  
\$2  
\$1  
\$3  
\$5



\$1  
\$0  
\$1  
\$2  
\$12  
\$11

# Exploration-exploitation trade-off



Which arm should I play?

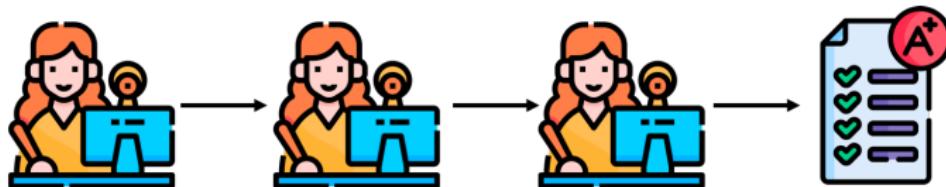
- Best arm observed so far? (exploitation)
- Or should I look around to try and find a better arm? (exploration)

We need **both** in order to maximize the total reward.

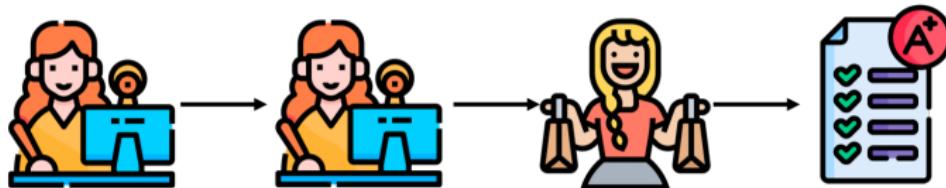
# Credit assignment problem

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What is the action that leads to the desired outcome?

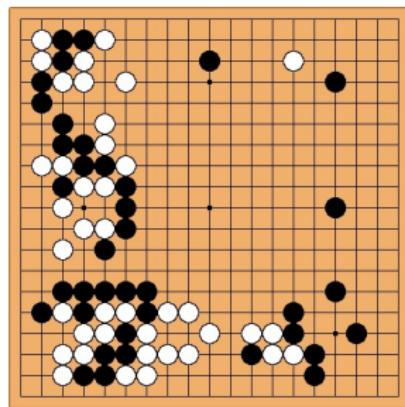


What if....



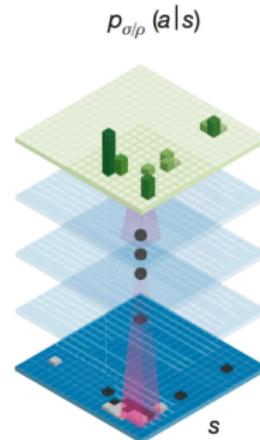
# Enormous problem size and function approximation

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$$S \approx 2 \cdot 10^{170}$$

Policy network



Value network

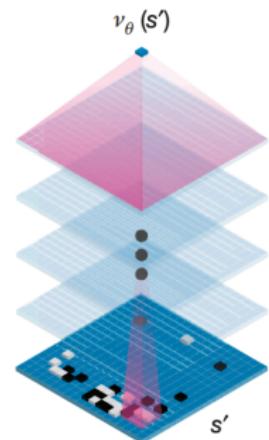
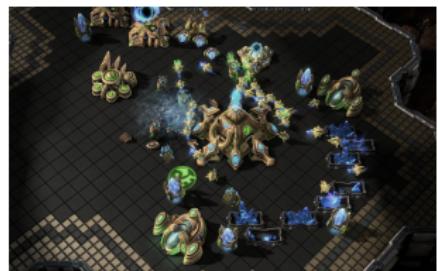


Figure credit: Alphago

# Multi-agent RL

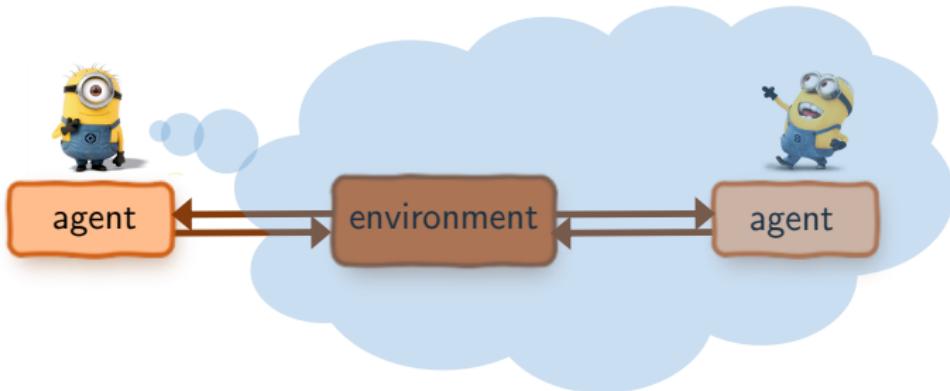
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*To collaborate or to compete, that is the question.*

# Challenges in MARL: nonstationarity

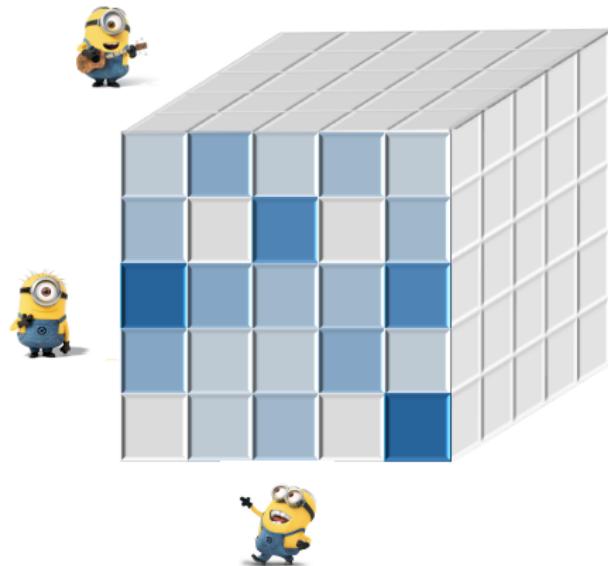
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From a single-agent perspective:  
the environment is **time-varying** and **nonstationary!**

# Challenges in MARL: curse of multiple agents

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The explosion of choices:  
The joint action space grows **exponentially** with the agents!

# Partial observability in RL

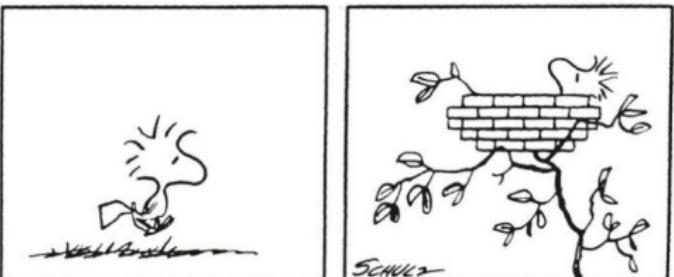
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# Goal of this course

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- **Not** a deep RL course
- Aim to build the “foundations”
- 800-level course: research-oriented
- models, algorithms and their analyses



# Sample efficiency

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Collecting data samples might be expensive or time-consuming



clinical trials



autonomous driving



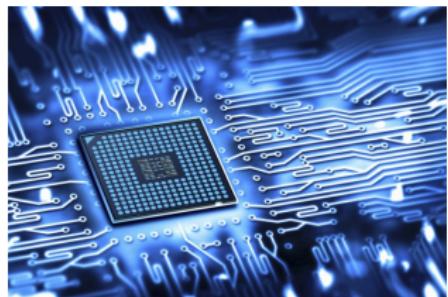
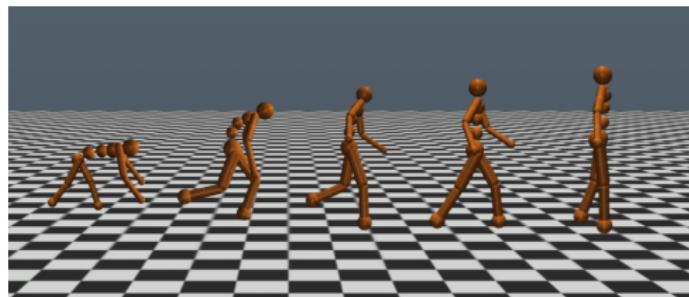
online ads

Calls for design of sample-efficient RL algorithms!

# Computational efficiency

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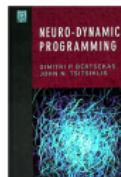
Running RL algorithms might take a long time and space



*many CPUs / GPUs / TPUs + computing hours*

Calls for computationally efficient RL algorithms!

# From asymptotic to non-asymptotic analyses

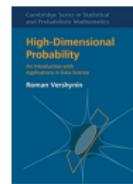


An Analysis of Temporal-Difference Learning with Function Approximation  
John N. Tsiatis, Member, IEEE, and Srivatsa Va Roy  
IEEE Transactions on Automatic Control, Vol. 46, No. 1, MAY 2001  
© 2000 Society for Industrial and Applied Mathematics  
Ergodicity Conditions for Stochastic Approximation and Reinforcement Learning  
V. S. DEDKOV<sup>a</sup> AND E. P. MENOY<sup>b</sup>

asymptotic analysis



finite-time &  
finite-sample analysis



Reinforcement Learning:  
Theory and Algorithms

Alekh Agarwal Nan Jiang Sham M. Kakade Wen Sun

December 9, 2020

1989

2020

Non-asymptotic analyses are key to understand sample and computational efficiency in modern RL.

# **Logistics**

# Basic information

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- Tue/Thu: 3:30 – 4:50 pm
- Instructor's office hours: Wed 1 – 2pm, PH B25
- TA's office hours: Jiin Woo, Thu 1 – 2pm, CIC 4117 Bellefield
- Course website:  
<https://users.ece.cmu.edu/~yuejiec/ece18813B.html>
- Piazza and gradescope.

## Why you **should** consider taking this course

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- There will be quite a few THEOREMS and PROOFS ...
  - Promote deeper understanding of scientific/engineering results
- Nonrigorous / heuristic from time to time
  - “Nonrigorous” but grounded in rigorous theory
  - Help develop intuition
- No exams!

# Tentative topics

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- Multi-arm bandit
- Markov decision processes
- RL with a generative model
- Online RL
- Offline RL
- Policy optimization
- Actor critic
- Function approximation and representation learning
- Multi-agent RL
- Partially-observed MDP

# Useful references

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We recommend these books, but will not follow them closely ...

- Reinforcement Learning: Theory and Algorithms (draft), by Alekh Agarwal, Nan Jiang, Sham M. Kakade, Wen Sun
- Reinforcement learning: An introduction, by Richard S. Sutton, Andrew G. Barto
- Reinforcement learning and optimal control, by Dimitri P. Bertsekas
- Bandit Algorithms, by Tor Lattimore, Csaba Szepesvari

More references will be provided at each lecture.

# Prerequisites

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- linear algebra
  - probability
  - a programming language (e.g. Matlab, Python, ...)
  - basic optimization
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- *Concentration inequalities* are a plus, but not necessary

# Grading

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- Homeworks (20%): ~2 problem sets
  - Use gradescope for submission and grading.
- Midterm Paper Presentations (25%)
  - An in-class presentation on a selected paper from a given pool is arranged in lieu of the midterm.
  - About 15-20 min each, highlight at least one key result
- Final project (55%)

# Final project

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Two forms

- literature review on a research **topic** (individual)
- original research (can be individual or a group of two)
  - *You are strongly encouraged to combine it with your own research*

Three milestones

- Proposal (March 23): up to 2 pages (NeurIPS format). Plan early! Use midterm paper as a planner.
- In-class presentation (last week of class)
- Report (May 14): up to 5 pages with unlimited appendix

Enjoy Yourself