

Solutions to Midterm Examination

February 24, 2014

1. Consider a database consisting of the following two tables with obvious meanings

course(course_id, course_name, no_credit, capacity),
 registration(student_id, course_id, grade).

Note that the underlined attributes are keys of the tables. Write triggers to impose the constraint that no student can register a course that is not offered by the university (i.e., not recorded in course table). (Assume that no foreign key constraints are enforced in the database.)

One needs to (1) give a list of events that must be monitored for imposing the constraint, and (2) present one trigger for any event in (1). [30]

Solution: To enforce the given constraint, the following events must be monitored:

- INSERT or UPDATE on registration
- DELETE or UPDATE on course

A trigger to monitor the first event is given below.

```

CREASTE TRIGGER foregin_key_on_registration
BEFORE INSERT OR UPDATE ON registration
FOR EACH ROW
DECLARE counter INT
BEGIN
    SELECT COUNT(*) INTO counter
    FROM   course
    WHERE  course_id = NEW.course_id;

    IF (counter < 1 )
        THEN raise_exception('the foreign key constraint violated
END;
```

2. Consider a relation schema $R = ABCDE$, functional dependencies

$B \rightarrow E$
 $E \rightarrow A$
 $A \rightarrow D$
 $D \rightarrow E$

and a decomposition $D = \{AB, BCD, ADE\}$ of R . Is D dependency preserving? Explain. [5]

Solution: Yes, D is dependency preserving. This is because the given set of FDs is equivalent to $F' = \{B \rightarrow A, E \rightarrow A, A \rightarrow D, D \rightarrow E\}$, and F' is dependency preserving with respect to D .

3. Consider the database schema $R = ABCDEF$, and the following FDs:

$ABF \rightarrow C$
 $CF \rightarrow B$
 $CD \rightarrow A$
 $BD \rightarrow AE$
 $C \rightarrow F$
 $B \rightarrow F$

- (a) Find a minimal cover of the given set of FDs. Show all steps.

Solution:

- i. Right reducing: Replace $BD \rightarrow AE$ with $BD \rightarrow A$ and $BD \rightarrow E$.

- ii. Left reducing: $ABF \rightarrow C$ can be replaced with: $AB \rightarrow C$ while $CF \rightarrow B$ can be replaced with: $C \rightarrow B$. This is because (1) $AB \rightarrow C$ is entailed by $ABF \rightarrow C$ and $B \rightarrow F$; and $C \rightarrow B$ is entailed by $CF \rightarrow B$ and $C \rightarrow F$; (2) $AB \rightarrow C$ entails $ABF \rightarrow C$ and $C \rightarrow B$ entails $CF \rightarrow B$; and therefore (3) the set $AB \rightarrow C, B \rightarrow F$ is equivalent to $ABF \rightarrow C, B \rightarrow F$; and $C \rightarrow B, C \rightarrow F$ is equivalent to $CF \rightarrow B, C \rightarrow F$.

That is, after Left-reducing, we have

$AB \rightarrow C$
 $C \rightarrow B$
 $CD \rightarrow A$
 $BD \rightarrow A$
 $BD \rightarrow E$
 $C \rightarrow F$
 $B \rightarrow F$

- iii. Eliminate redundant FDs: $C \rightarrow F$ is entailed by $C \rightarrow B$ and $B \rightarrow F$, while $CD \rightarrow A$ is entailed by $C \rightarrow B$ and $BD \rightarrow A$. Therefore, a minimal cover is

$AB \rightarrow C$
 $C \rightarrow B$
 $BD \rightarrow A$
 $BD \rightarrow E$
 $B \rightarrow F$

- (b) Construct a join lossless, dependency preserving, and 3NF decomposition of R . [20]

Solution: The 3NF decomposition that corresponds to this minimal cover is $\{ABC, BDAE, BF\}$. Note that $BDAE$ is a super key of R .

4. Consider the database schema $R = ABCDE$ and a set of MVDs $M = \{AB \twoheadrightarrow D\}$. Prove or disprove that $D = \{ABE, ABCD\}$ is a join lossless decomposition of R with respect to M . Note that a proof must follow the definitions of the join lossless and MVD while a counter example is sufficient for a disproof. [5]

Solution: D is not a join lossless decomposition of R , as demonstrated in the following counter example.

Consider the following table r .

A	B	C	D	E
a	b	c1	d	e1
a	b	c2	d	e2

Obviously, r satisfies $M = \{AB \twoheadrightarrow D\}$ but $r \neq \pi_{ABE} \bowtie \pi_{ABCD}$ as demonstrated below.

$$\pi_{ABE} \bowtie \pi_{ABCD} = \begin{array}{|c|c|c|} \hline \mathbf{A} & \mathbf{B} & \mathbf{E} \\ \hline a & b & e1 \\ \hline a & b & e2 \\ \hline \end{array} \bowtie \begin{array}{|c|c|c|c|} \hline \mathbf{A} & \mathbf{B} & \mathbf{C} & \mathbf{D} \\ \hline a & b & c1 & d \\ \hline a & b & c2 & d \\ \hline \end{array} = \begin{array}{|c|c|c|c|c|} \hline \mathbf{A} & \mathbf{B} & \mathbf{C} & \mathbf{D} & \mathbf{E} \\ \hline a & b & c1 & d & e1 \\ \hline a & b & c1 & d & e2 \\ \hline a & b & c2 & d & e1 \\ \hline a & b & c2 & d & e2 \\ \hline \end{array}$$

5. Consider the following database schema with obvious meanings:

prof(p_id, p_name, department)
course(c_code, department, c_name)
teaching(p_id, c_code, term)

and the following query

```
SELECT c.c_name, p.p_name
FROM   prof p, teaching t, course c
WHERE  t.term = 'Fall 2011' AND p.department = 'cs' AND
       p.p_id = t.p_id AND t.c_code = c.c_code
```

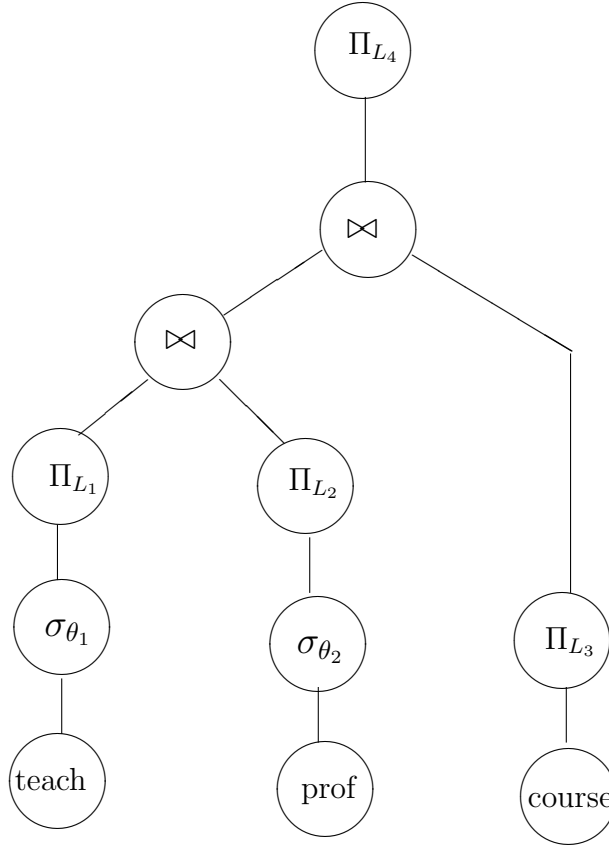
- (a) Show the unoptimized relational algebra expression that corresponding to the above SQL query.

Solution: $\Pi_{course.c_name, prof.p_name} \sigma_{\theta} (prof \bowtie teaching \bowtie course)$

where θ represents $teaching.term = Fall\ 2007 \wedge prof.department = cs$.

- (b) Draw the optimized query tree (i.e., with all selections and/or projections pushed as far down as possible) for the expression. [20]

Solution:



Where

θ_1 : term = 'Fall 2007'

θ_2 : department = 'CS'

L_1 : p_id, c_code

L_2 : p_id, p_name

L_3 : c_code, c_name

L_4 : course.c_name, prof.p_name