

ANNOUNCEMENT OF WINNERS

of the eighty-second competition held on December 4, 2021

In each of the following categories, the listing is in alphabetical order

THE PUTNAM FELLOWS — THE FIVE HIGHEST-RANKING INDIVIDUALS

Each receives an award of \$2,500

Andrew Gu	Massachusetts Institute of Technology
Michael Ren	Massachusetts Institute of Technology
Edward Wan	Massachusetts Institute of Technology
Shengtong Zhang	Massachusetts Institute of Technology
Daniel Zhu	Massachusetts Institute of Technology

THE NEXT TEN HIGHEST-RANKING INDIVIDUALS

Each receives an award of \$1,000

Ankit Bisain	Massachusetts Institute of Technology
Quanlin Chen	Stanford University
Tianze Jiang	Massachusetts Institute of Technology
Dain Kim	Massachusetts Institute of Technology
Sean J. Li	Massachusetts Institute of Technology
Brian S. Liu	Massachusetts Institute of Technology
Kevin J. Liu	Massachusetts Institute of Technology
Mihir A. Singhal	Massachusetts Institute of Technology
Noah Walsh	Massachusetts Institute of Technology
Rui Yao	Massachusetts Institute of Technology

THE NEXT TWELVE HIGHEST-RANKING INDIVIDUALS

Each receives an award of \$250

Swapnil Garg Massachusetts Institute of Technology Thomas Guo Massachusetts Institute of Technology

Minjae Kwon Princeton University
Frank Lu Princeton University

Zhao Yu Ma

Holden Mui

Kevin Ren

Victor Rong

Carl Schildkraut

Tristan Shin

Massachusetts Institute of Technology

Franklyn Wang Harvard University

Guanpeng A. Xu Massachusetts Institute of Technology

HONORABLE MENTION — INDIVIDUALS

Gradin Anderson, Brigham Young University Adam Ardeishar, Massachusetts Institute of Technology Adam Bertelli, Carnegie Mellon University Ciprian Mircea Bonciocat, University of California, Los Angeles Krit Boonsiriseth, Massachusetts Institute of Technology Joseph Camacho, Brigham Young University Sanjana Das, Massachusetts Institute of Technology Sixiang Gao, Carnegie Mellon University Weizhen Gao, Carnegie Mellon University Kyle J. Gatesman, Johns Hopkins University Gopal K. Goel, Massachusetts Institute of Technology Howard L. Halim, Carnegie Mellon University Joseph W. Heerens, Massachusetts Institute of Technology Daniel X. Hong, Massachusetts Institute of Technology Edward Hou, Carnegie Mellon University Ivan Hu, University of Wisconsin Vincent Huang, Massachusetts Institute of Technology Aaron Alvarado K. Julistiono, Massachusetts Institute of Technology Ashton Keith, Binghamton University Aidan M. Kelley, Washington University John S. Ko, Massachusetts Institute of Technology Nitin A. Kumar, Massachusetts Institute of Technology Thomas J. Lam, Carnegie Mellon University Phuoc Dinh Le, Southern Methodist University Tran Duy Anh Le, University of Rochester

Saba Lepsveridze, Massachusetts Institute of Technology

Daniel Li, Massachusetts Institute of Technology

Kevin Li, Stanford University

Ritam Nag, Massachusetts Institute of Technology Quan M. Nguyen, Massachusetts Institute of Technology Vladyslav Oleksenko, Carnegie Mellon University Misheel Otgonbayar, Massachusetts Institute of Technology Alan Peng, Massachusetts Institute of Technology Gregory Pylypovych, Massachusetts Institute of Technology Timothy Qian, Massachusetts Institute of Technology Niyanth Rao, Carnegie Mellon University Brian E. Reinhart, Massachusetts Institute of Technology Dilhan H. Salgado, Carnegie Mellon University Gian Cordana Sanjaya, University of Waterloo Eric Shen, Harvard University Zeyu Shen, Duke University Tomasz Slusarczyk, Massachusetts Institute of Technology Nathan Smith, Washington University Kenta Suzuki, Massachusetts Institute of Technology Sheldon K. Tan, Harvard University Colin S. Tang, Massachusetts Institute of Technology Vittal Thirumalai, Massachusetts Institute of Technology Rahul K. Thomas, Stanford University Sasha Voitovych, University of Toronto Jianzhi Wang, University of California, Berkeley William Wang, Massachusetts Institute of Technology Xunjing Wei, Massachusetts Institute of Technology Richard H. Wu, University of California, Berkeley Alex Xu, University of Michigan Daniel Xu, Massachusetts Institute of Technology

Unubold Munkhbat, Massachusetts Institute of Technology

Michael Li, University of Toronto
Samuel J. Li, University of Toronto
Zhening Li, Massachusetts Institute of Technology
Wentinn N. Liao, University of California, Berkeley
Andrew Y. Lin, Massachusetts Institute of Technology
James H. Lin, Massachusetts Institute of Technology
Jason Liu, Massachusetts Institute of Technology
Steven Liu, Massachusetts Institute of Technology
Yijia Liu, Duke University
Jeffrey Lu, Massachusetts Institute of Technology
Edis Memis, Harvard University

Binwei Yan, Massachusetts Institute of Technology
Andrew Yao, Massachusetts Institute of Technology
Zi Song Yeoh, Massachusetts Institute of Technology
Justin Y. Yu, Massachusetts Institute of Technology
Runze Yu, University of California, Los Angeles
Fedir Yudin, Massachusetts Institute of Technology
Ethan A. Zahid, Massachusetts Institute of Technology
Brad W. Zhang, Carnegie Mellon University
Daniel J. Zhang, University of California, Santa Barbara
Jacob B. Zhang, University of California, Los Angeles
Honglin Zhu, Massachusetts Institute of Technology

ELIZABETH LOWELL PUTNAM PRIZE

Receives an award of \$1,000

Dain Kim Massachusetts Institute of Technology

WINNING TEAMS

Rank	School	Team Members (in alphabetical order)
1	Massachusetts Institute of Technology	Edward Wan, Shengtong Zhang, and Daniel G. Zhu
2	Princeton University	Minjae Kwon, Frank Lu, and Aleksa Milojevic
3	Harvard University	Eric Shen, Sheldon K. Tan, and Franklyn Wang
4	Stanford University	Quanlin Chen, Kevin Li, and Rahul K. Thomas
4	University of California, Los Angeles	Ciprian Mircea Bonciocat, Runze Yu, and Jacob B. Zhang

The institution with the first-place team receives an award of \$25,000, and each member of the team receives \$1,000. The team and member awards for second place are \$20,000 and \$800, respectively; for third place, \$15,000 and \$600; for fourth place, \$10,000 and \$400; and for fifth place, \$5,000 and \$200.

HONORABLE MENTION — TEAMS

Listed by university in alphabetical order

School	Team Members (in alphabetical order)
Carnegie Mellon University	Adam Bertelli, Edward Hou, Dilhan H. Salgado
Duke University	Yijia Liu, Nathan Nguyen, and Zeyu Shen
University of California, Berkeley	Wentinn N. Liao, Jianzhi Wang, and Richard H. Wu
University of Toronto	Michael Li, Samuel J Li, and Sasha Voitovych
University of Waterloo	Alexander Monteith-Pistor, Gian Cordana Sanjaya, and Rui Ming Xiong

THE WILLIAM LOWELL PUTNAM MATHEMATICAL COMPETITION WAS PREPARED BY:

Andrew Bernoff, Harvey Mudd College — Chair of The Problems Committee

Karl Mahlburg, Susquehanna International Group — Member of The Problems Committee

Richard Stong, Center For Communications Research — Member of The Problems Committee

Gabriel Carroll, University of Toronto — Contributor To The Problems Committee

Andrew Granville, University of Montreal — Contributor To The Problems Committee

Daniel Ullman, George Washington University — Director of The Competition

Mark Krusemeyer, Carleton College — Associate Director of The Competition

SCORE—RANK CORRESPONDENCE

A participant is said to have rank n if n-1 participants scored higher

Score	Rank										
119	1	68	28	51	55	35	127	21	329	7	1022
110	2	67	29	50	57	34	130	20	352	6	1067
99	3	66	30	49	65	33	136	19	404	5	1142
90	4	65	32	48	70	32	150	18	423	4	1314
89	5	64	33	46	72	31	167	17	449	3	2200
83	6	61	34	45	74	30	193	16	464	2	2270
82	7	60	35	44	77	29	212	15	489	1	2327
80	8	59	37	43	80	28	225	14	536	0	2431
79	9	58	40	42	84	27	238	13	635		
77	11	57	41	41	89	26	244	12	671		
75	16	56	42	40	96	25	252	11	739		
73	18	55	45	39	106	24	265	10	829		
72	20	53	46	38	112	23	282	9	956		
71	21	52	50	36	123	22	303	8	979		

FREQUENCY DISTRIBUTION OF PROBLEM SCORES OF THE TOP 535 CONTESTANTS

Score	A 1	A2	А3	A4	A 5	A6	B1	B2	В3	B4	B5	В6
10	369	239	66	7	130	4	204	114	28	27	5	8
9	14	14	2	0	20	1	18	12	10	40	4	1
8	36	36	4	2	5	1	47	1	0	12	1	2
7	4	14	2	2	3	0	16	0	0	0	2	0
6	8	0	0	0	0	0	0	0	0	0	0	0
5	0	0	0	0	0	0	0	0	0	0	0	0
4	93	0	0	0	0	0	0	0	0	0	0	0
3	0	31	39	0	6	0	0	1	0	0	1	0
2	2	41	49	0	35	0	23	11	2	34	0	0
1	1	44	52	1	34	1	32	102	3	35	4	16
0	6	59	78	115	114	150	115	124	80	62	94	52
NA	2	57	243	408	188	378	80	170	412	325	424	456

STUDENTS RANKED 106—193

Listed by university in alphabetical order

Arizona State University, Tempe, AZ

Tanner J. Reese

Bob Jones University, Greenville, SC

Erick J. Ross

Brandeis University, Waltham, MA

Benjamin M. Kamen

Brown University, Providence, RI

Luke Choi Carter Cobb Dominick Joo

California Institute of Technology, Pasadena, CA

August Chen

Carnegie Mellon University, Pittsburgh, PA

Alan M. Abraham Eric J. Kim Sam Rosenstrauch Isaac R. Browne Christopher Lambert Justin W. Sun Advait V. Nene Haveesh S. Viswanatha Samuel R. Delatore

Justin Hsieh Yan Pan Richard Wu Callan Jacobus Qingyi Peng Grant Yu

Cornell University, Ithaca, NY

Sikai Shen

Duke University, Durham, NC

Nathan Nguyen Harry Chen

Fairfield University, Fairfield, CT

Thanh Le

Florida State University, Tallahassee, FL

Graham L. O'Donnell

William Y. Hu

Harvard University, Cambridge, MA

Kevin Du Fabio Pruneri Gabriel D. Wu **Daniel Sheremeta**

Harvey Mudd College, Claremont, CA

Ian Shors

Haverford College, Haverford, PA

Guilherme Zeus Dantas e Moura Lucas L. Nelson

Indiana University— Purdue University Indianapolis, Indianapolis, IN

Croix Gyurek

Massachusetts Institute of Technology, Cambridge, MA

Bhavya Agrawalla	Sean Elliott	Rupert M. Li	Nguyen Tran Bach
Brandon Chen	Jonathan Huang	William Lin	Holden E. Watson
Matthew Cho	Maxwell Jiang	Youssef Marrakchi	Benjamin P. Wright
Akash Das	Hyunwoo Lee	Asaad Mohammedsaleh	Jeffery Yu
		All 0 1 '1	

Nishant Dhankhar Jeffery Li Aleksandre Saatashvil

McGill University, Montreal, QC, Canada

Antoine Labelle

Montgomery College, Rockville, MD

Trang TT. Vu

Northeastern University, Boston, MA

Noble Mushtak

Northwestern University, Evanston, IL

Akhil S. Kalghatgi

Princeton University, Princeton, NJ

George H. Bentley Marko Medvedev Adam X. Huang Aleksa Milojevic Sunay Joshi Ben Zenker

Rice University, Houston, TX

Mark Helman

Rose-Hulman Institute of Technology, Terre Haute, IN

Reed C. Phillips

Stanford University, Stanford, CA

Andrei Mandelshtam Zichuan Xu Katherine Y. Yu

University of British Columbia, Vancouver, BC, Canada

Ray Ng Arvin Sahami

University of California, Berkeley, CA

Shreyas Ramamurthy Henry Zeng

University of California, Irvine, CA

Grady J. Crossley

University of California, Los Angeles, CA

Issac Li

University of California, San Diego, CA

Jingyue Zhang

University of California, Santa Cruz, CA

Sam A. Reifenstein

University of Chicago, Chicago, IL

Arjun B. Venkatraman Derek Zhu

University of Illinois, Urbana-Champaign, IL

Brendan A. Biernacki Pavle Vuksanovic

University of Maryland, College Park, MD

Steppan Konoplev Thomas Luo

University of Michigan, Ann Arbor, MI

Ramchandra Apte Adam J. Earnst

University of Minnesota, Twin Cities, Minneapolis, MN

Nathan Mihm

University of New Mexico, Albuquerque, NM

Franklin Pezzuti Dyer

University of Pennsylvania, Philadelphia, PA

Gokul K. Murugadoss

University of Texas, Austin, TX

Luis Kim

University of Toronto, Toronto, ON, Canada

Alptekin C. Goksan Chayim Lowen Alexander Ryabchenko

University of Virginia, Charlottesville, VA

Declan R. Stacy

University of Washington, Seattle, WA

Coby Tran

University of Waterloo, Waterloo, ON, Canada

Yundi Duan Rui Ming Xiong Alexander Monteith-Pistor Michael Yang

Washington University, St. Louis, MO

Shifan Dong

William and Mary, Williamsburg, VA

Jason Cheah

Yale University, New Haven, CT

Derek Dong Jason Wang Steven S. Ma Ran Wang

Students Ranked 212—489

Listed by university in alphabetical order

Amherst College, Amherst, MA

Alan Li Derek Zhang

Arizona State University, Tempe, AZ

Matthew Hurley Aareyan Manzoor

Boston University, Boston, MA

Henry A. Todorow

Brigham Young University, Provo, UT

Gordon Bridge Quinlan T. Leishman James Camacho Daniel South

Dallin Christiansen

Brown University, Providence, RI

Ethan D. Bove Andrew Yuan Kyle K. Lee Xiaochi Zhang

Akash B. Singirikonda

Bryn Mawr College, Bryn Mawr, PA

Jiachen Kang

Bucknell University, Lewisburg, PA

Anh Tran

California Institute of Technology, Pasadena, CA

Akshay Gowrishankar Joseph R. Litvin Depei Li Yakov Shalunov

California Polytechnic State University, Pomona, CA

Peter C. DeVries

California Polytechnic State University, San Luis Obispo, CA

Mav Lara

California State University Channel Islands, Ventura County, CA

Kai L. Murray

Carleton College, Northfield, MN

Wasin Meesena

Carnegie Mellon University, Pittsburgh, PA

Siyuan Chen Daniel D. Kim Parth D. Shastri Puhua Cheng Suhas Kotha David Tang

Min Yeong Choi Vinod Krishnamoorthy Mario C. Tutuncu-Macias

Gabriel Ciccu Falcon Lins Zack T. Lee John Wang

Xinyu CuiLucas LiuJacob C. WeinerYucheng DaiEthan LuBraden R. Yates

Russell Emerine Rose H. Luttmer Kevin You

Evan Fang Eric H. Oh Gregory Zelevinsky

Rajeev Godse Aidan B. Pevida Yixuan Zheng
Ethan Gu Aresh Pourkavoos Allen Zheng
Eric Huang Khunpob Sereesuchart Eric Zheng
Joseph S. Kalarickal Saadiq Shaikh Kevin A. Zhou

Case Western Reserve University, Cleveland, OH

Ryan Karpuszka

Clemson University, Clemson, SC

Lucy Staubes

Columbia University, New York City, NY

Ashwin Padaki Kevin Y. Zhang

Cornell University, Ithaca, NY

Tomas Alvarez Rowan D. Hess Zichen Wang

Courant Institute of Mathematical Sciences—New York University, New York, NY

Ethan Joo Yuelong Li Nicholas Wang

Dartmouth College, Hanover, NH

Finn Hulse

Davidson College, Davidson, NC

William Jo Smith Kenan B. Wood

Drexel University, Philadelphia, PA

Duy D. Nguyen

Duke University, Durham, NC

Feng Cong
Allan Guo
Marcos Hirai Catao
Yi Li
Steven Li

Jerry Liu
Kevin H. Tu
Ximeng Wang
Andy Y. Wu
Yinhong Zhao

Florida Atlantic University, Boca Raton, FL

Christian X. Engman

Georgetown University, Washington, DC

Joe W. Kleban

Georgia Institute of Technology, Atlanta, GA

Jeffrey S. Chang
Alexander Divoux
Vasisht L. Ganesh
Dorian E. Kidonakis

Neil R. Patram
Suchet J. Sapre
Daniel D. Shen
Lixin Zheng

Georgia Southern University - Armstrong Campus, Savannah, GA

Jesus Omar Sistos Barron

Grinnell College, Grinnell, IA

Lilith O. Hafner

Harvard University, Cambridge, MA

Gaurav M. Goel Michael Hwang Alexander L. Zhang

Harvey Mudd College, Claremont, CA

Tiger Che Prakod Ngamlamai Mathus Leungpathomaram Cedar F. Turek

Haverford College, Haverford, PA

Joao Pedro Mello de Carvalho Logan A. Post

Iowa State University, Ames, IA

Andrew Osborne

Johns Hopkins University, Baltimore, MD

Yuheng Shi Sean J. O'Connor Everett Xu

Kent State University, Kent, OH

Nathaniel D. Miller

Loyola Marymount University, Los Angeles, CA

Jeffrey Huang

Massachusetts Institute of Technology, Cambridge, MA

Khalid Ajran David Hu Anders Olsen
Adithya S. Balachandran Andrew Huang Steven Reyes
Nikoloz Birkadze Shawn Im Juan E. Reyes
David J. Chen Gabriel Kammer Natanon Therdpraisan
Abdellatif Anas Chentouf Daniel Li Christopher Tong

Matija Delic Anqi Li David Vulakh
Owen M. Dugan Yuka Machino Catherine Wu
Chirag Falor Srinath V. Mahankali Jesse Yang
Vincent K. Fan Andrei T. Marginean Jeremy Zhou

Letong Hong Isabel E. McGuigan

McGill University, Montreal, QC, Canada

Yuhe Jiang Alexander S. Koran Qiu Shi Wang

Michigan Technological University, Houghton, MI

Alan K. Bouwman

Northeastern University, Boston, MA

Devin Brown

Princeton University, Princeton, NJ

Daniel Carter Stephen Jiang Atanas B. Dinev Austen Mazenko Zander Hill Igor Medvedev

Purdue University, Lafayette, IN

Zijin Liu

Queens University, Kingston, ON, Canada

Bijan Betel Miri Raymond Jing

Reed College, Portland, OR

Tyler Dunaisky Daniel J. Zou

Rensselaer Polytechnic Institute, Troy, NY

Alex B. Moore

Rice University, Houston, TX

Ruofena Liu Arie Ogranovich Alan Tapper

Rochester Institute of Technology, Rochester, NY

Evan RV. Rysdam

Rutgers, State University of New Jersey, New Brunswick, NJ

Ozan Acikgoz Enver S. Aman

Stanford University, Stanford, CA

David Kewei Lin Matias Shundi Michael Cho Yunchu Dai Bradley K. Moon Aoden M. Teo Tae Kyu Kim lan R. Ruohoniemi Anthony Zhan

Sidhart Krishnan Danny Sallis

Stevens Institute of Technology, Hoboken, NJ

Eshan Tiyakaran

Stony Brook University, Stony Brook, NY

Calvin Aw

Syracuse University, Syracuse, NY

Connor B. Ritchie

Texas A&M University, College Station, TX

Ethan Luo Jason Luo

Université de Sherbrooke, Sherbrooke, QC, Canada

Ismael El Yassini

University of Arkansas, Fayetteville, AR

Michael A. Logal

University of Alabama, Tuscaloosa, AL

Jacob B. Glidewell Justin Z. Saye

University of Alberta, Edmonton, AB, Canada

Edmond Tuong Coleton Kotch Sergii Penner

University of British Columbia, Vancouver, BC, Canada

Eugene K. Chau Oakley M. Edens Siyang Lin

University of Calgary, Calgary, AB, Canada

John Zheng

University of California, Berkeley, CA

Dhruba Ghosh
Ajit Kadaveru
Adam A. Khoja
Austin Lei
Axel J. Li
Andrew D. Lin
Ishaan Patkar
Zachary G. Slonim

University of California, Irvine, CA

David B. Militante

University of California, Los Angeles, CA

Duc M Hoang

John J. Li

Alvin Liu

Curtis Liu

Sumith R. Nalabolu

Sachin Sahay

Zachary Tu

Eric Wu

Chujun Xu

Hongyu Zhu

University of California, San Diego, CA

Mark L. Barbone Derek Cantor Shubham Bhargava Jared A. Hughes

University of California, Santa Barbara, CA

Theodore S. Bafrali Drew N. Miller
Abhinav Ganesh Christian D. Reynaldo
Dongming Hua

University of Chicago, Chicago, IL

William Hu Cameron A. Chang Sparsho De Andre F. Emery

University of Dallas, Irving, TX

Isaac Hellerman

University of Delaware, Newark, DE

Leon Zhao

University of Florida, Gainesville, FL

Hugh W. Dennin
Carson A. Jones
Alejandro Leon
Jake B. Shannin
Zonshen Yu

University of Illinois, Urbana-Champaign, IL

Rohan Bokaria Erin Kim
David T. James Ruzhang Yang
Aditya Jain

University of Iowa, Iowa City, IA

Nick Morrow Carter J. Tams

University of Kentucky, Lexington, KY

Noah Owen

University of Manitoba, Winnipeg, MB, Canada

Marshall Kaatz

University of Maryland, College Park, MD

John C. Brownfield Garrett D. Peters
David D. Fang Jackson T. Reynolds
Isaac A. Mammel

University of Massachusetts, Amherst, MA

Nathaniel C. Reid

University of Michigan, Ann Arbor, MI

Marcus C. Gozon Tuong Vu Le Jia Guo An H. Nguyen

University of Minnesota, Twin Cities, Minneapolis, MN

Nhung Pham Andrew T. Hale

University of Nevada, Las Vegas, NV

Gaelan Chen

University of Nevada, Reno, NV

Logan K. Leavitt

University of North Carolina, Chapel Hill, NC

Stepan Malkov

University of North Texas, Denton, TX

Michalis W. Paizanis

University of Notre Dame, Notre Dame, IN

William K. Grannis

University of Pennsylvania, Philadelphia, PA

Tyler Edwards Benjamin Lee David Kogan Zhong Zhang

University of Rochester, Rochester, NY

Phuc H. Lam Zhiyu Lei

University of Southern California, Los Angeles, CA

Benjamin L. Cohen Joshua Speckman

University of Texas, Austin, TX

Alexander M. Burton Mihir Shah Lazar Ilic Brian Wang Aaron J. Lamoreaux Hubert Yang

University of Texas, Dallas, TX

Evan M. Bailey

University of Toronto, Toronto, ON, Canada

Zelin ChenYao KuangNicholas SullivanJonah ChenYunong LiJing WangFreeman ChengJiyuan LuBoyu Zheng

University of Utah, Salt Lake City, UT

Emil Geisler

University of Virginia, Charlottesville, VA

Varun Vejalla

University of Washington, Seattle, WA

Gregory Baimetov Benjamin Li Nelson Y. Sun

University of Waterloo, Waterloo, ON, Canada

Marcus Chan Richard Y. Kang Davi C. Sena Thinula De Silva Tam An Le Quang Kevin Wan Andrew Dong Nathan Lo Moses Xu

Michael Du Jonathan C. Nitisastro Danny X. Zhang

Shuo Gao Om Patel

University of Wisconsin, Madison, WI

Joseph Cai Nitit Jongsawatsataporn

Vanderbilt University, Nashville, TN

Gabriel Diraviam Kevin Gomez

Villanova University, Villanova, PA

Abdullah Al Rafi Mahmud

Virginia Wesleyan University, Virginia Beach, VA

June Richardson

Wagner College, Staten Island, NY

Mohamed E. Lotfi

Washington University, St. Louis, MO

Nicholai Dimov

Wheaton College, Wheaton, IL

Daniel R. McKay

Williams College, Williamstown, MA

Rauan Kaldybayev Alexander E. Shashkov Jonathan S. Rogers Benjamin M. Baily

Yale University, New Haven, CT

John Gunderson Andy N. Nilipour Raymond Yang Eddie Hu Tushar S. Patel Stephen Y. Yin Frank Li Vismay Sharan Michael Ying Deyuan Li Preston A. Smith Fred Zhang