## Practical 5

## LU Decomposition Method

Definitiom: A non - singular matrix A ha s a LU decopmosition if it can be expressed as the product of a lower triangualr matrix L and an upper triangualr matrix U i.e., A = LU

Q. To find the LU decomposition

$$\begin{aligned} & \text{LUDecomp} \left[ \text{AO}_{-}, \ n_{-} \right] := \text{Module} \left[ \left( \lambda = \text{AO}, i, p \right), \ U = \text{AO}; \ L = \text{IdentityMatrix} \left[ n \right]; \right. \\ & \text{Print} \left[ \text{MatrixForm} \left[ L \right], \ \text{MatrixForm} \left[ U \right], \ " = ", \\ & \text{MatrixForm} \left[ \text{AO} \right]; \right]; \\ & \text{For} \left[ p = 1, \ p \leq n-1, \ p++, \right. \\ & m = \frac{\lambda_{\left\{ \left[ i, p \right] \right\}}}{\lambda_{\left\{ \left[ p, p \right] \right\}}}; \\ & L_{\left\{ \left[ i, p \right] \right\}} = m; \\ & \lambda_{\left\{ \left[ \left[ i, p \right] \right] } = m; \\ & \lambda_{\left\{ \left[ \left[ i, p \right] \right] } = m, \\ & \lambda_{\left\{ \left[ \left[ i, p \right] \right] } = m, \right. \right. \\ & MatrixForm \left[ L \right], \ \text{MatrixForm} \left[ U \right], \\ & " = ", \ \text{MatrixForm} \left[ \lambda O \right]; \right\}; \right]; \\ & \text{Print} \left[ "L", "=", \ \text{MatrixForm} \left[ U \right]; \right. \\ & \lambda = \left( \frac{4}{3} \ 2 \ 3 \right), \\ & \lambda = \left( \frac{4}{3} \ 2 \ 4 \right); \\ & LUDecomp \left[ \lambda, 3 \right] \end{aligned}$$

$$L = \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{3} & \frac{25}{4} \\ 0 & 0 & -4 \end{pmatrix}$$

$$U = \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{2} & \frac{25}{4} \\ 0 & 0 & -4 \end{pmatrix}$$

$$U = \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{2} & \frac{25}{4} \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{2} & \frac{25}{4} \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{2} & \frac{25}{4} \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{2} & \frac{25}{4} \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{2} & \frac{25}{4} \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{2} & \frac{25}{4} \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{2} & \frac{25}{4} \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{2} & \frac{25}{4} \\ 0 & 0 & \frac{7}{4} \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{2} & \frac{25}{4} \\ 0 & 0 & \frac{7}{4} \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{2} & \frac{25}{4} \\ 0 & 0 & \frac{7}{4} \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{2} & \frac{25}{4} \\ 0 & 0 & \frac{7}{4} \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{2} & \frac{25}{4} \\ 0 & 0 & \frac{7}{4} \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{2} & \frac{25}{4} \\ 0 & 0 & \frac{7}{4} \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{2} & \frac{25}{4} \\ 0 & 0 & \frac{7}{4} \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{2} & \frac{25}{4} \\ 0 & 0 & \frac{7}{4} \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{2} & \frac{25}{4} \\ 0 & 0 & \frac{7}{4} \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{2} & \frac{25}{4} \\ 0 & 0 & -4 \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & \frac{5}{2} & \frac{25}{4} \\ 0 & 0 & -4 \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 4 & 2 & 3 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 4$$

$$A = \begin{pmatrix} 1 & 2 & 6 \\ 4 & 8 & -1 \\ -2 & 3 & 5 \end{pmatrix}$$

LUDecomp[A, 3]

$$\{\{1, 2, 6\}, \{4, 8, -1\}, \{-2, 3, 5\}\}$$

$$\left( \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{array} \right) \left( \begin{array}{ccc} 1 & 2 & 6 \\ 4 & 8 & -1 \\ -2 & 3 & 5 \end{array} \right) \ = \ \left( \begin{array}{ccc} 1 & 2 & 6 \\ 4 & 8 & -1 \\ -2 & 3 & 5 \end{array} \right)$$

$$\left(\begin{array}{ccc} 1 & 0 & 0 \\ 4 & 1 & 0 \\ 0 & 0 & 1 \end{array}\right) \left(\begin{array}{ccc} 1 & 2 & 6 \\ 0 & 0 & -25 \\ -2 & 3 & 5 \end{array}\right) \ = \ \left(\begin{array}{ccc} 1 & 2 & 6 \\ 4 & 8 & -1 \\ -2 & 3 & 5 \end{array}\right)$$

$$\left(\begin{array}{ccc} 1 & 0 & 0 \\ 4 & 1 & 0 \\ -2 & 0 & 1 \end{array}\right) \left(\begin{array}{ccc} 1 & 2 & 6 \\ 0 & 0 & -25 \\ 0 & 7 & 17 \end{array}\right) \ = \ \left(\begin{array}{ccc} 1 & 2 & 6 \\ 4 & 8 & -1 \\ -2 & 3 & 5 \end{array}\right)$$

Power::infy: Infinite expression  $\frac{1}{0}$  encountered.  $\gg$ 

 $\infty$ ::indet : Indeterminate expression 0 ComplexInfinity encountered.  $\gg$ 

 $\infty$ ::indet : Indeterminate expression 0 ComplexInfinity encountered.  $\gg$ 

$$\begin{pmatrix} 1 & 0 & 0 \\ 4 & 1 & 0 \\ -2 \text{ ComplexInfinity } 1 \end{pmatrix} \begin{pmatrix} 1 & 2 & 6 \\ 0 & 0 & 0 & -25 \\ \text{Indeterminate Indeterminate ComplexInfinity} \end{pmatrix} = \begin{pmatrix} 1 & 2 & 6 \\ 4 & 8 & -1 \\ -2 & 3 & 5 \end{pmatrix}$$

Remark: A has no LU decomposition