



# Least Squares and SLAM

## *Intro*

Giorgio Grisetti

Part of the material of this course is taken from the Robotics 2 lectures given by G.Grisetti, W.Burgard, C.Stachniss, K.Arras, D. Tipaldi and M.Bennewitz

# SLAM

- SLAM= Simultaneous Localization and Mapping
  - Estimate:
    - the map of the environment
    - the trajectory of a moving device
- using a sequence of sensor measurements.



# SLAM

- SLAM= Simultaneous Localization and Mapping

- Estimate:

- the **map** of the environment
- the **trajectory** of a moving device

**these quantities  
are correlated**

using a sequence of sensor measurements.



# Why SLAM is so Important?

- Most applications require to localize a device in a map.
- A map cannot always be provided.
- Do **SLAM**!



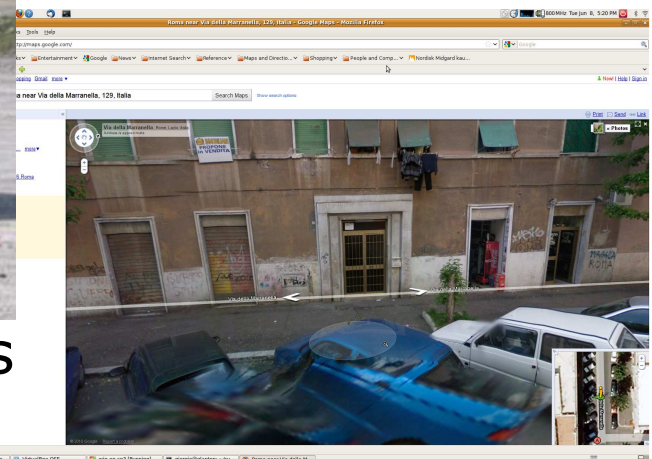
service  
robotics

industrial  
applications



autonomous  
cars

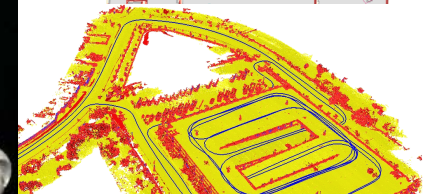
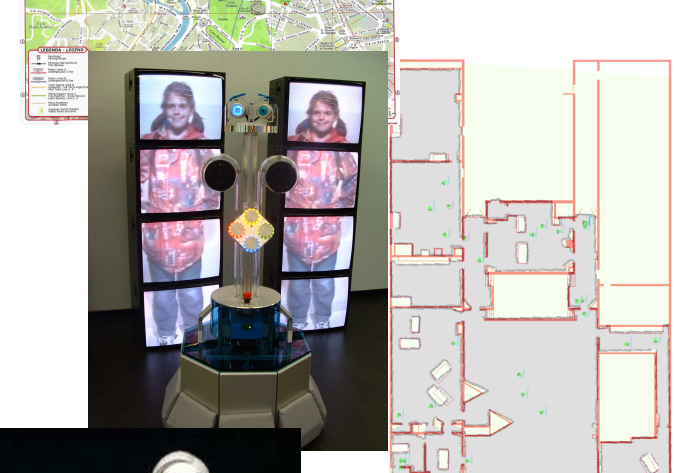
Google street view



# History

time and size of the environment  
↓

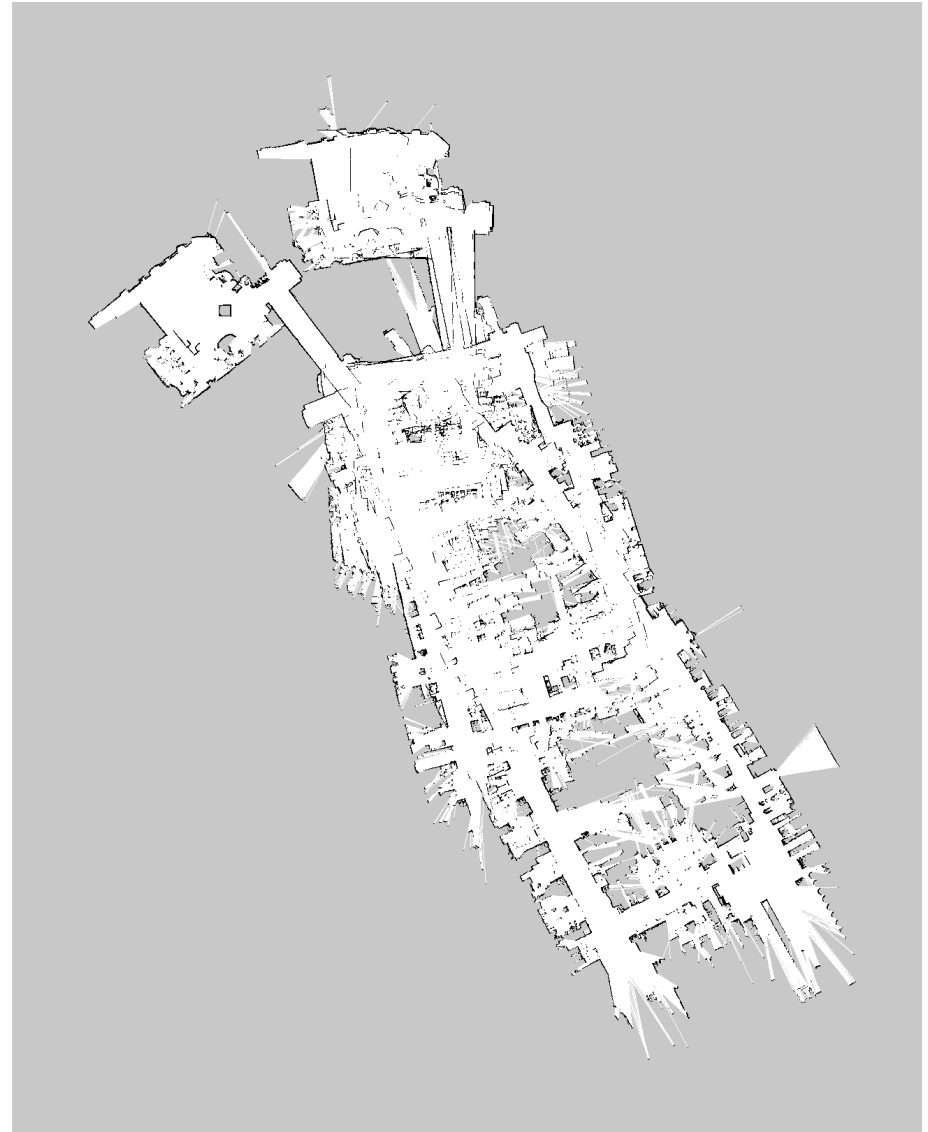
- 1960 Bundle Adjustment (~10 images)
- 1970 Recursive Partitioning (~1000 images)
- 1990 (SLAM is born)
- 1993 Scan-Matching, Iconic maps
- 1997 Graph-SLAM
- 2000 Modern Sparse Matrix Techniques for BA
- 2002 FastSLAM
- 2003 ESDF, Treemap, TJTF
- 2005 SAM
- 2006 Appearance-Based Localization
- 2006 Efficient Graph-Based SLAM
- 2010 Towards the unification of BA and SLAM





# Graph-based SLAM in a Nutshell

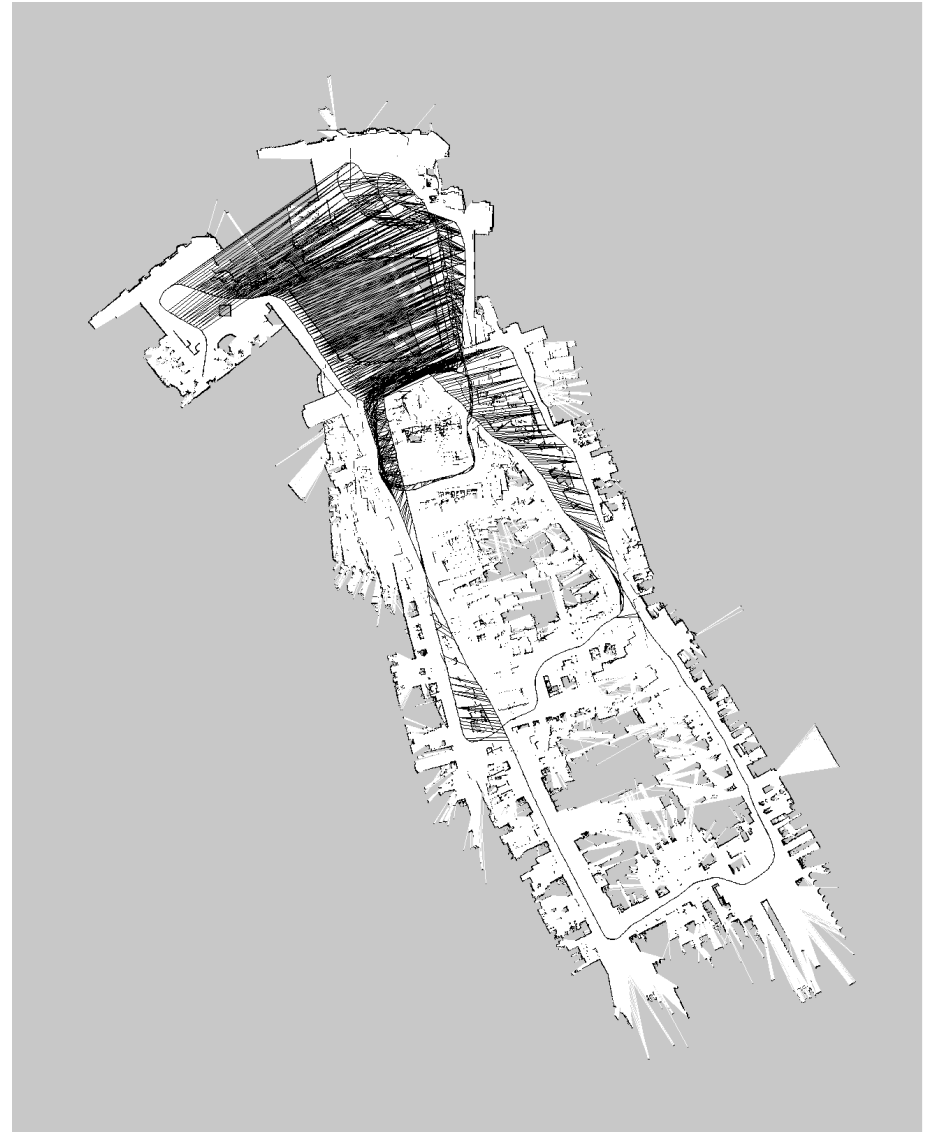
- Node:
  - robot position and
  - laser measurement.
- Edge:
  - spatial transformation between nodes
  - depends on the matching of scans



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# Graph-based SLAM in a Nutshell

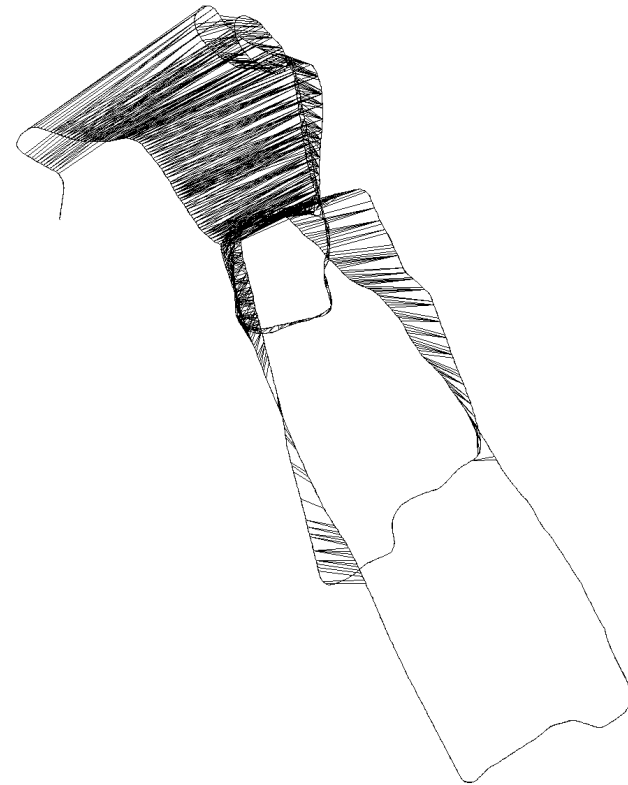
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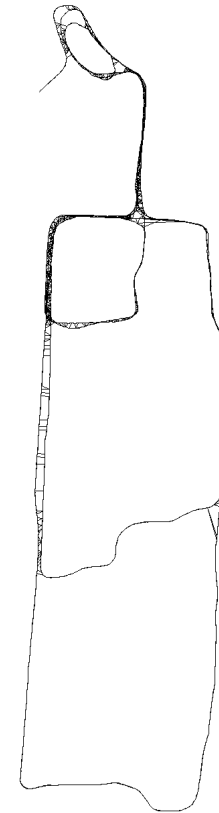
- The graph “abstracts away” the measurements
- The most likely is trajectory obtained by optimization.





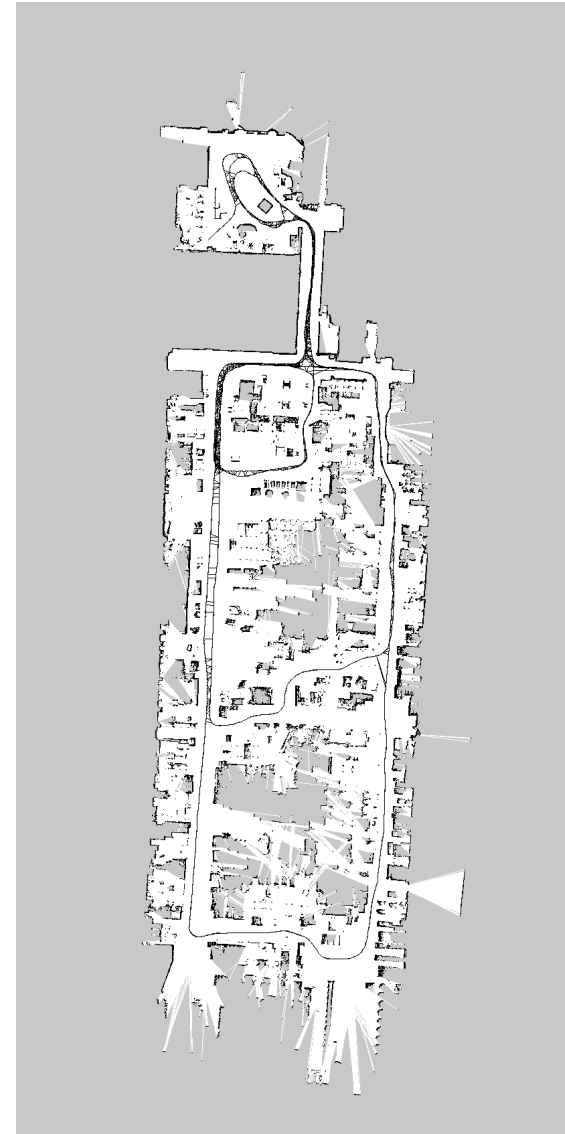
# Graph-based SLAM in a Nutshell

- The graph “abstracts away” the measurements
- The most likely is trajectory obtained by optimization.
- ... like this



# Graph-based SLAM in a Nutshell

- ... and thus the map.

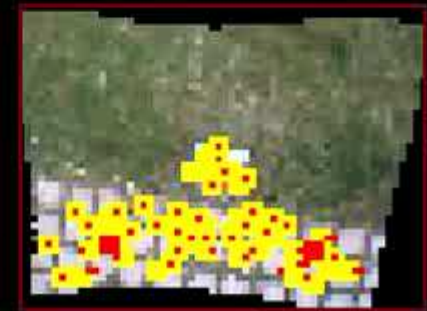


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# An Example using Lasers

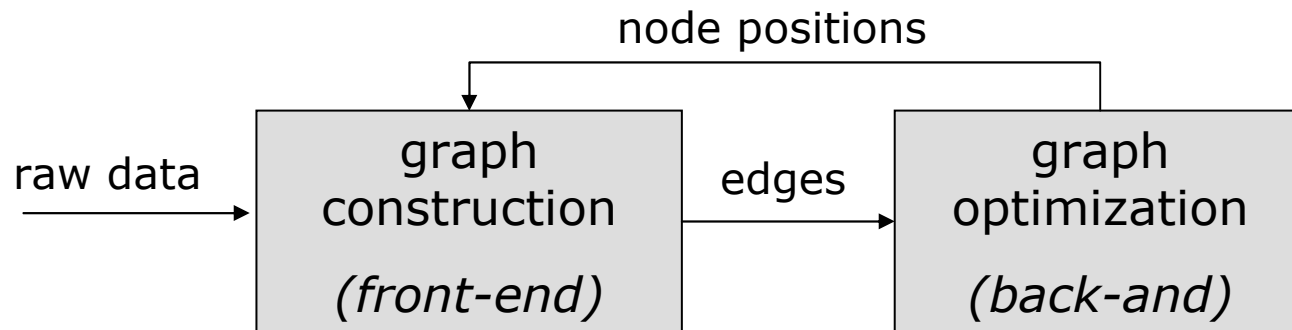


# ... or Vision



# Front-end and Back-end

- **Front-end:** extracts constraints from the sensor data
- **Back-end:** optimizes the pose-graph to reduce the error caused by the constraints



➡ Insight: intermediate solutions are needed to make good data associations

# Front-end and Back-end

- **Front-end**

- This part is sensor dependent
- We will discuss robots equipped with:
  - laser range finders
  - odometry

- **Back-end**

- We will discuss how to solve this problem with efficient least-squares approaches that exploit the problem's structure.

- **Calibration**

- A working system needs to be accurately tuned, and we will show how to do this with LS.



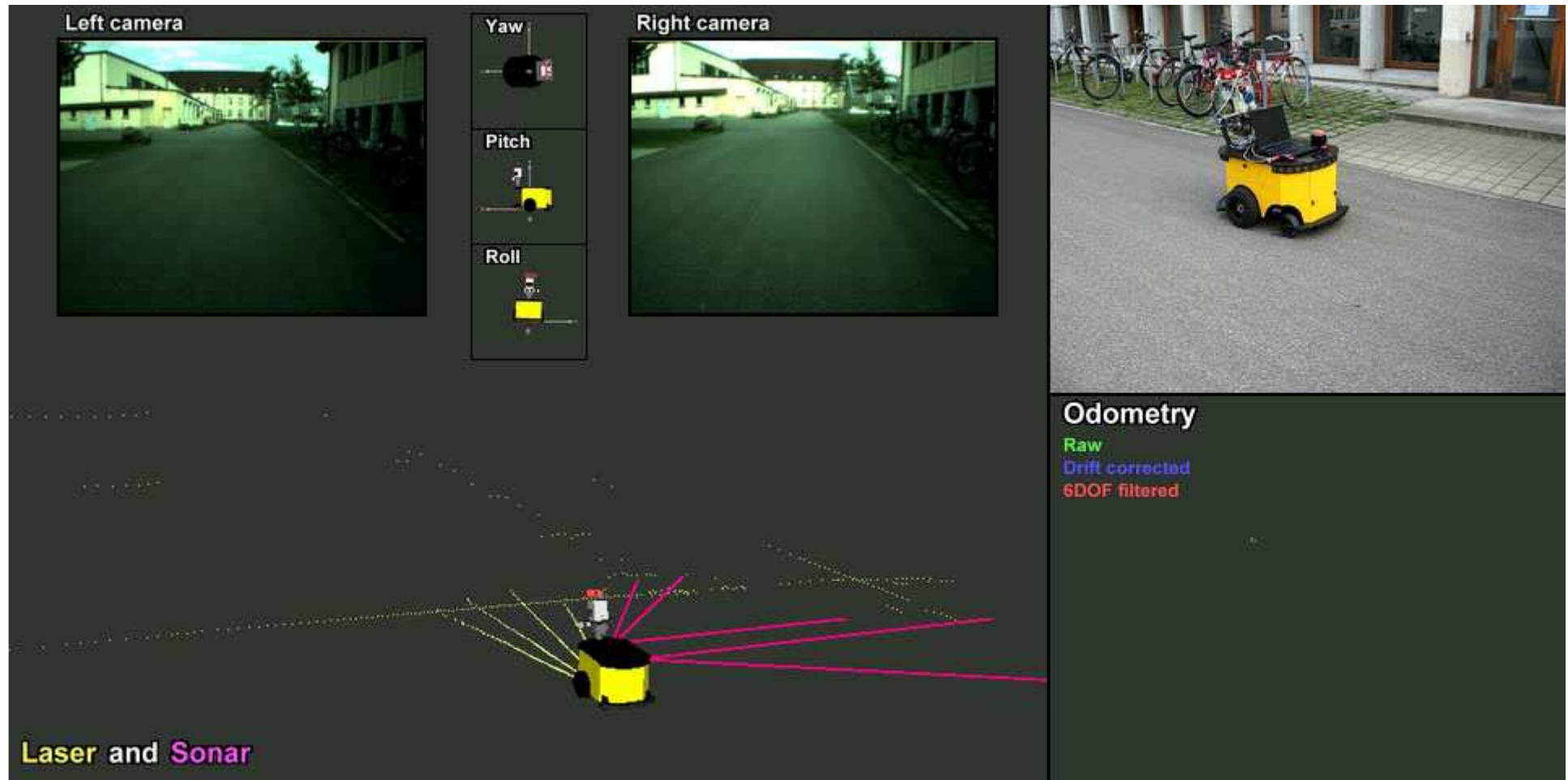
# Outline of the Course

- A (short!) refresher of linear algebra
- Introduction to Octave/Matlab
- Robot and sensor models
- Probability theory
- Particle Filtering and Localization
- Scan Matching (ICP)
- Least squares estimation
- Odometry calibration (and practical)
- Pose-graph optimization (and practical)
- Landmark-graph (and practical)

# Goals of the Course

- Get into LSE
  - You should be able to construct an LS estimator for typical problems
- Get some insights on SLAM and Filtering in this context
- See running systems and construct your own.
- Have access to real robot data.
- Have fun.

# Real Data



# Some Applications

