CSC 252: Computer Organization Spring 2018: Lecture 2

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Action Items:

- Programming Assignment 1 is out
- Trivia 1 is due on Friday, midnight

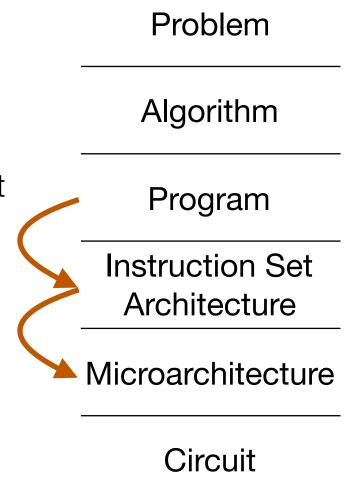
Slide Credits: Randal E. Bryant, David R. O'Hallaron

Announcement

- Programming Assignment 1 is out
 - Details: http://cs.rochester.edu/courses/252/spring2018/
 labs/assignment1.html
 - Due on Feb 2, 11:59 PM
 - Trivia due Friday, 1/26, 11:59 PM
 - You have 3 slip days (not for trivia)
- Ask the TAs if you have any questions regarding programming assignments

Previously in 252...

- How is a humanreadable program translated to a representation that computers can understand?
- How does a modern computer execute that program?



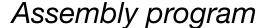
Scope of Computer Systems (CSC 252)

Previously in 252...

C Program

```
void add() {
  int a = 1;
  int b = 2;
  int c = a + b;
}
```

Pre-processor Compiler



movl \$1, -4(%rbp) movl \$2, -8(%rbp) movl -4(%rbp), %eax addl -8(%rbp), %eax

Previously in 252...

Assembly program

movl \$1, -4(%rbp) movl \$2, -8(%rbp) movl -4(%rbp), %eax addl -8(%rbp), %eax



Executable Binary

```
00011001 ...
01101010 ...
11010101 ...
01110001 ...
```

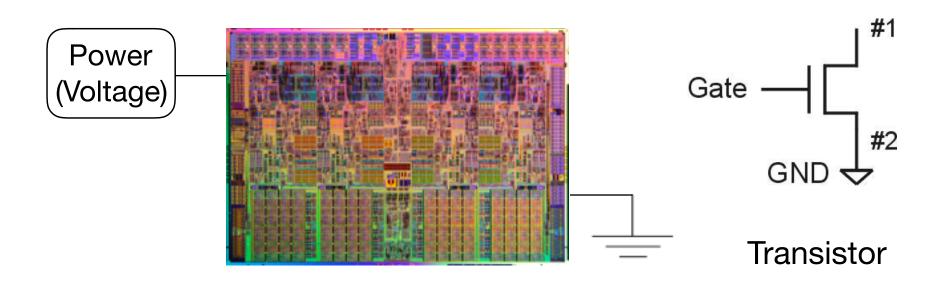
- Is ISA referring to assembly or binary?
 - They are the same thing; different representations.
- Instruction = Operator + Operand(s)

Today: Representing Information in Binary

- Why Binary (bits)?
- Bit-level manipulations
- Integers
 - Representation: unsigned and signed
 - Conversion, casting
 - Expanding, truncating
 - Addition, negation, multiplication, shifting
 - Summary
- Representations in memory, pointers, strings

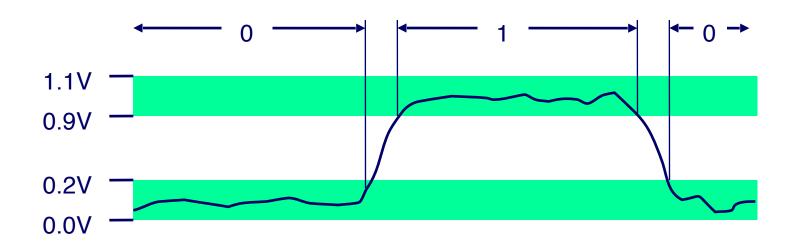
Everything is bits

- Each bit is 0 or 1
- By encoding/interpreting sets of bits in various ways
 - Computers determine what to do (instructions)
- Why bits? Electronic Implementation



Everything is bits

- Each bit is 0 or 1
- By encoding/interpreting sets of bits in various ways
 - Computers determine what to do (instructions)
- Why bits? Electronic Implementation
 - Transistor has two states: presence of a high voltage ("1"); presence of a low voltage ("0")

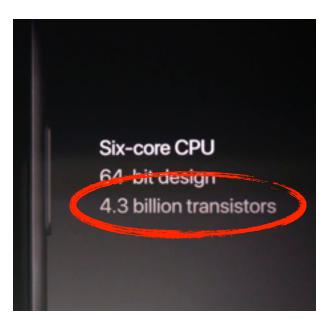


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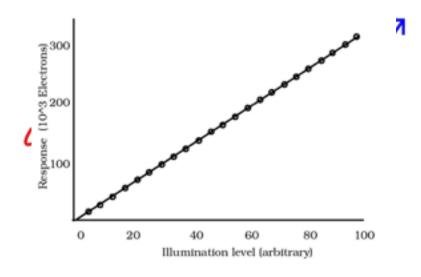


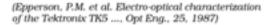


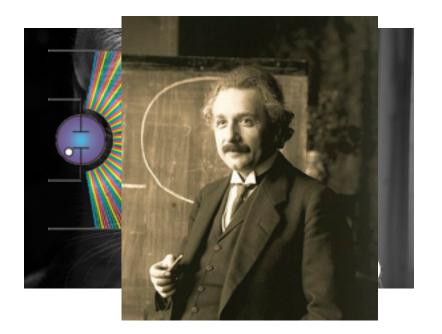


Aside: Why Limit Ourselves Only to Binary?

- Voltage is continuous. We can interpret it however we want.
- Classic Example: Camera Sensor
 - Photoelectric Effect







Binary Notation

- Base 2 Number Representation
 - e.g., $1011_2 = 11_{10}$
- Weighted Positional Notation
 - Each bit has a weight depending on its position

•
$$b_3b_2b_1b_0 = b^{0*}2^0 + b^{1*}2^1 + b^{2*}2^2 + b^{3*}2^3$$

•
$$1011_2 = 1*2^0 + 1*2^1 + 0*2^2 + 1*2^3 = 11_{10}$$

Binary Arithmetic

Decimal	Binary
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111
8	1000
9	1001
10	1010
11	1011
12	1100
13	1101
14	1110
15	1111

Hexdecimal (Hex) Notation

- Base 16 Number Representation
 - Use characters '0' to '9' and 'A' to 'F'
 - Four bits per Hex digit
 - $111111110_2 = FE_{16}$
- Write FA1D37B₁₆ in C as
 - 0xFA1D37B
 - 0xfa1d37b

Hex	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
Α	10	1010
В	11	1011
С	12	1100
D	13	1101
Е	14	1110
F	15	1111

Bit, Byte, Word

- Byte = 8 bits
 - Binary 0000000₂ to 11111111₂; Decimal: 0₁₀ to 255₁₀; Hex: 00₁₆ to FF₁₆
 - Least Significant Bit (LSb) vs. Most Significant Bit (MSb)



- Word = 4 Bytes (32-bit machine) / 8 Bytes (64-bit machine)
 - Least Significant Byte (LSB) vs. Most Significant Byte (MSB)

Questions?

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Boolean Algebra

- Developed by George Boole in 19th Century
 - Algebraic representation of logic
 - Encode "True" as 1 and "False" as 0

And

A&B = 1 when both A=1 and B=1

\frown	•
U	

- A | B = 1 when either A=1 or B=1

&	0	1
0	0	0
1	0	1

Ι	0	1
0	0	1
1	1	1

Not

- ~A = 1 when A=0

~	
0	1
1	0

Exclusive-Or (Xor)

- A^B = 1 when either A=1 or B=1, but not both

٨	0	1
0	0	1
1	1	0

General Boolean Algebras

- Operate on Bit Vectors
 - Operations applied bitwise

```
01101001 01101001 01101001

& 01010101 | 01010101 ^ 01010101 ~ 01010101

01000001 01111101 00111100 10101010
```

All of the Properties of Boolean Algebra Apply

Bit-Level Operations in C

- Operations &, I, ~, ^ Available in C
 - Apply to any "integral" data type
 - long, int, short, char, unsigned
 - View arguments as bit vectors
 - Arguments applied bit-wise
- Examples (Char data type)
 - $\sim 0 \times 41 \rightarrow 0 \times BE$
 - $\sim 01000001_2 \rightarrow 10111110_2$
 - $\sim 0 \times 00 \rightarrow 0 \times FF$
 - $\sim 0000000002 \rightarrow 11111111112$
 - $0x69 \& 0x55 \rightarrow 0x41$
 - 01101001_2 & $01010101_2 \rightarrow 01000001_2$
 - $0x69 \mid 0x55 \rightarrow 0x7D$
 - $01101001_2 \mid 01010101_2 \rightarrow 011111101_2$

Contrast: Logic Operations in C

- Contrast to Logical Operators
 - &&, II, !
 - View 0 as "Fals"
 - Anything ponzer
 - Always
 - Early t
- Examples
 - !0x41
 - !0x00
 - !!0x41

Watch out for && vs. & (and || vs. |)... one of the more common oopsies in C programming

- 0x69 && 0x33 → 0x01
- $0x69 | 1 0x55 \rightarrow 0x01$
- p && *p (avoids null pointer access)

Shift Operations

- Left Shift: x << y
 - Shift bit-vector **x** left **y** positions
 - Throw away extra bits on left
 - Fill with 0's on right
- Right Shift: x >> y
 - Shift bit-vector **x** right **y** positions
 - Throw away extra bits on right
 - Logical shift
 - Fill with 0's on left
 - Arithmetic shift
 - Replicate most significant bit on left
- Undefined Behavior
 - Shift amount < 0 or ≥ word size

Argument x	01100010
<< 3	00010 <i>000</i>
Log. >> 2	00011000
Arith. >> 2	00011000

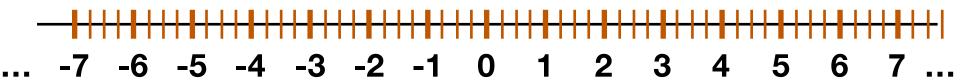
Argument x	10100010
<< 3	00010 <i>000</i>
Log. >> 2	<i>00</i> 101000
Arith. >> 2	<i>11</i> 101000

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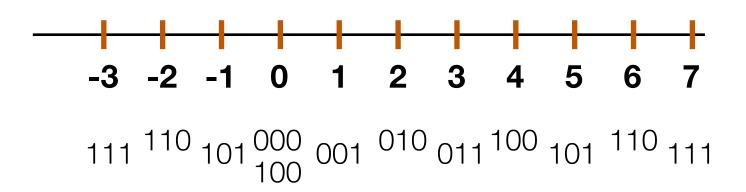
Representing Numbers in Binary

- What numbers do we need to represent in bits?
 - Integer (Negative and Non-negative)
 - Fractions
 - Irrationals



Encoding Negative Numbers

- So far we have been discussing non-negative numbers: so called unsigned. How about negative numbers?
- Solution 1: Sign-magnitude
 - First bit represents sign; 0 for positive; 1 for negative
 - The rest represents magnitude



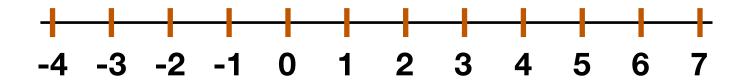
Sign-Magnitude Implications

- Bits have different semantics
 - Two zeros...
 - Normal arithmetic doesn't work
 - Make hardware design harder

Binary
000
001
010
011
100
101
110
111

Encoding Negative Numbers

Solution 2: Two's Complement



	Signed	Unsigned	Bit
	Weight	Weight	Position
	0	0	0
	1	1	1
	2	2	2
	-4	4	3
Stage -			

Signed	Unsigned	Binary
0	0	000
1	1	001
2	2	010
3	3	011
-4 -3 -2	4	100
-3	5	101
-2	6	110
-1	7	111

Two-Complement Encoding Example

x = 15213: 00111011 01101101y = -15213: 11000100 10010011

Weight	152	213	-152	213
1	1	1	1	1
2	0	0	1	2
4	1	4	0	0
8	1	8	0	0
16	0	0	1	16
32	1	32	0	0
64	1	64	0	0
128	0	0	1	128
256	1	256	0	0
512	1	512	0	0
1024	0	0	1	1024
2048	1	2048	0	0
4096	1	4096	0	0
8192	1	8192	0	0
16384	0	0	1	16384
-32768	0	0	1	-32768
Sum		15213		-15213

Two-Complement Implications

- Only 1 zero
- Usual arithmetic still works
- There is a bit that represents sign!
- Most widely used in today's machines

	010
+)	101
	111

Signed	Binary
0	000
1	001
2	010
3	011
-4	100
-3 -2	101
-2	110
-1	111

Numeric Ranges

Unsigned Values

•
$$UMax = 2^{w} - 1$$

Two's Complement Values

■
$$TMin = -2^{w-1}$$

100...0

■
$$TMax = 2^{w-1} - 1$$

011...1

Other Values

Values for W = 16

	Decimal	Hex	Binary
UMax	65535	FF FF	11111111 11111111
TMax	32767	7F FF	01111111 111111111
TMin	-32768	80 00	10000000 000000000
-1	-1	FF FF	11111111 11111111
0	0	00 00	00000000 00000000

Data Representations in C (in Bytes)

- By default variables are signed
- Unless explicitly declared as unsigned (e.g., unsigned int)
- Signed variables use two-complement encoding

C Data Type	32-bit	64-bit
char	1	1
short	2	2
int	4	4
long	4	8

Data Representations in C (in Bytes)

	W			
	8	16	32	64
UMax	255	65,535	4,294,967,295	18,446,744,073,709,551,615
TMax	127	32,767	2,147,483,647	9,223,372,036,854,775,807
TMin	-128	-32,768	-2,147,483,648	-9,223,372,036,854,775,808

C Data Type	32-bit	64-bit
char	1	1
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int	4	4
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C Language

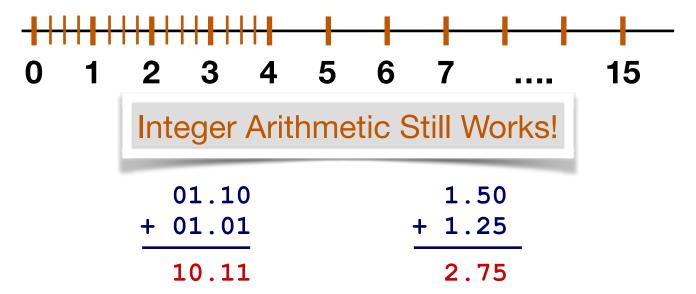
- •#include <limits.h>
- Declares constants, e.g.,
 - \bullet ULONG_MAX
 - \bullet LONG_MAX
 - •LONG_MIN
- Values platform specific

Can We Represent Fractions in Binary?

- What does 10.01₂ mean?
- C.f., Decimal

•
$$12.45 = 1*10^{1} + 2*10^{0} + 4*10^{-1} + 5*10^{-2}$$

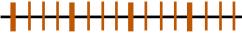
•
$$10.01_2 = 1^21 + 0^20 + 0^21 + 1^22 = 2.25_{10}$$



Decimal	Binary
0	00.00
0.25	00.01
0.5	00.10
0.75	00.11
1	01.00
1.25	01.01
1.5	01.10
1.75	01.11
2	10.00
2.25	10.01
2.5	10.10
2.75	10.11
3	11.00
3.25	11.01
3.5	11.10
3.75	11.11

Fixed-Point Representation

- Fixed interval between two representable numbers as long as the binary point stays fixed
 - Each bit represents 0.25₁₀
- Fixed-point representation of numbers
 - Integer is one special case of fixed-point

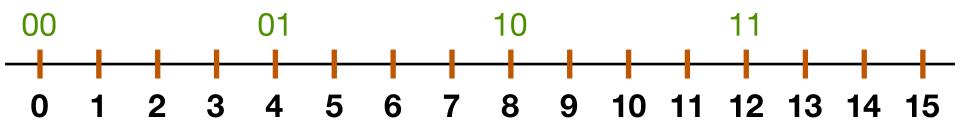


0 1 2 3

	01.10	
+	01.01	
	10.11	

Decimal	Binary
0	00.00
0.25	00.01
0.5	00.10
0.75	00.11
1	01.00
1.25	01.01
1.5	01.10
1.75	01.11
2	10.00
2.25	10.01
2.5	10.10
2.75	10.11
3	11.00
3.25	11.01
3.5	11.10
3.75	11.11

Aside: Quantization



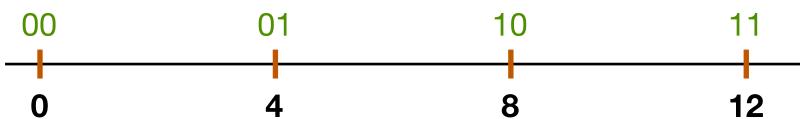
- Representing all integers precisely requires 4 bits
- What if
 - 1, 2
 - 5, 6
 - We

Note that this is different from "base 4"

- $10_4 = 1 * 4^1 + 0 * 4^0 = 4$
- Every increment still only increments 1
- That is, 1 bit represents 4₁₀
 - 10_2 becomes $4 * (1 * 2^1) = 8$
 - Every time we increment a bit, the value is incremented by 4
 - 1, 2, 3 are represented approximately by 10₂

Aside: Quantization

Questions?



- Saves storage space and improves computation speed
 - 50% space saving

