

# **CSC 252: Computer Organization**

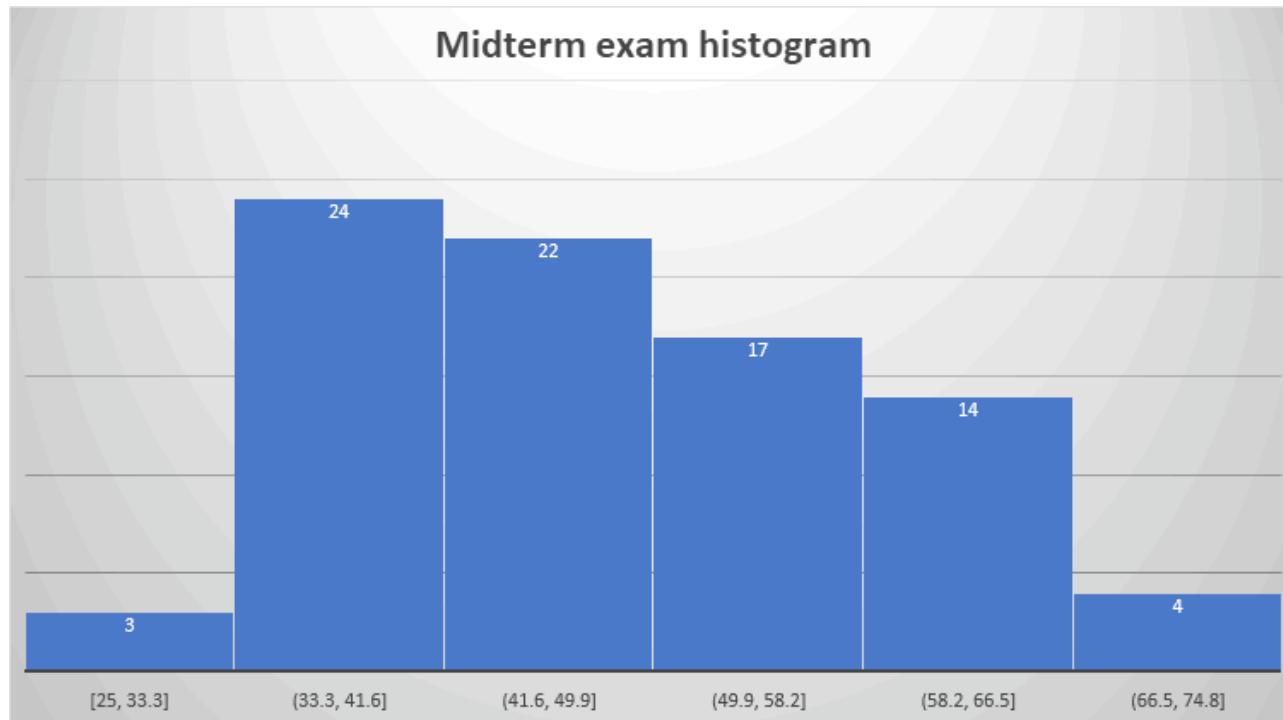
## **Spring 2021: Lecture 17**

Instructor: Yuhao Zhu

Department of Computer Science  
University of Rochester

# Announcements

- Mid-term grades released. Solution on the website.
- Talk to a TA if you have doubts. Make an appointment if you can't make any TA office hours.
- Make sure BB grade is the same as that in Gradescope.



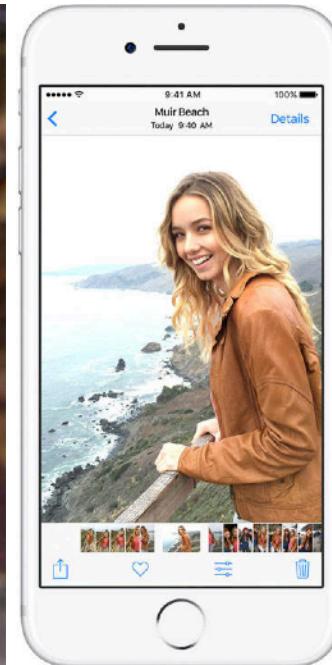
# A Shameless Plug

- CSC 292/572 Mobile Visual Computing. Fall 2021
- <https://www.cs.rochester.edu/courses/572/fall2020/index.html>

Portrait Mode



HDR Mode



# A Shameless Plug

- CSC 292/572 Mobile Visual Computing. Fall 2021
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Computer graphics,  
physically-based rendering



# A Shameless Plug

- CSC 292/572 Mobile Visual Computing. Fall 2021
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360 video



Video streaming and compression

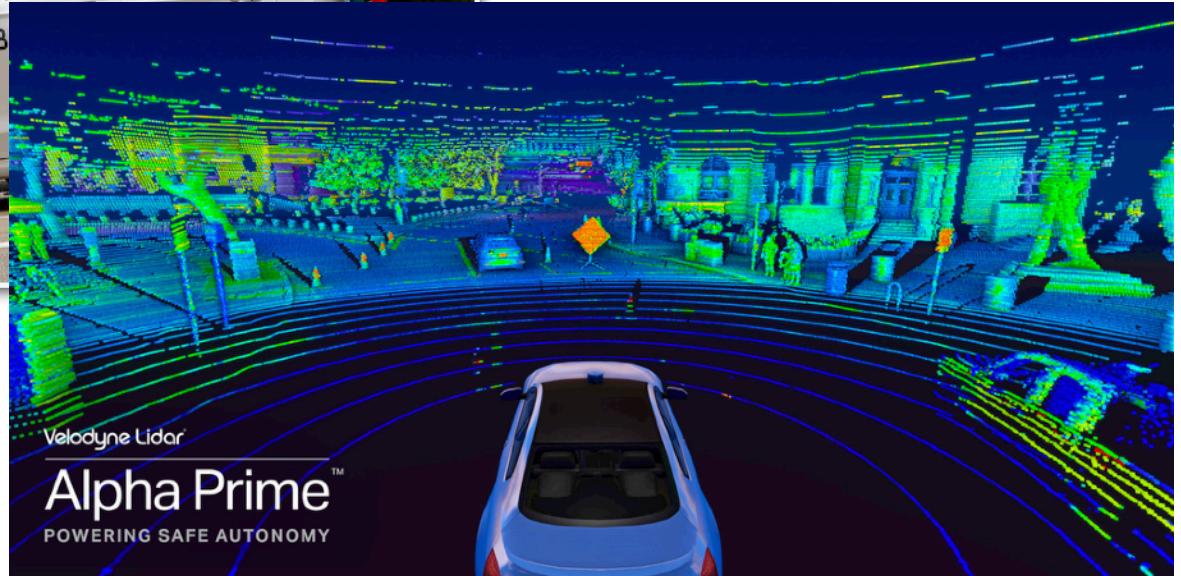


# A Shameless Plug

- CSC 292/572 Mobile Visual Computing. Fall 2021
- <https://www.cs.rochester.edu/courses/572/fall2020/index.html>



**How self-driving cars  
perceive and  
understand the world**



# A Shameless Plug

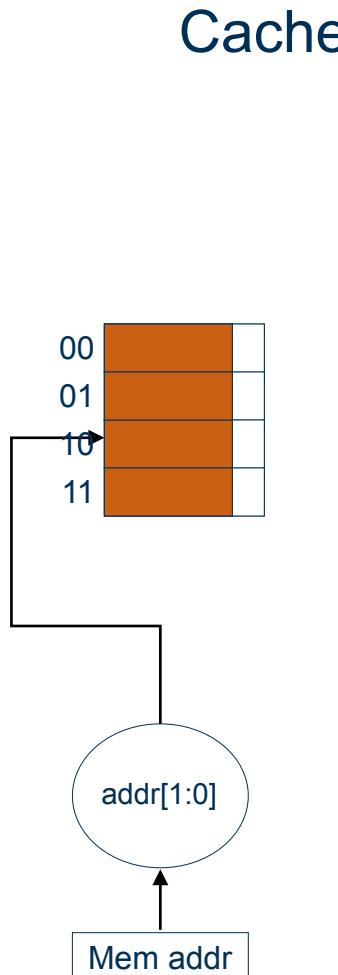
- CSC 292/572 Mobile Visual Computing. Fall 2021
- <https://www.cs.rochester.edu/courses/572/fall2020/index.html>



**Demystifying Augmented  
and Virtual Reality**



# Direct-Mapped Cache



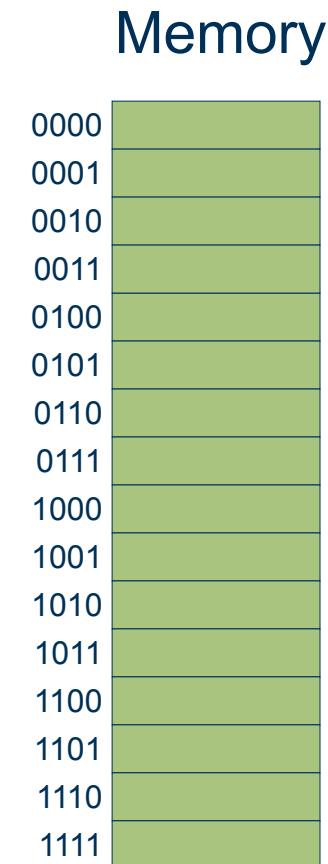
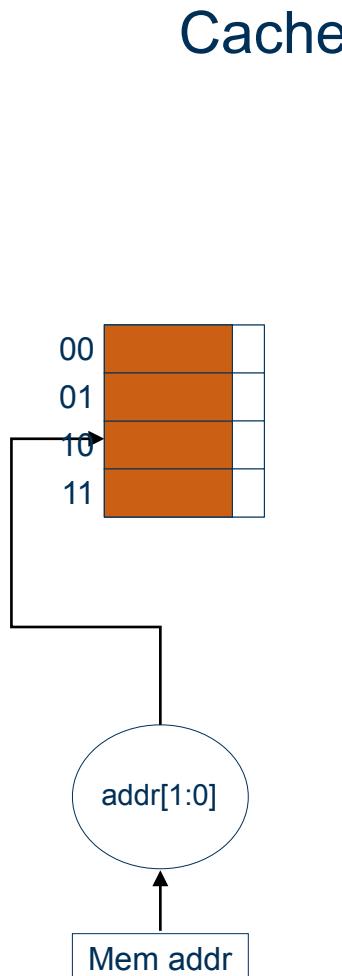
Memory

0000	
0001	
0010	
0011	
0100	
0101	
0110	
0111	
1000	
1001	
1010	
1011	
1100	
1101	
1110	
1111	

- Direct-Mapped Cache

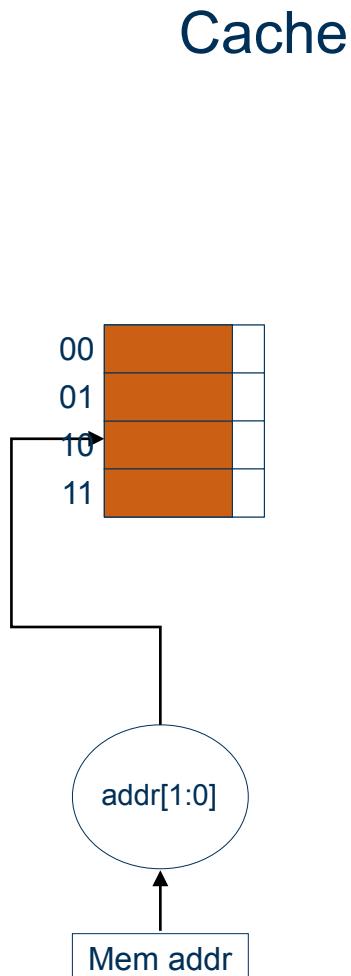
- $CA = ADDR[1], ADDR[0]$
- Always use the lower order address bits

# Direct-Mapped Cache



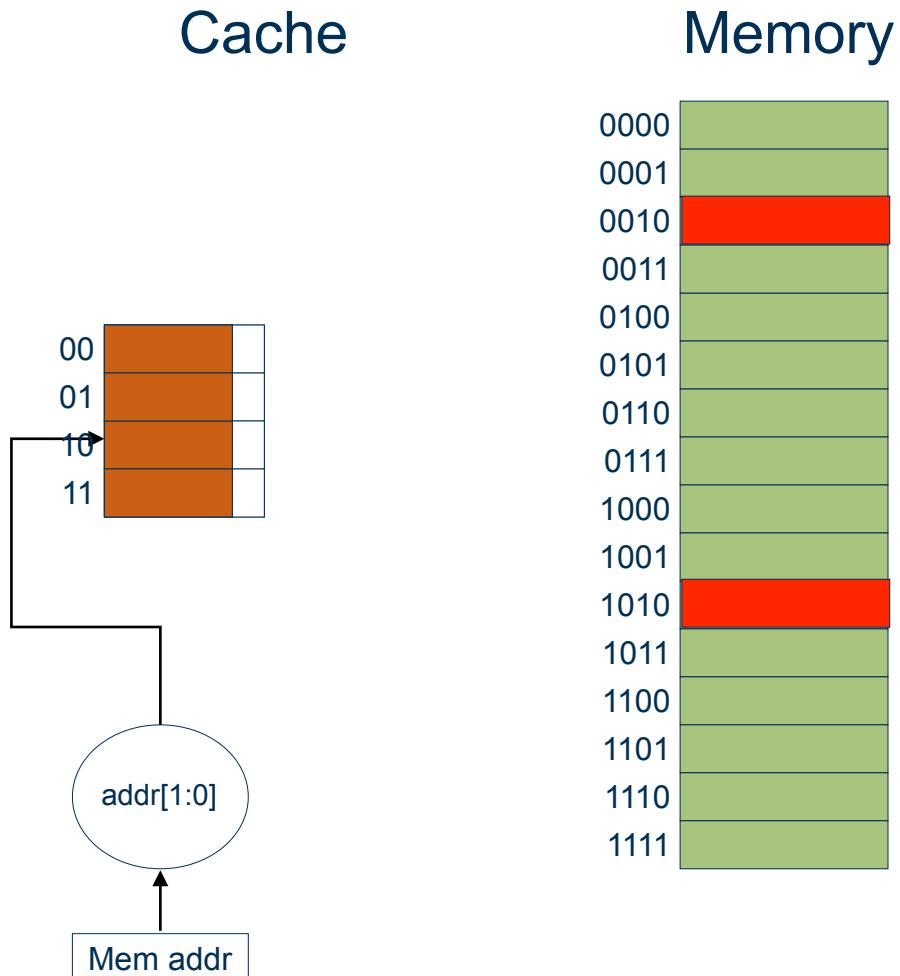
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  - $CA = ADDR[1], ADDR[0]$
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- Multiple addresses can be mapped to the same location

# Direct-Mapped Cache



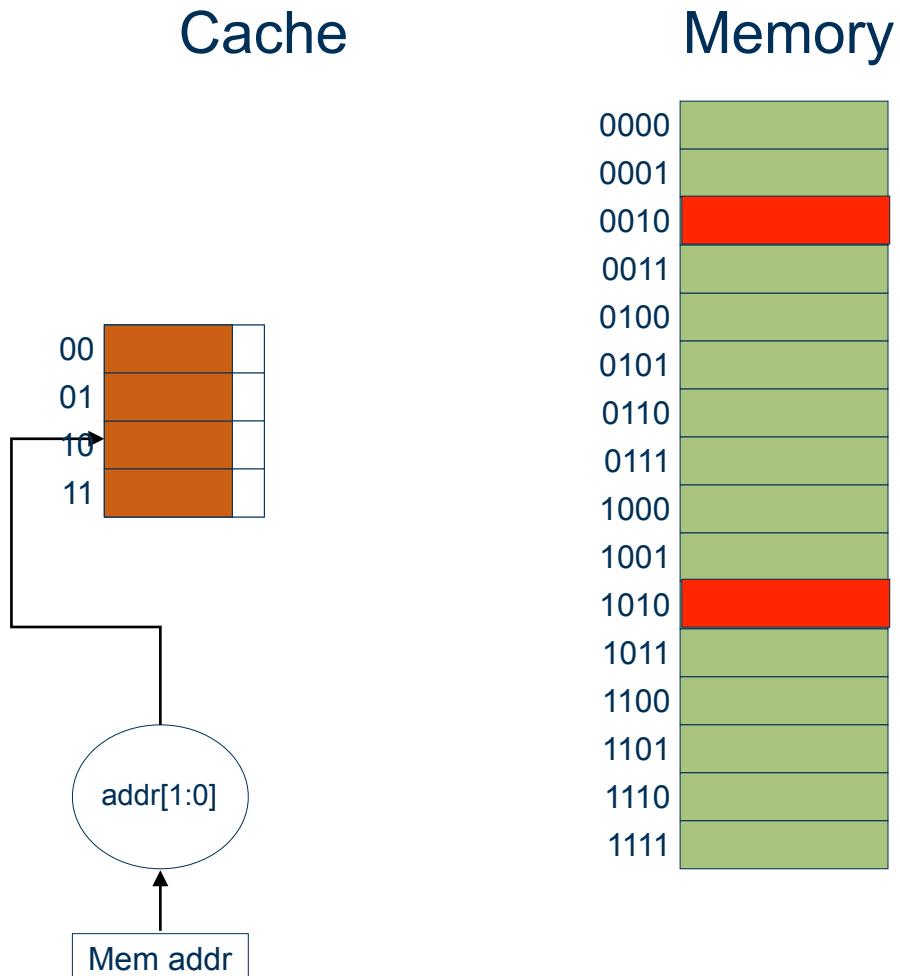
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  - $CA = ADDR[1], ADDR[0]$
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  - E.g., 0010 and 1010

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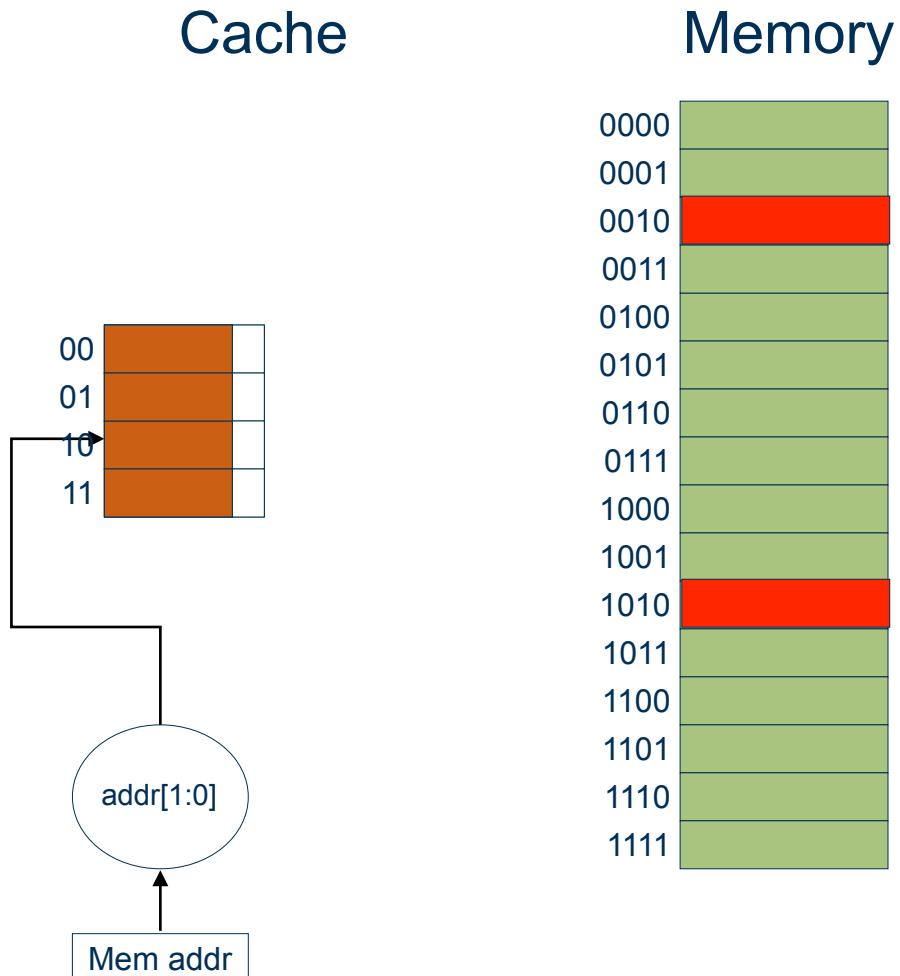
- Direct-Mapped Cache
  - $CA = ADDR[1], ADDR[0]$
  - Always use the lower order address bits
- Multiple addresses can be mapped to the same location
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- How do we differentiate between different memory locations that are mapped to the same cache location?

# Direct-Mapped Cache



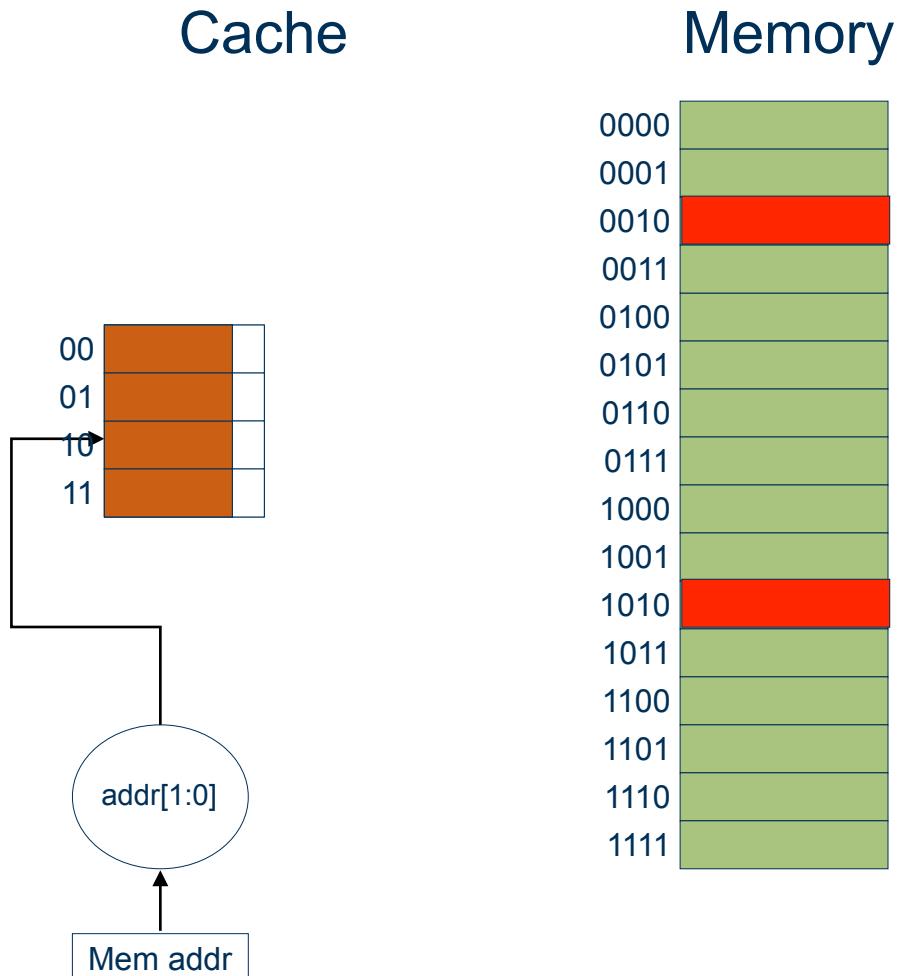
- Direct-Mapped Cache
  - CA = ADDR[1],ADDR[0]
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  - Add a tag field for that purpose

# Direct-Mapped Cache



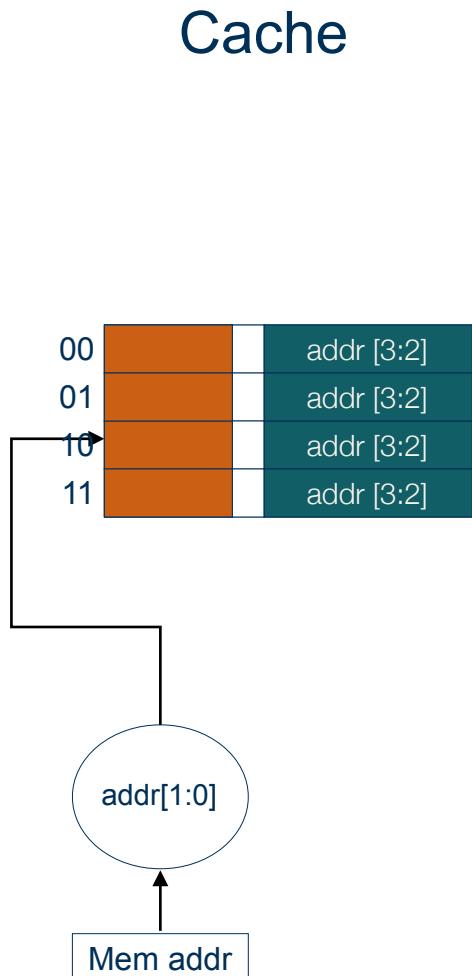
- **Direct-Mapped Cache**
  - $CA = ADDR[1], ADDR[0]$
  - Always use the lower order address bits
- **Multiple addresses can be mapped to the same location**
  - E.g., 0010 and 1010
- **How do we differentiate between different memory locations that are mapped to the same cache location?**
  - Add a tag field for that purpose
  - What should the tag field be?

# Direct-Mapped Cache



- **Direct-Mapped Cache**
  - $CA = ADDR[1], ADDR[0]$
  - Always use the lower order address bits
- Multiple addresses can be mapped to the same location
  - E.g., 0010 and 1010
- How do we differentiate between different memory locations that are mapped to the same cache location?
  - Add a tag field for that purpose
  - What should the tag field be?
  - $ADDR[3]$  and  $ADDR[2]$  in this particular example

# Direct-Mapped Cache



## Memory

0000	green
0001	green
0010	red
0011	green
0100	green
0101	green
0110	green
0111	green
1000	green
1001	green
1010	red
1011	green
1100	green
1101	green
1110	green
1111	green

- Direct-Mapped Cache

- $CA = ADDR[1], ADDR[0]$
- Always use the lower order address bits

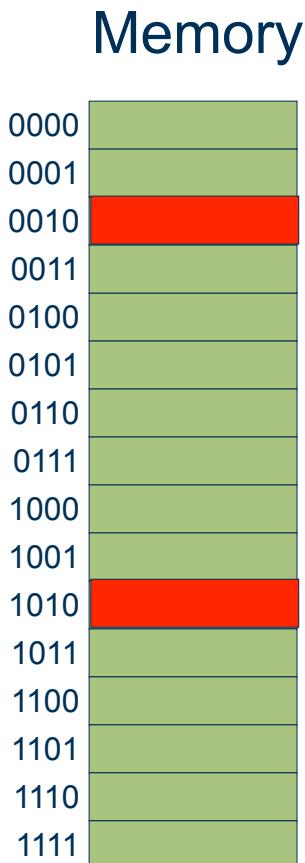
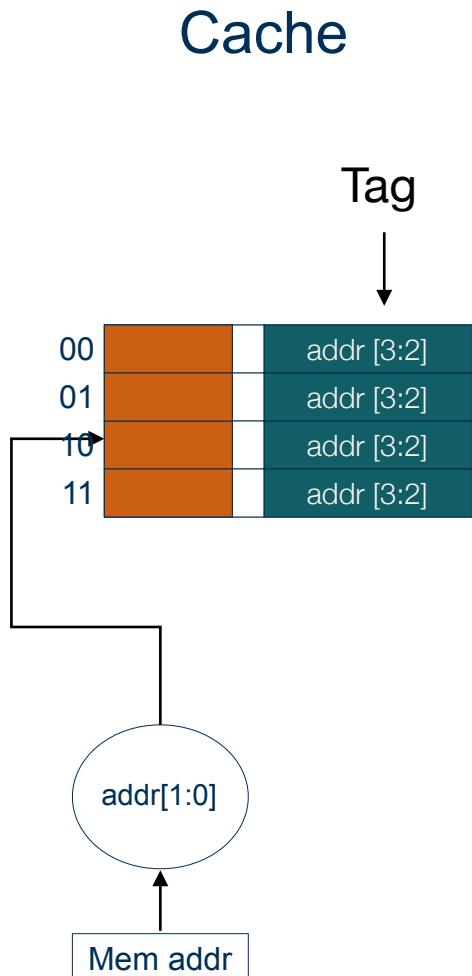
- Multiple addresses can be mapped to the same location

- E.g., 0010 and 1010

- How do we differentiate between different memory locations that are mapped to the same cache location?

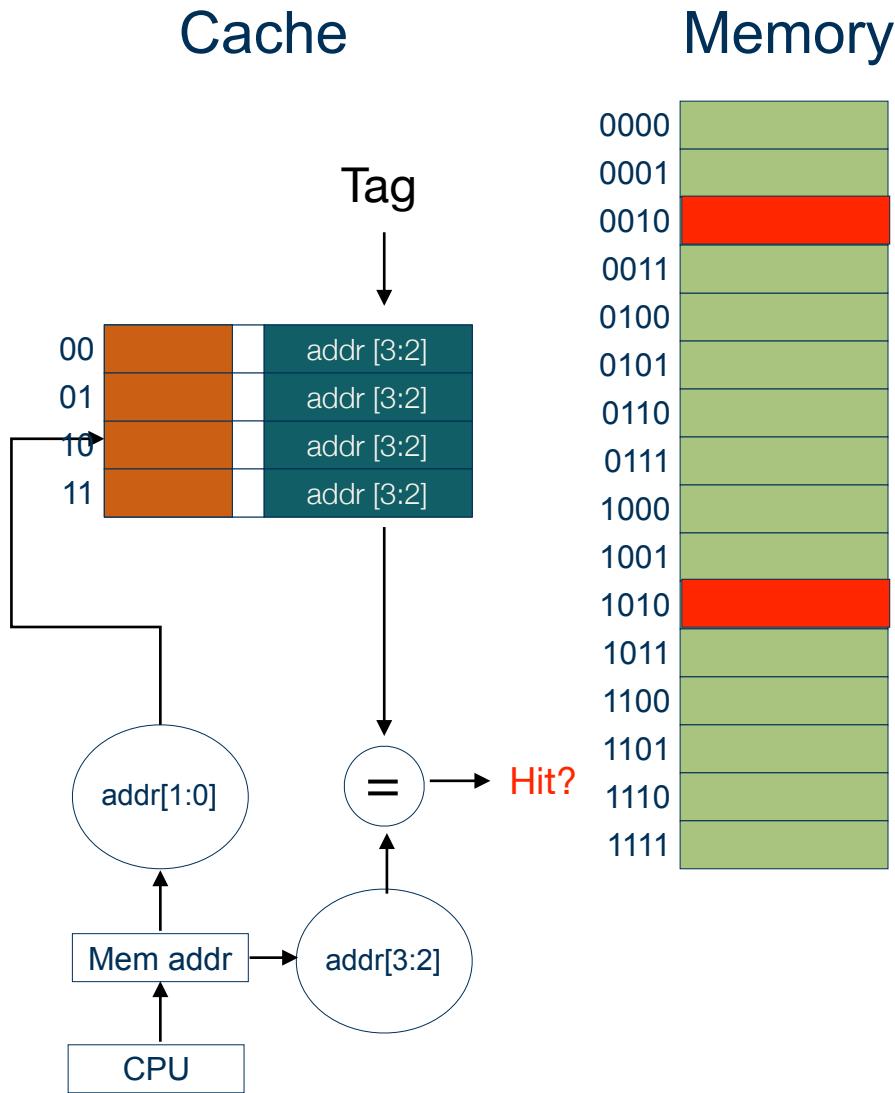
- Add a tag field for that purpose
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# Direct-Mapped Cache



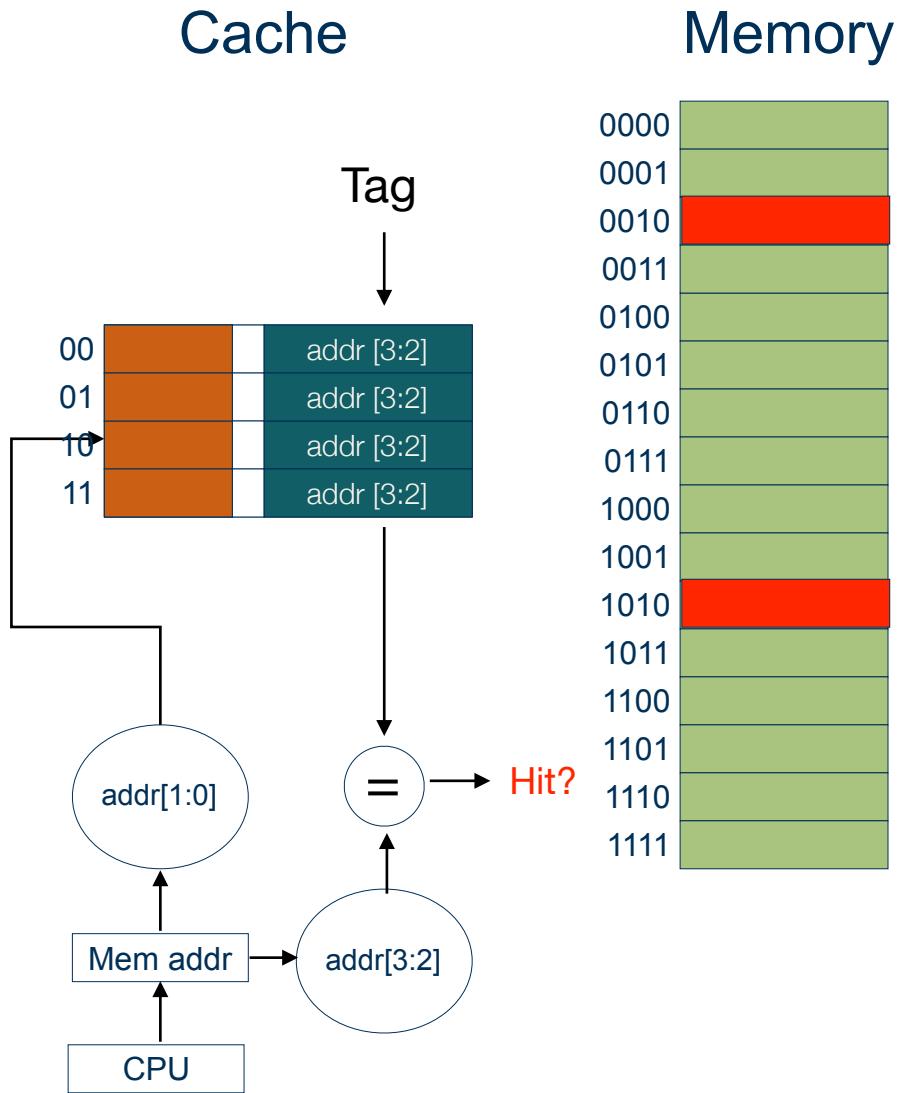
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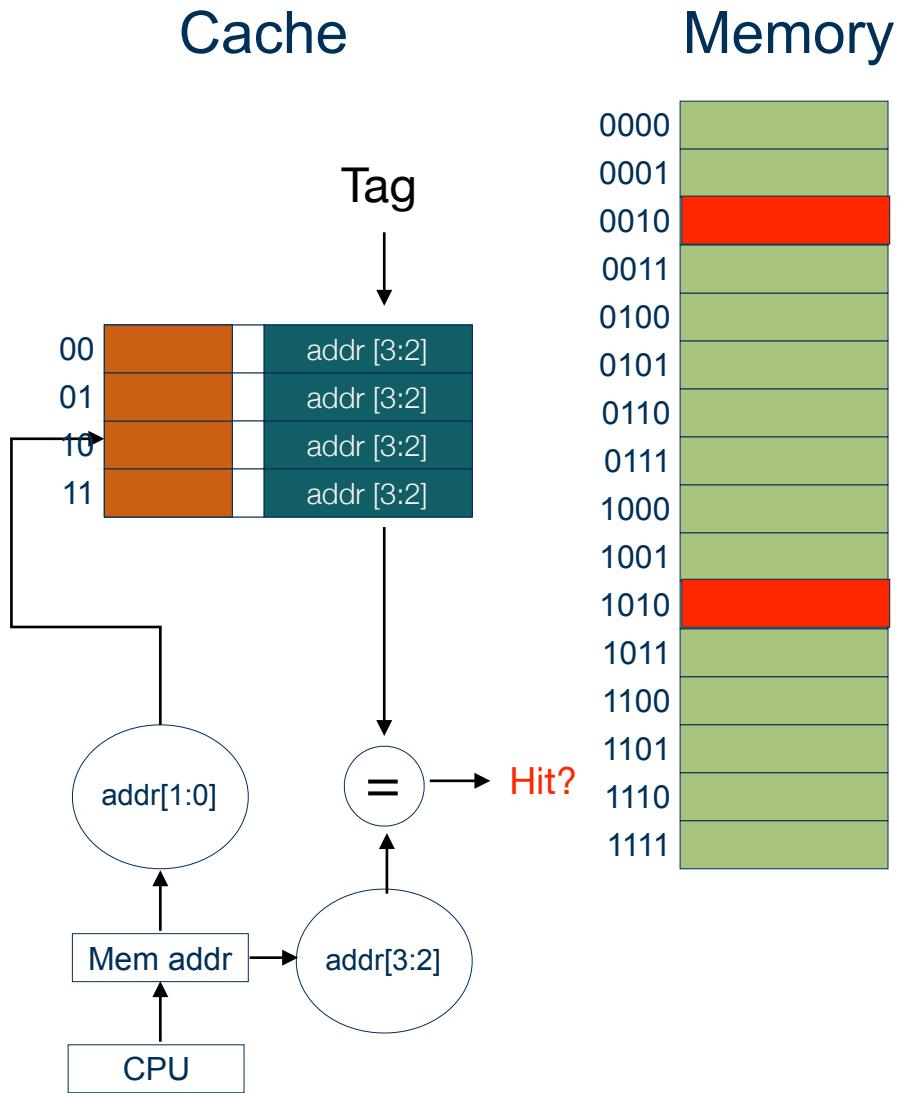
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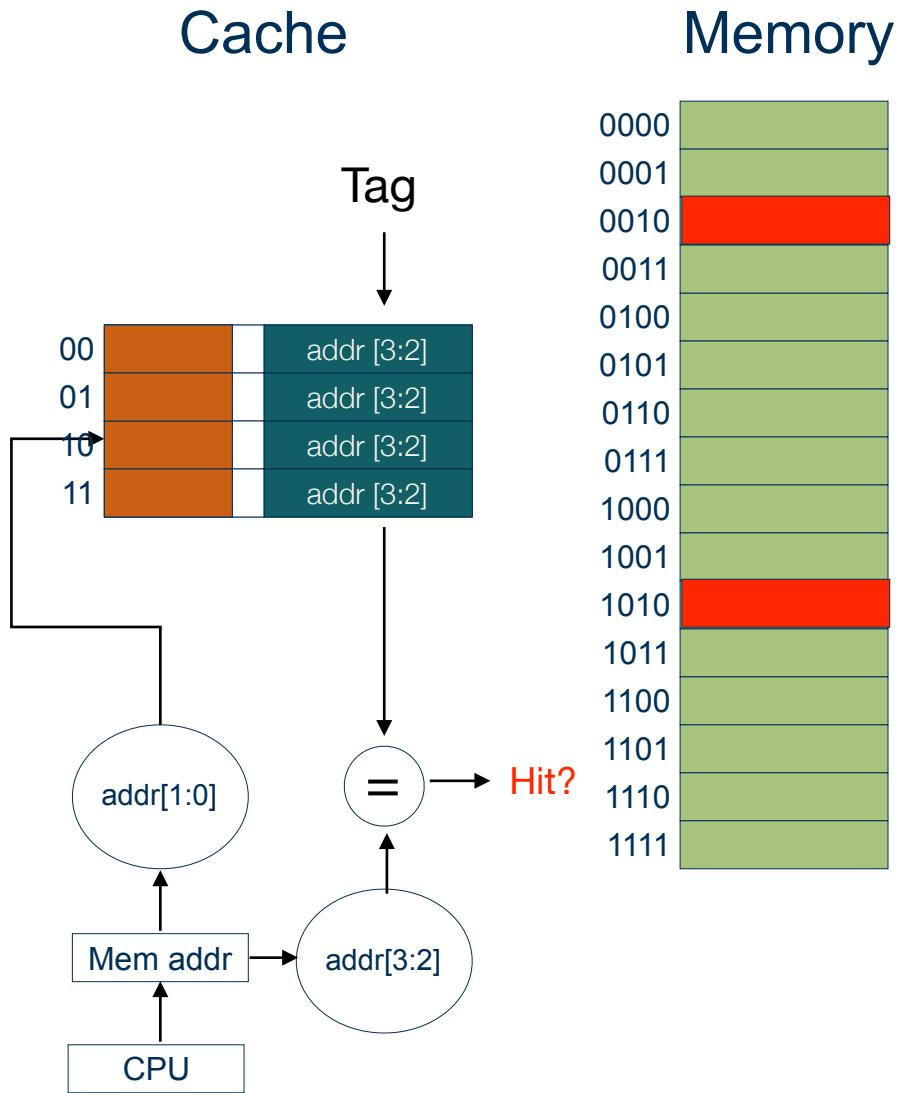
- Limitation: each memory location can be mapped to only one cache location.

# Direct-Mapped Cache



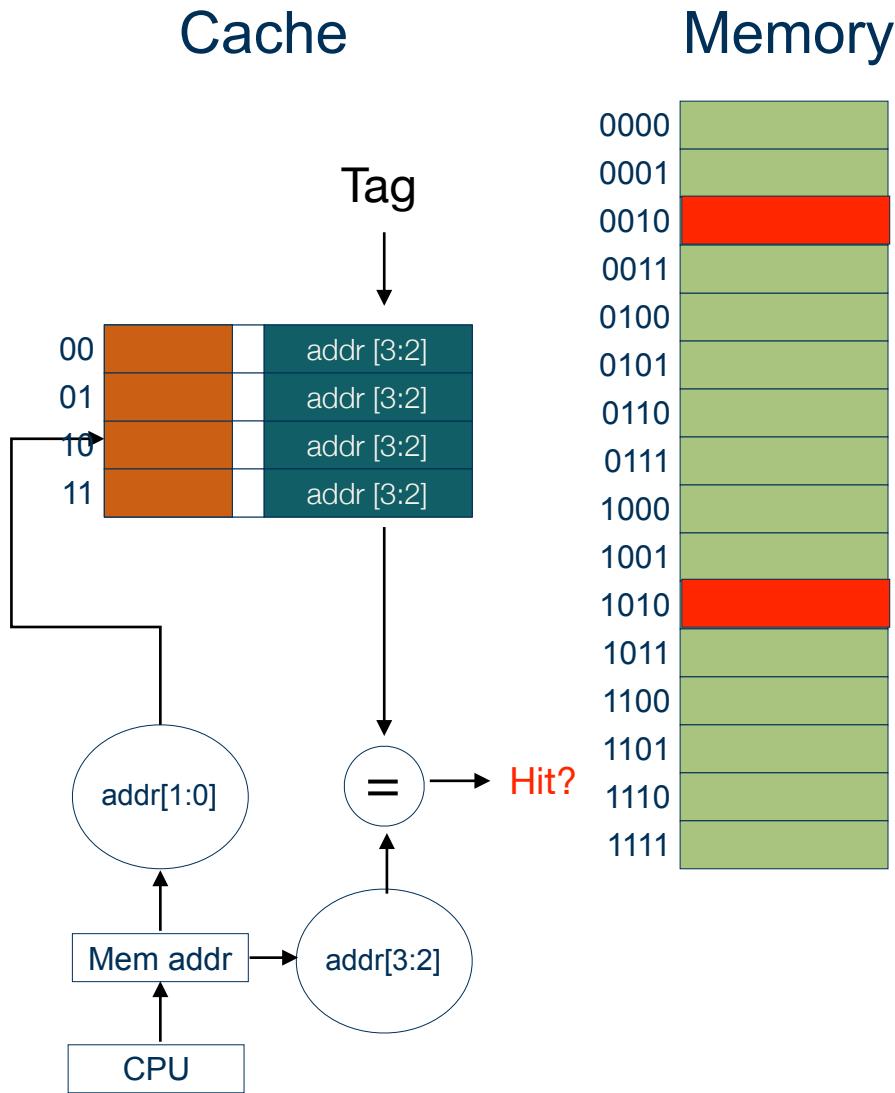
- Limitation: each memory location can be mapped to only one cache location.
- This leads to a lot of conflicts.

# Direct-Mapped Cache



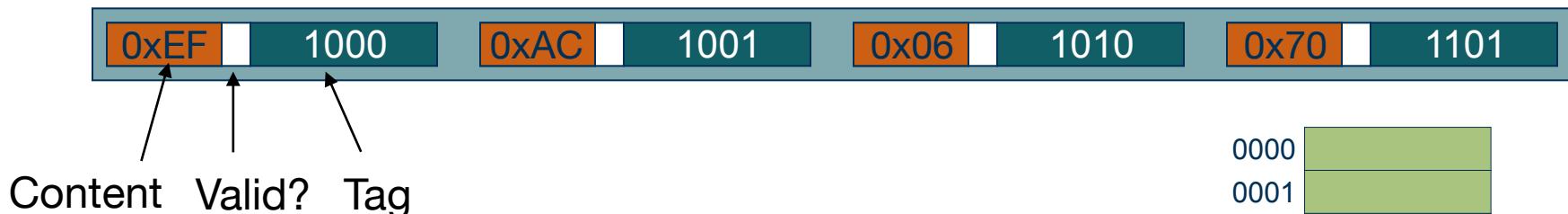
- Limitation: each memory location can be mapped to only one cache location.
- This leads to a lot of conflicts.
- How do we improve this?

# Direct-Mapped Cache



- Limitation: each memory location can be mapped to only one cache location.
- This leads to a lot of conflicts.
- How do we improve this?
- Can each memory location have the flexibility to be mapped to different cache locations?

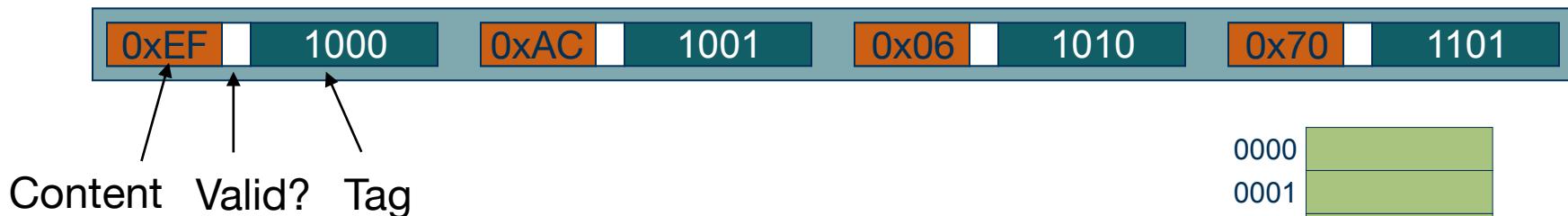
# Fully Associative Cache



- Every memory location can be mapped to any cache line in the cache.

0000	
0001	
0010	
0011	
0100	
0101	
0110	
0111	
1000	0xEF
1001	0xAC
1010	0x06
1011	
1100	
1101	0x70
1110	
1111	

# Fully Associative Cache



- Every memory location can be mapped to any cache line in the cache.
- Given a request to address A from the CPU, detecting cache hit/miss requires:
  - Comparing address A with all four tags in the cache (a.k.a., associative search)

0000	
0001	
0010	
0011	
0100	
0101	
0110	
0111	
1000	0xEF
1001	0xAC
1010	0x06
1011	
1100	
1101	0x70
1110	
1111	

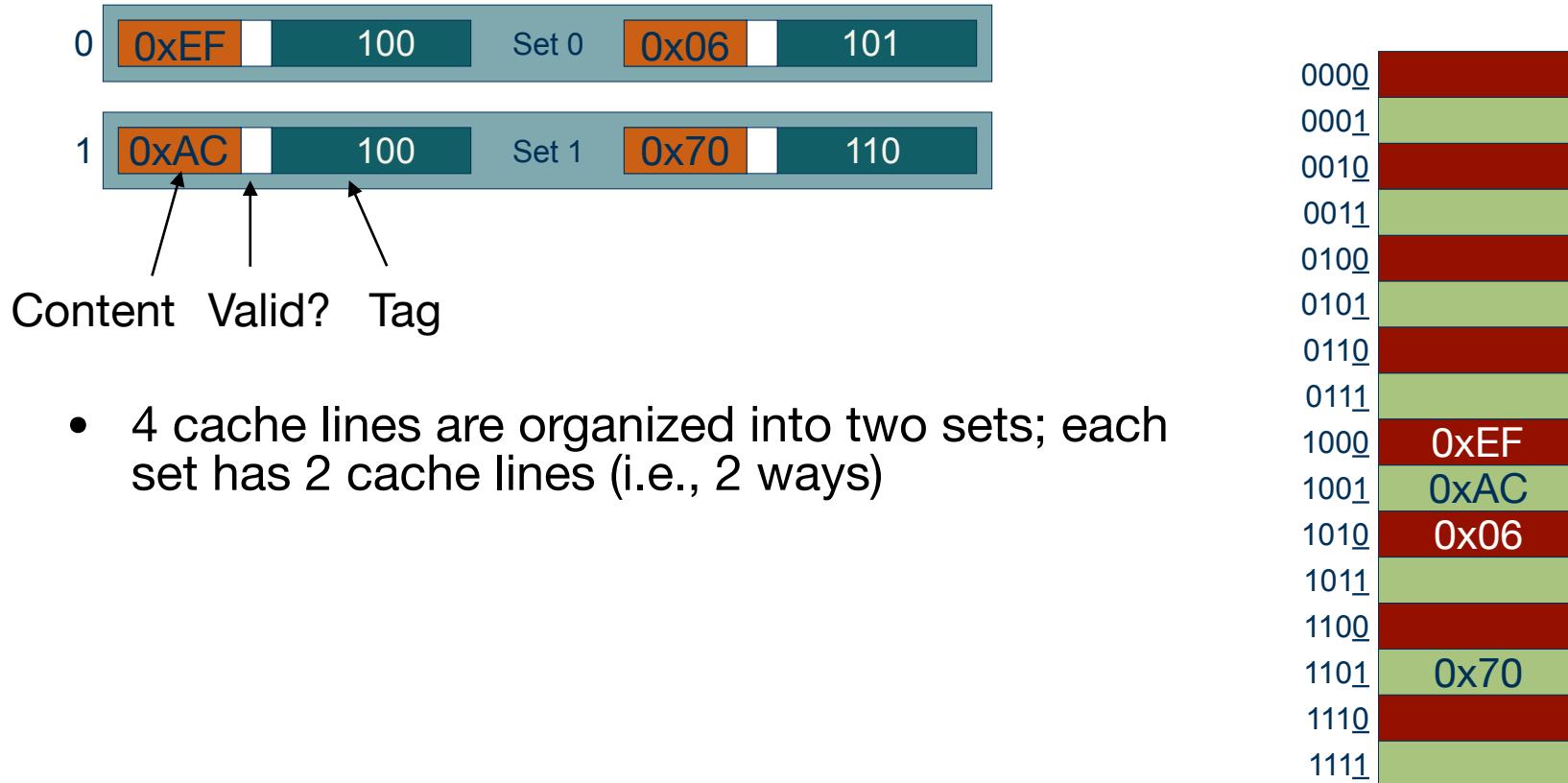
# A Few Terminologies



- A cache line: content + valid bit + tag bits
  - Valid bit + tag bits are “overhead”
  - Content is what you really want to store
  - But we need valid and tag bits to correctly access the cache

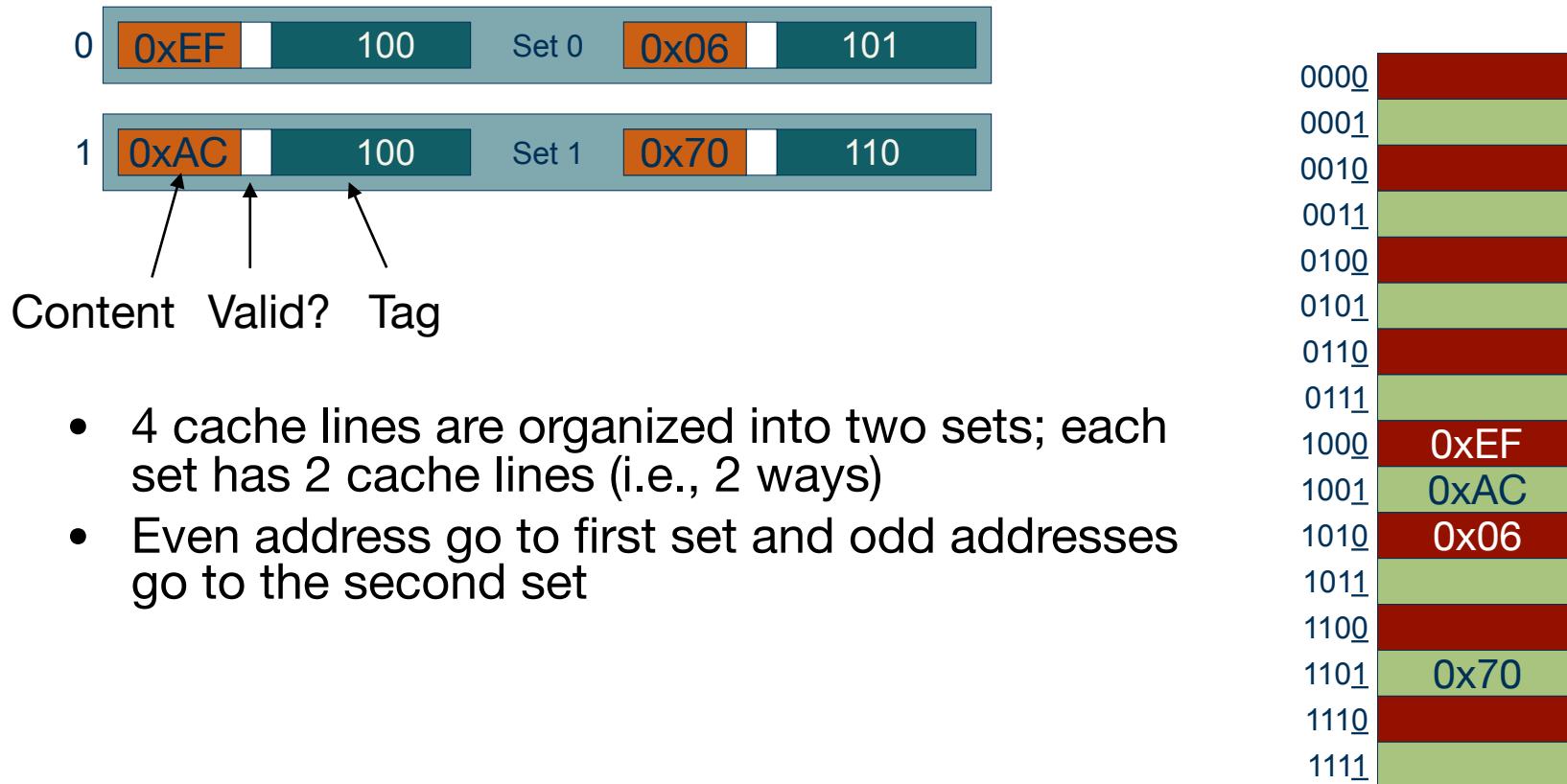
0000	
0001	
0010	
0011	
0100	
0101	
0110	
0111	
1000	0xEF
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1010	0x06
1011	
1100	
1101	0x70
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1111	

# A Middle Ground: 2-Way Associative Cache



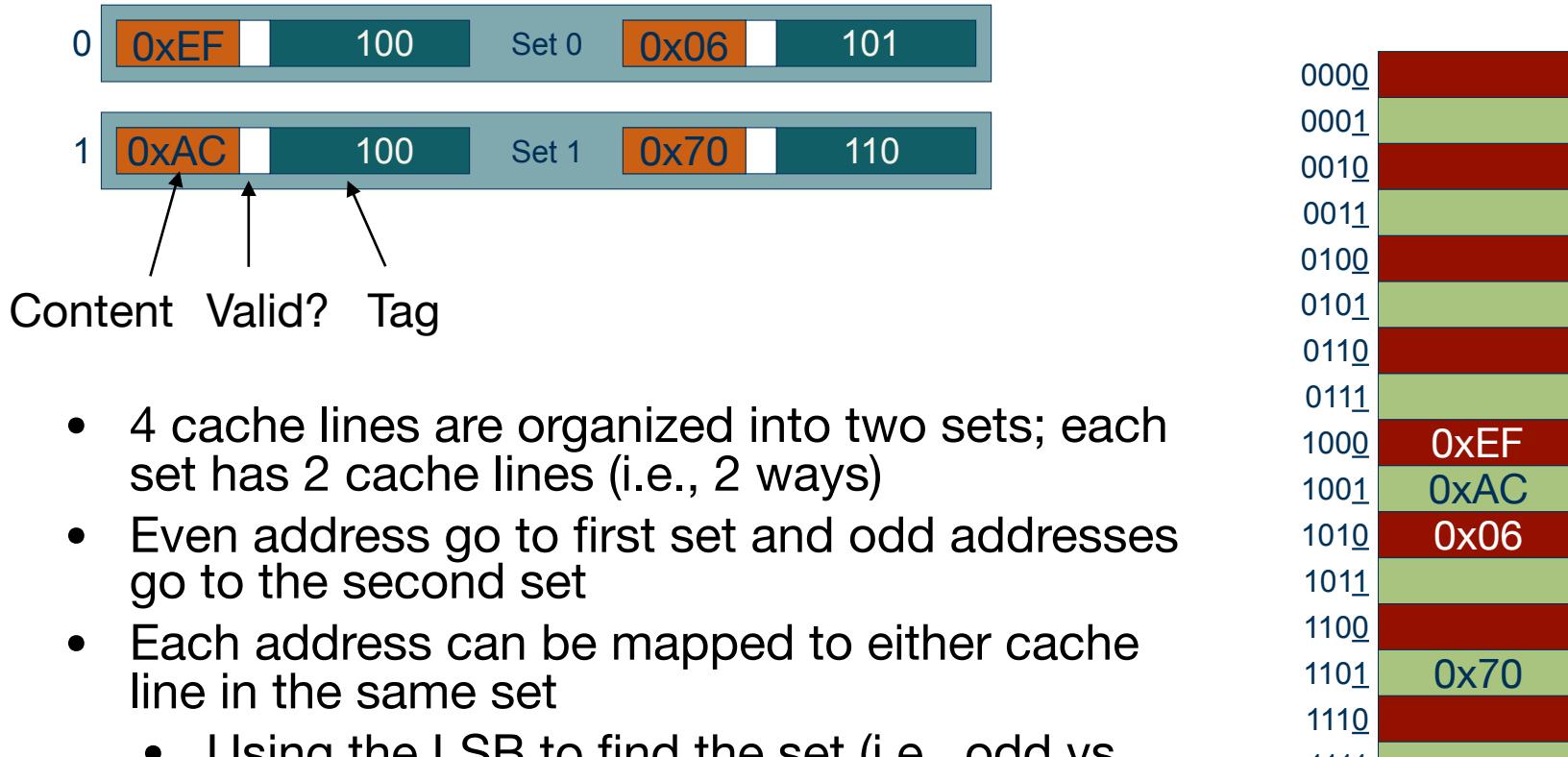
- 4 cache lines are organized into two sets; each set has 2 cache lines (i.e., 2 ways)

# A Middle Ground: 2-Way Associative Cache



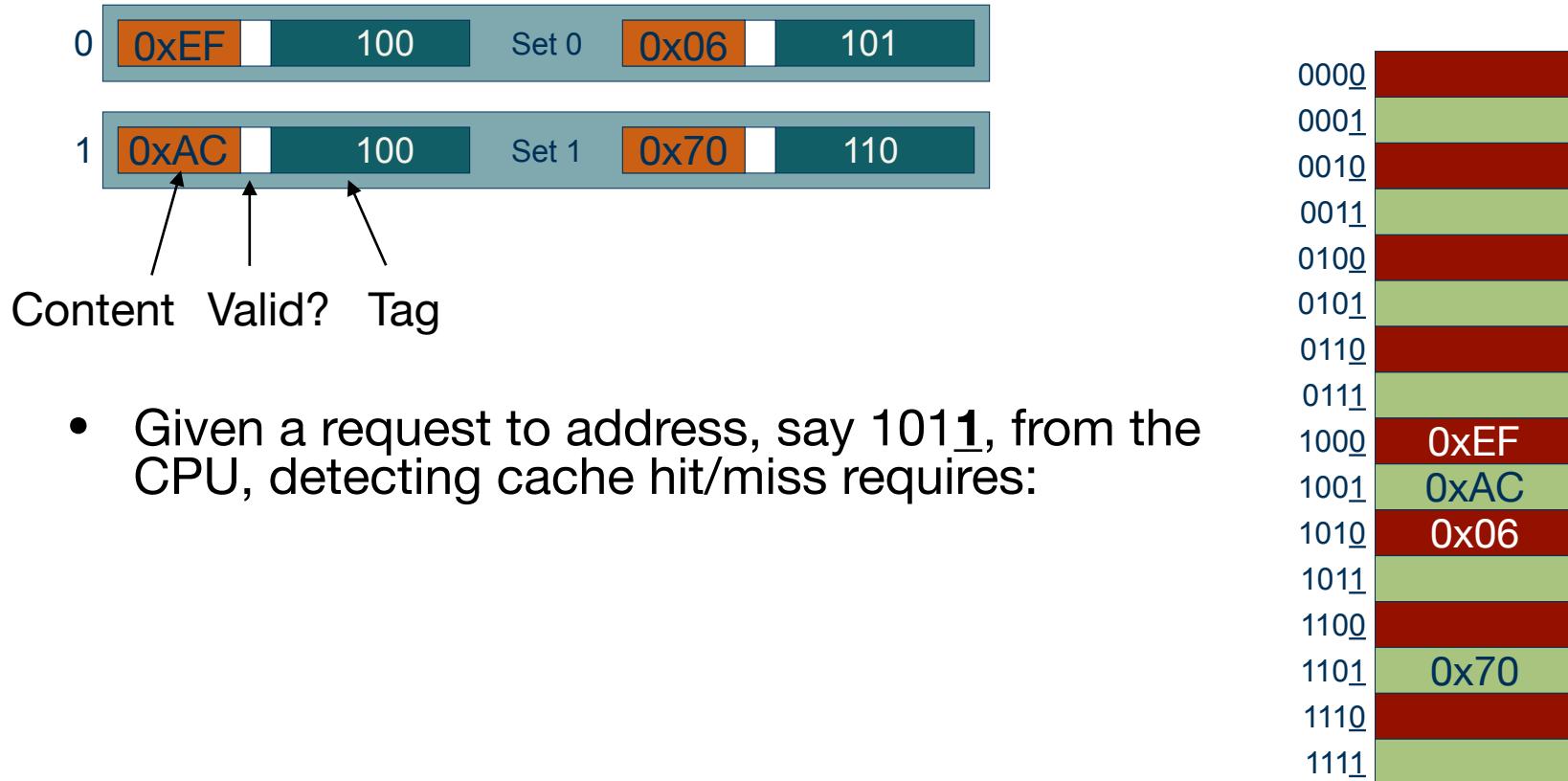
- 4 cache lines are organized into two sets; each set has 2 cache lines (i.e., 2 ways)
- Even address go to first set and odd addresses go to the second set

# A Middle Ground: 2-Way Associative Cache



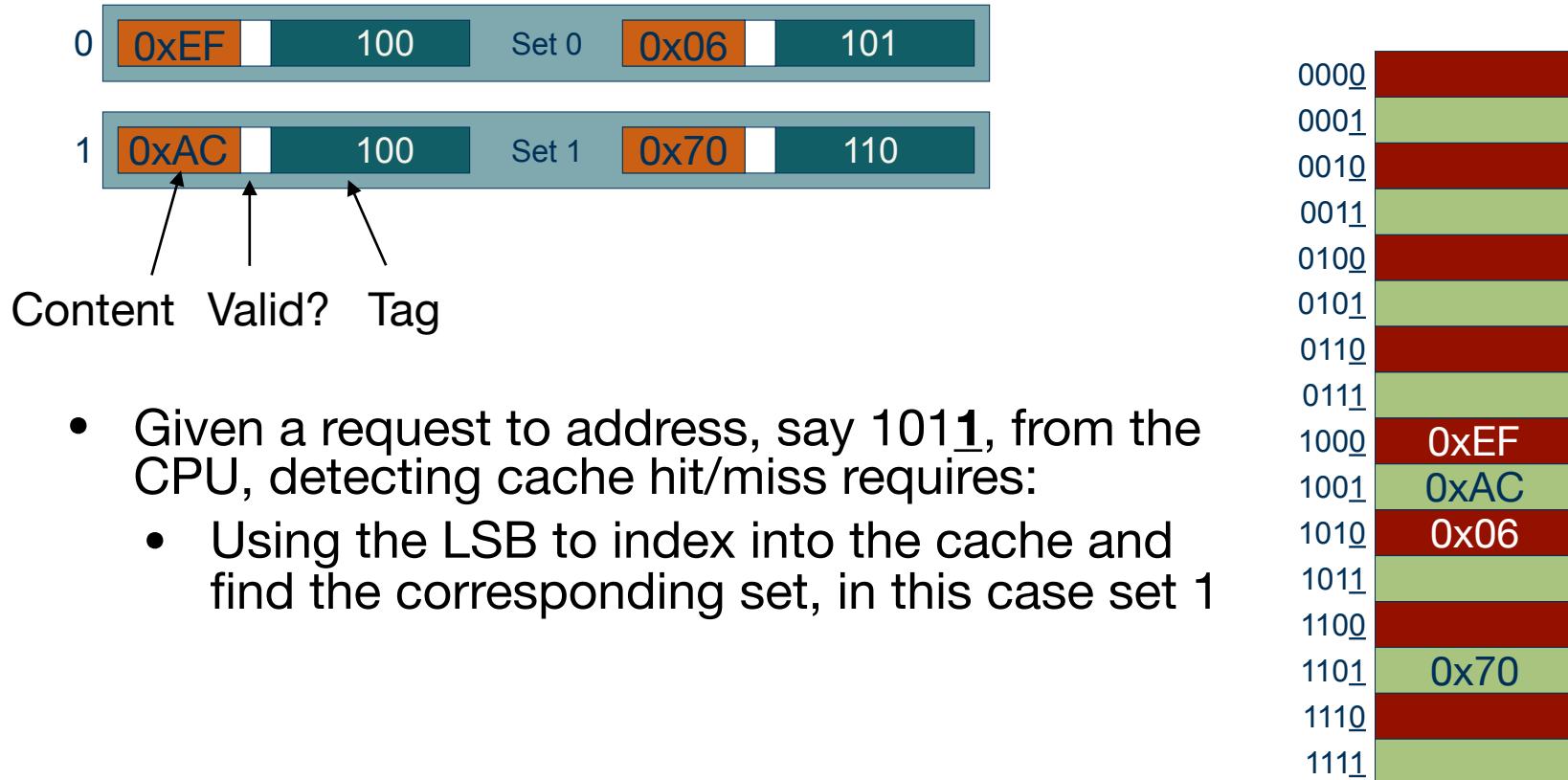
- 4 cache lines are organized into two sets; each set has 2 cache lines (i.e., 2 ways)
- Even addresses go to first set and odd addresses go to the second set
- Each address can be mapped to either cache line in the same set
  - Using the LSB to find the set (i.e., odd vs. even)
  - Tag now stores the higher 3 bits instead of the entire address

# 2-Way Associative Cache



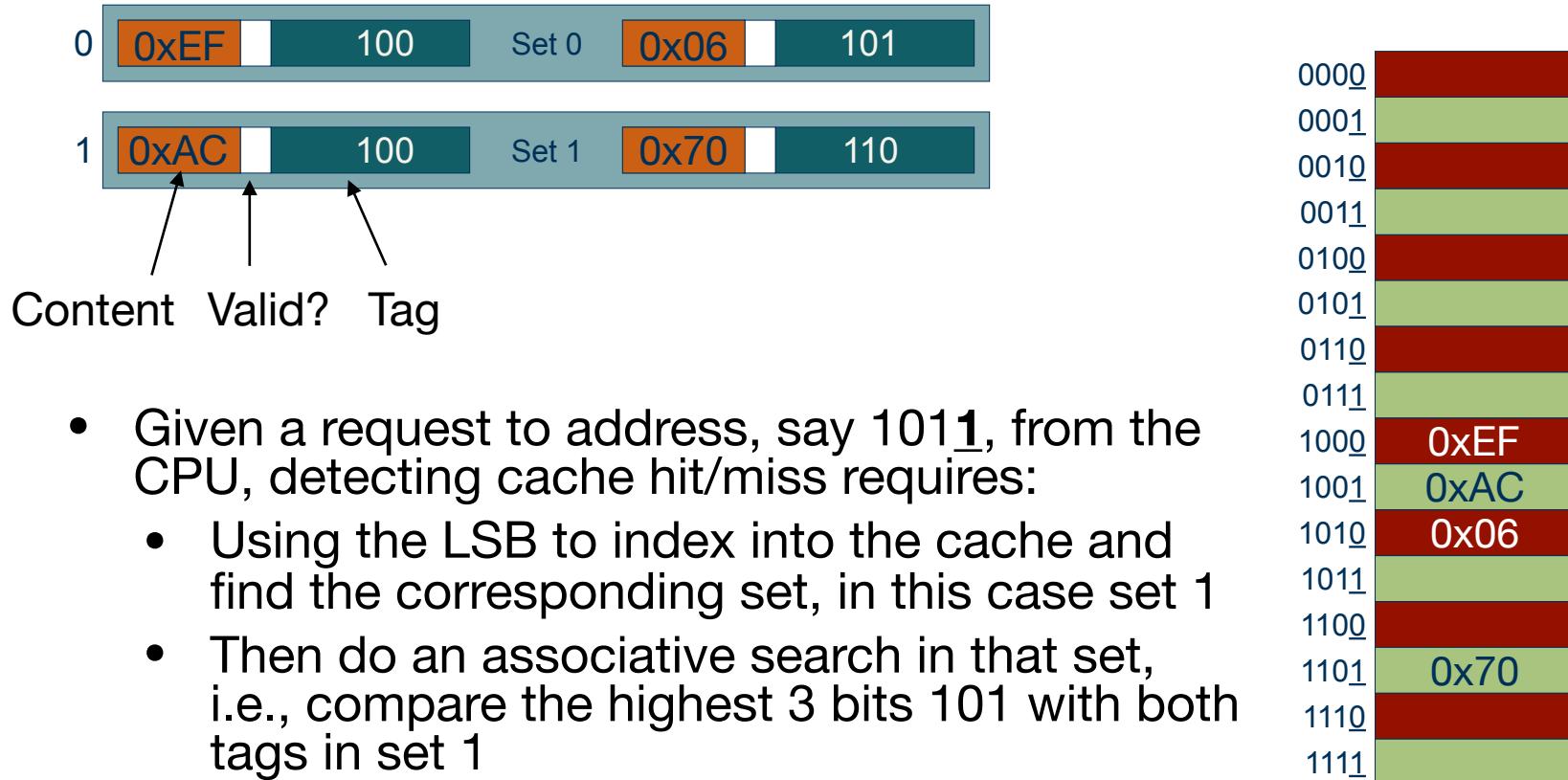
- Given a request to address, say **1011**, from the CPU, detecting cache hit/miss requires:

# 2-Way Associative Cache



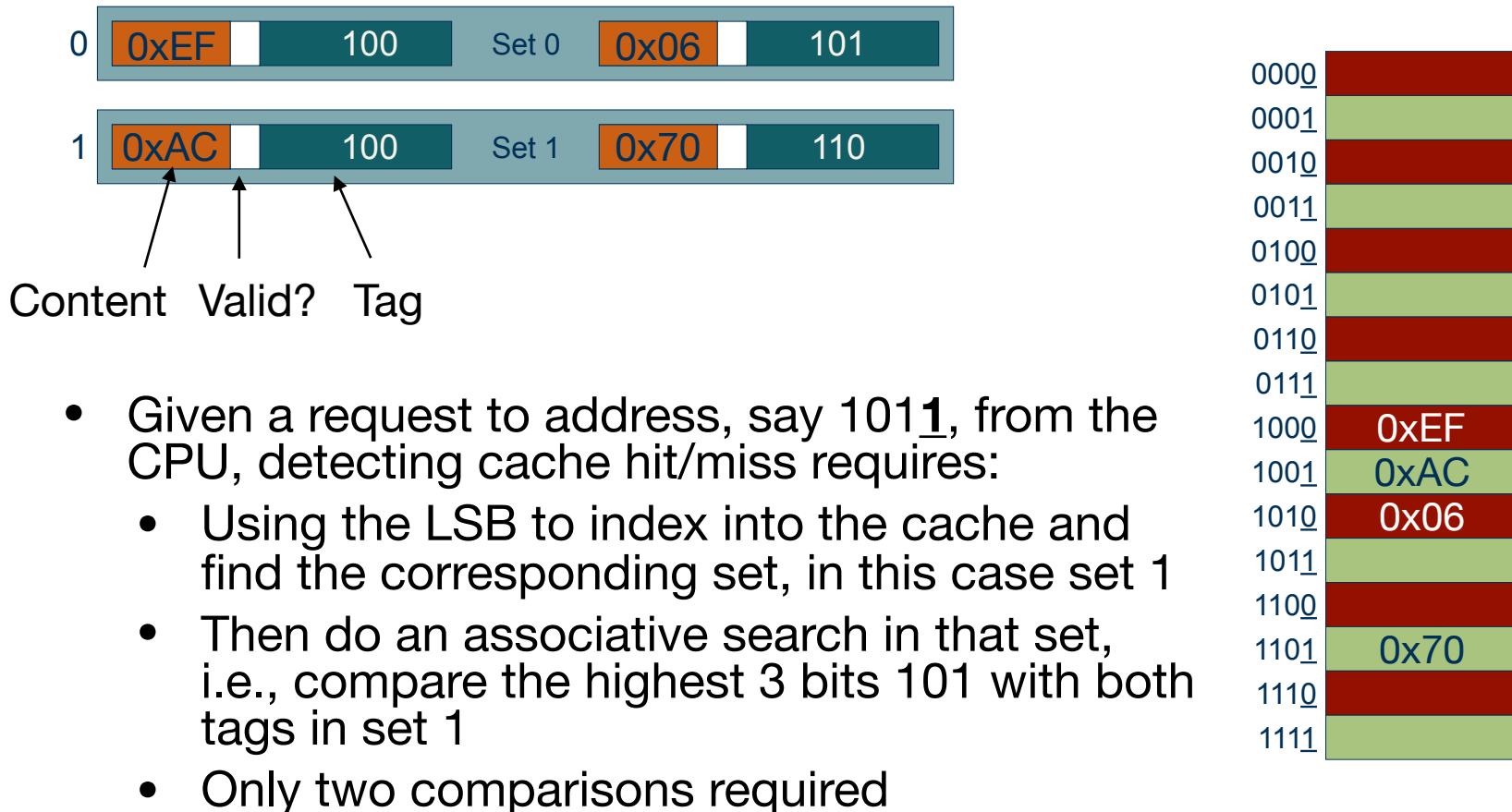
- Given a request to address, say **1011**, from the CPU, detecting cache hit/miss requires:
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# 2-Way Associative Cache

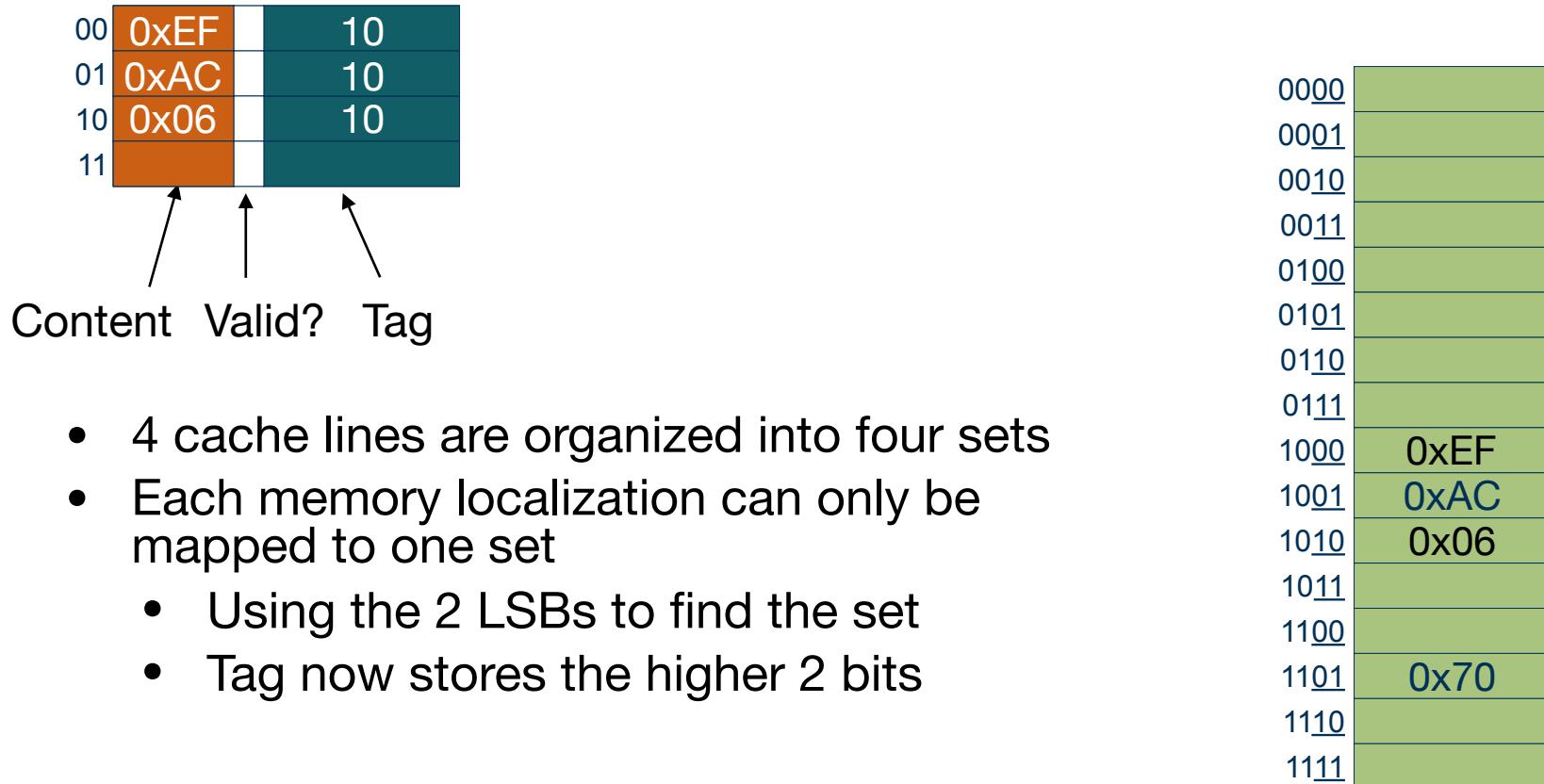


- Given a request to address, say **1011**, from the CPU, detecting cache hit/miss requires:
  - Using the LSB to index into the cache and find the corresponding set, in this case set 1
  - Then do an associative search in that set, i.e., compare the highest 3 bits 101 with both tags in set 1

# 2-Way Associative Cache



# Direct-Mapped (1-way Associative) Cache



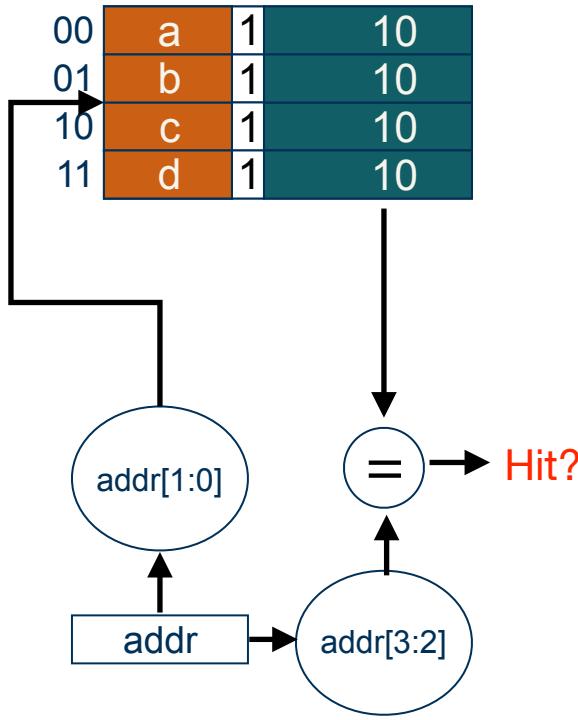
# **Associative verses Direct Mapped Trade-offs**

# Associative verses Direct Mapped Trade-offs

- Direct-Mapped cache
  - Generally lower hit rate
  - Simpler, Faster

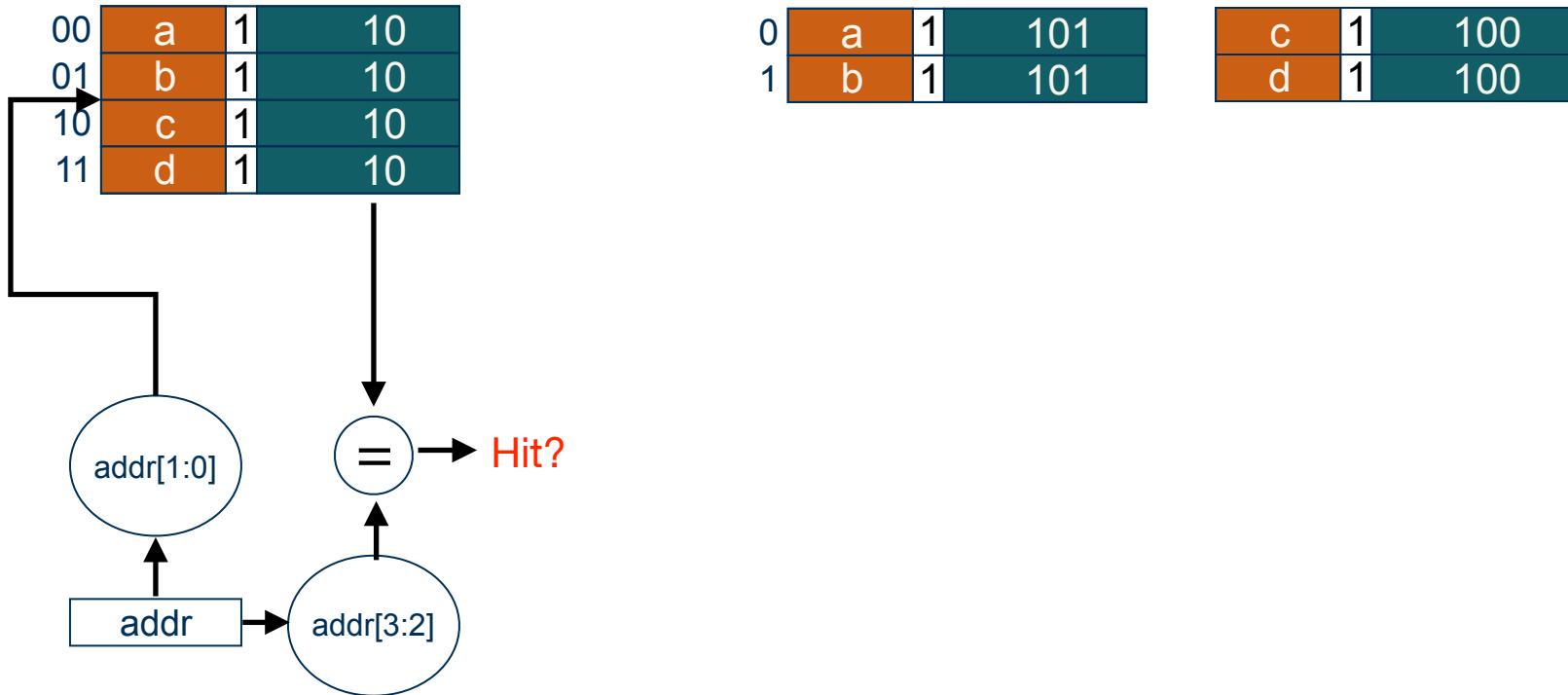
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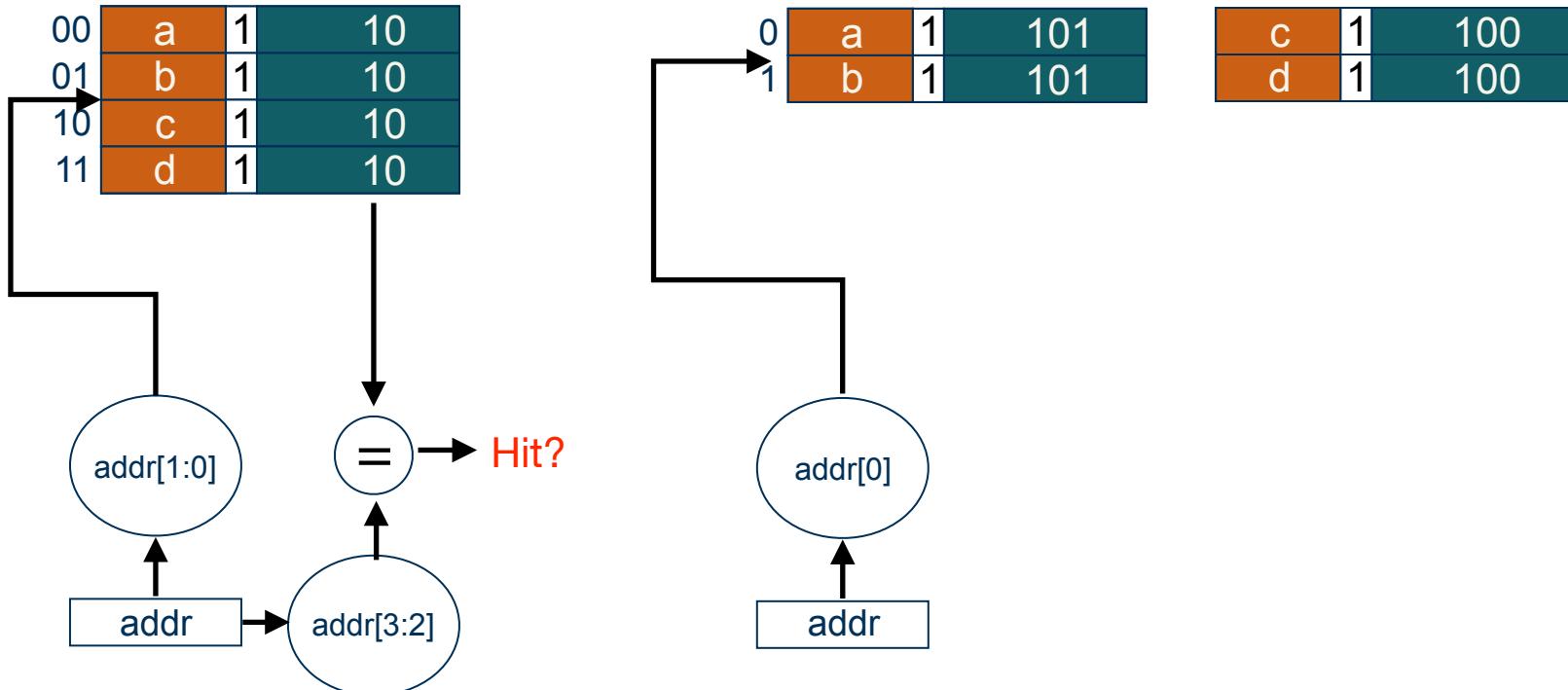
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- Associative cache
  - Generally higher hit rate. Better utilization of cache resources
  - Slower and higher power consumption. Why?



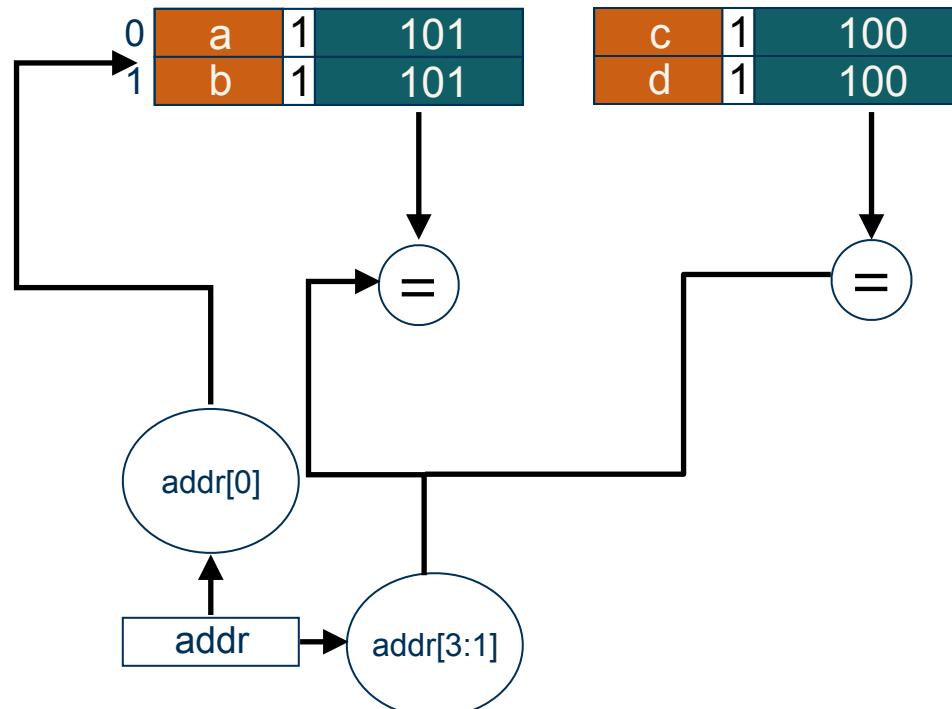
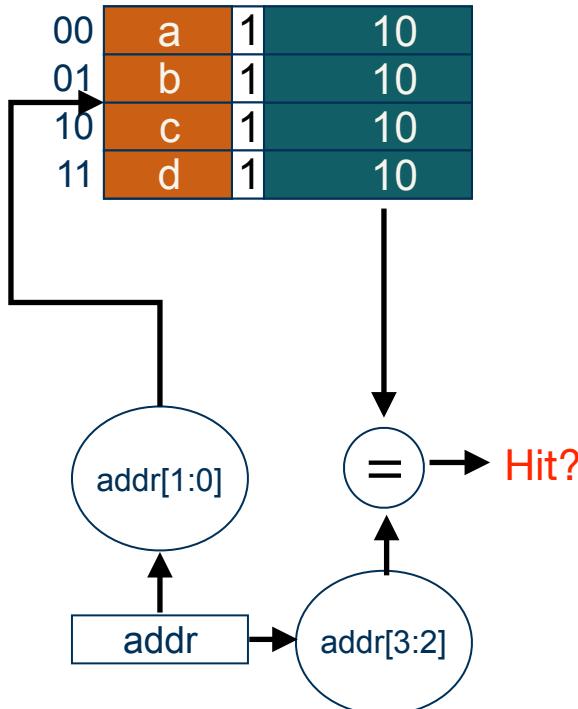
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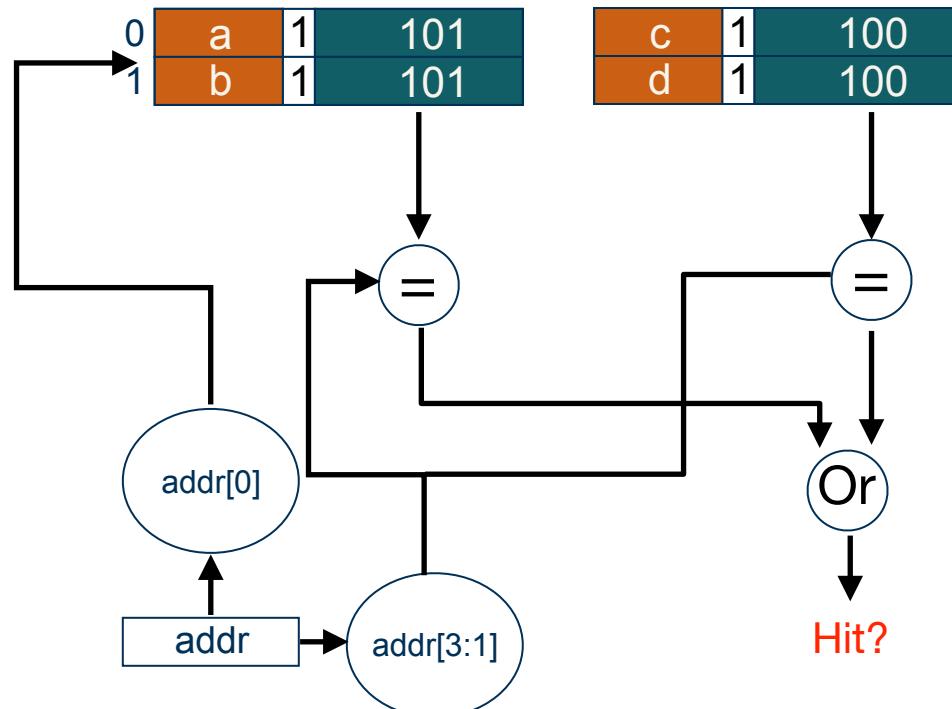
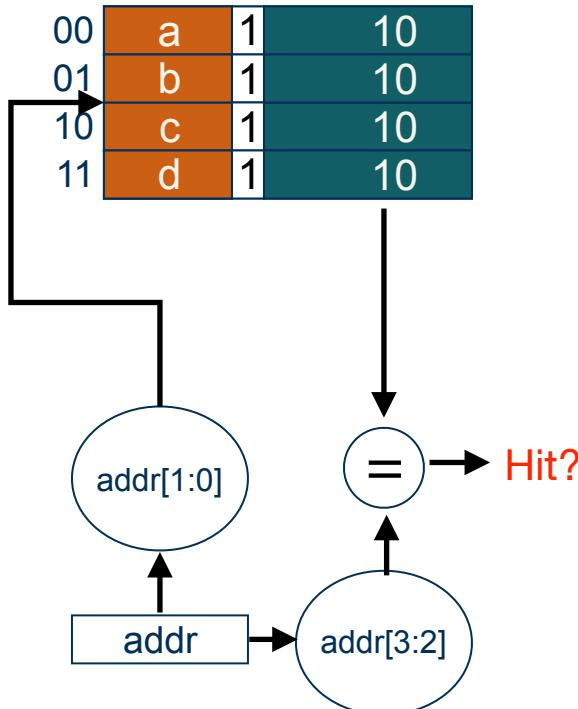
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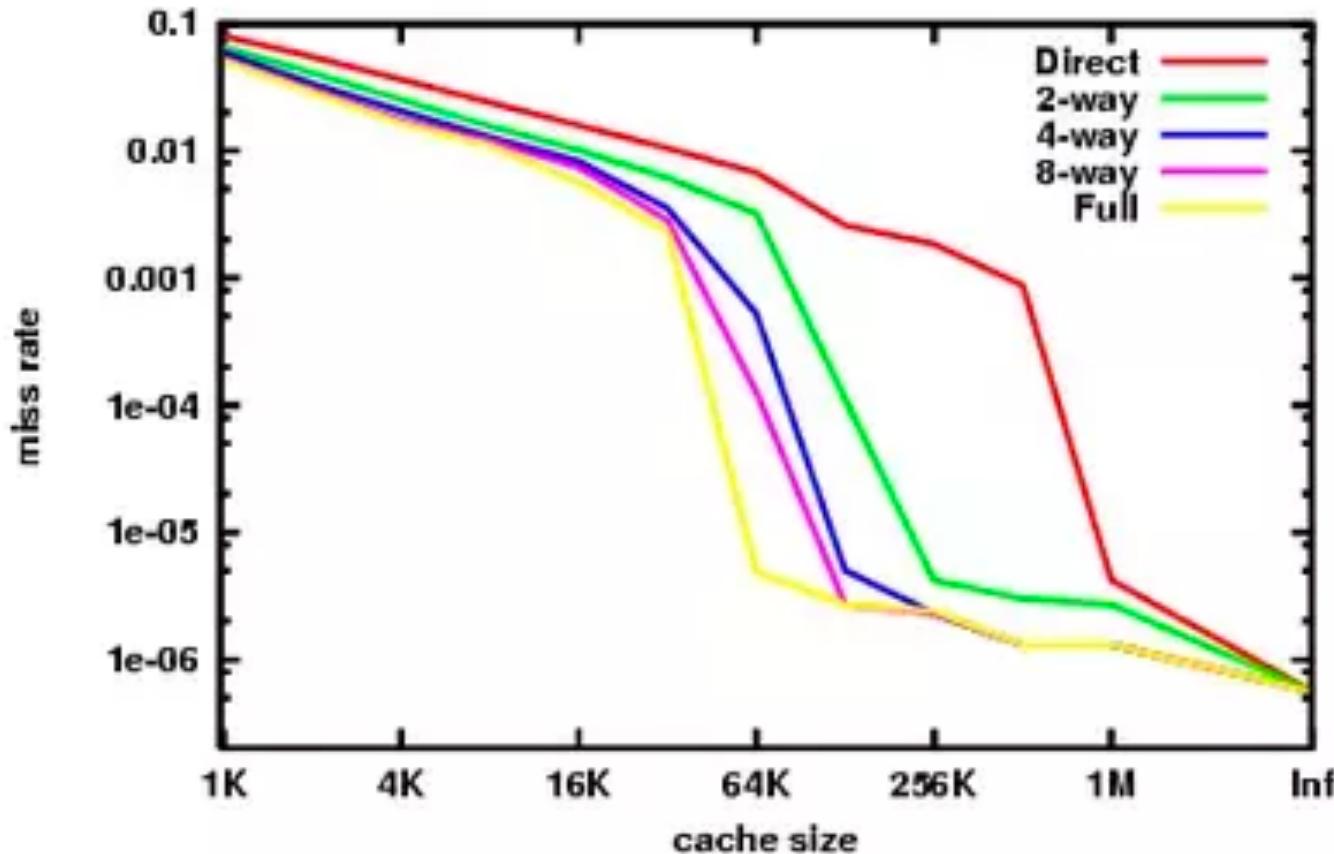


# Associative verses Direct Mapped Trade-offs

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# Associative verses Direct Mapped Trade-offs



Miss rate versus cache size on the Integer portion of SPEC CPU2000

# Cache Organization

- Finding a name in a roster
- If the roster is completely unorganized
  - Need to compare the name with all the names in the roster
  - Same as a fully-associative cache
- If the roster is ordered by last name, and within the same last name different first names are unordered
  - First find the last name group
  - Then compare the first name with all the first names in the same group
  - Same as a set-associative cache

# Cache Access Summary (So far...)

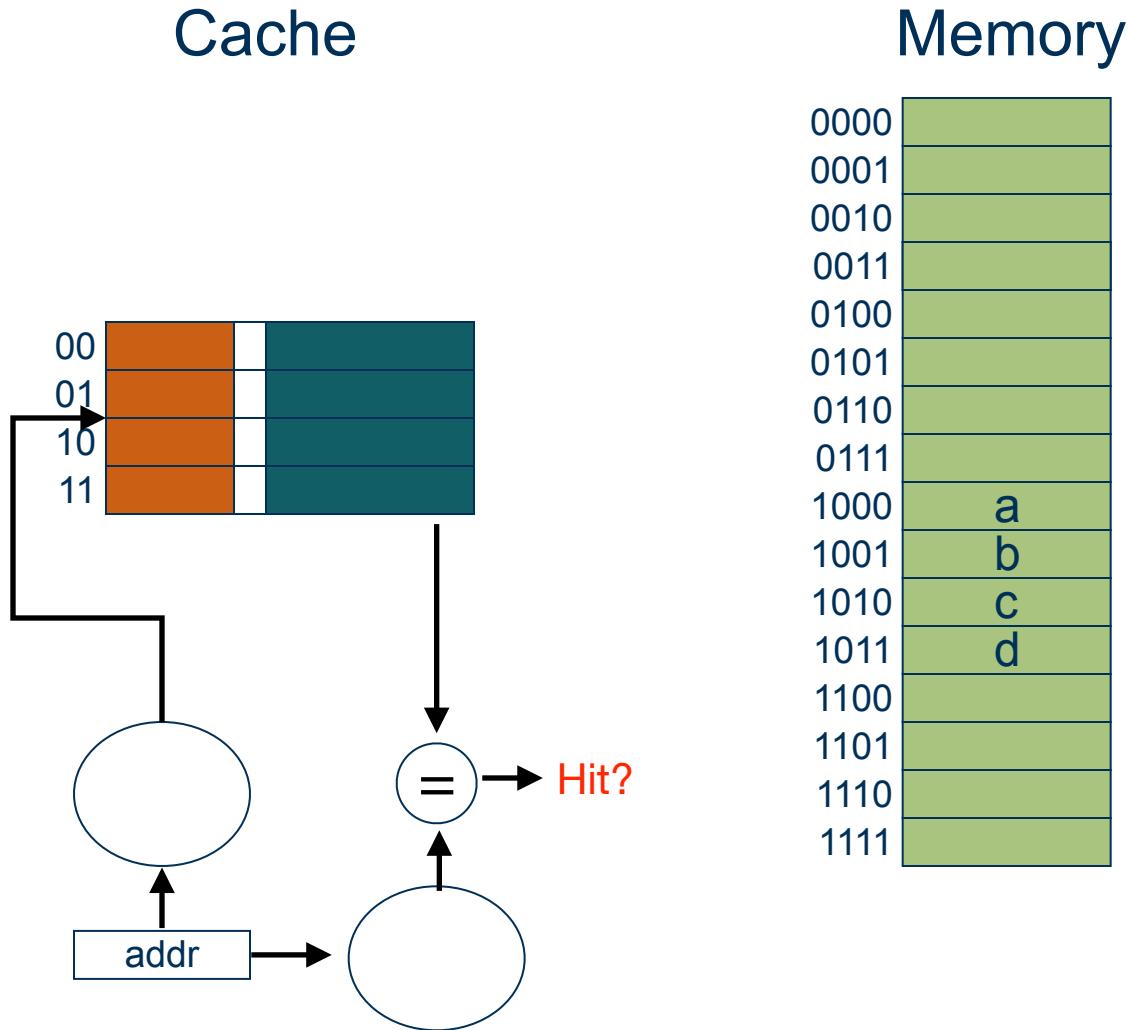
- Assuming  $b$  bits in a memory address
- The  $b$  bits are split into two halves:
  - Lower  $s$  bits used as index to find a set. Total sets  $S = 2^s$
  - The higher  $(b - s)$  bits are used for the tag
- Associativity  $n$  (i.e., the number of ways in a cache set) is **independent** of the the split between index and tag



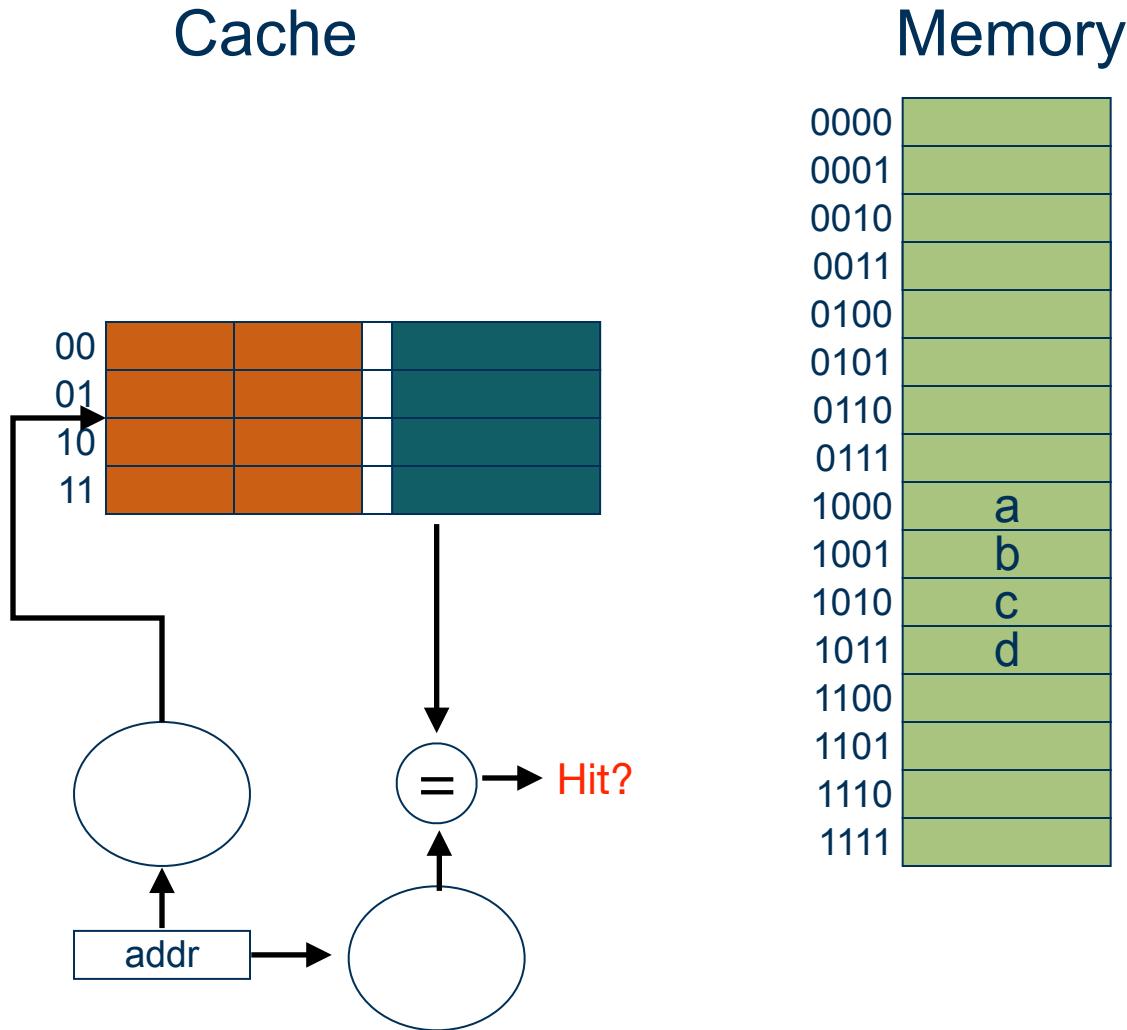
# Locality again

- So far: temporal locality
- What about spatial?
- Idea: Each cache location (cache line) store multiple bytes

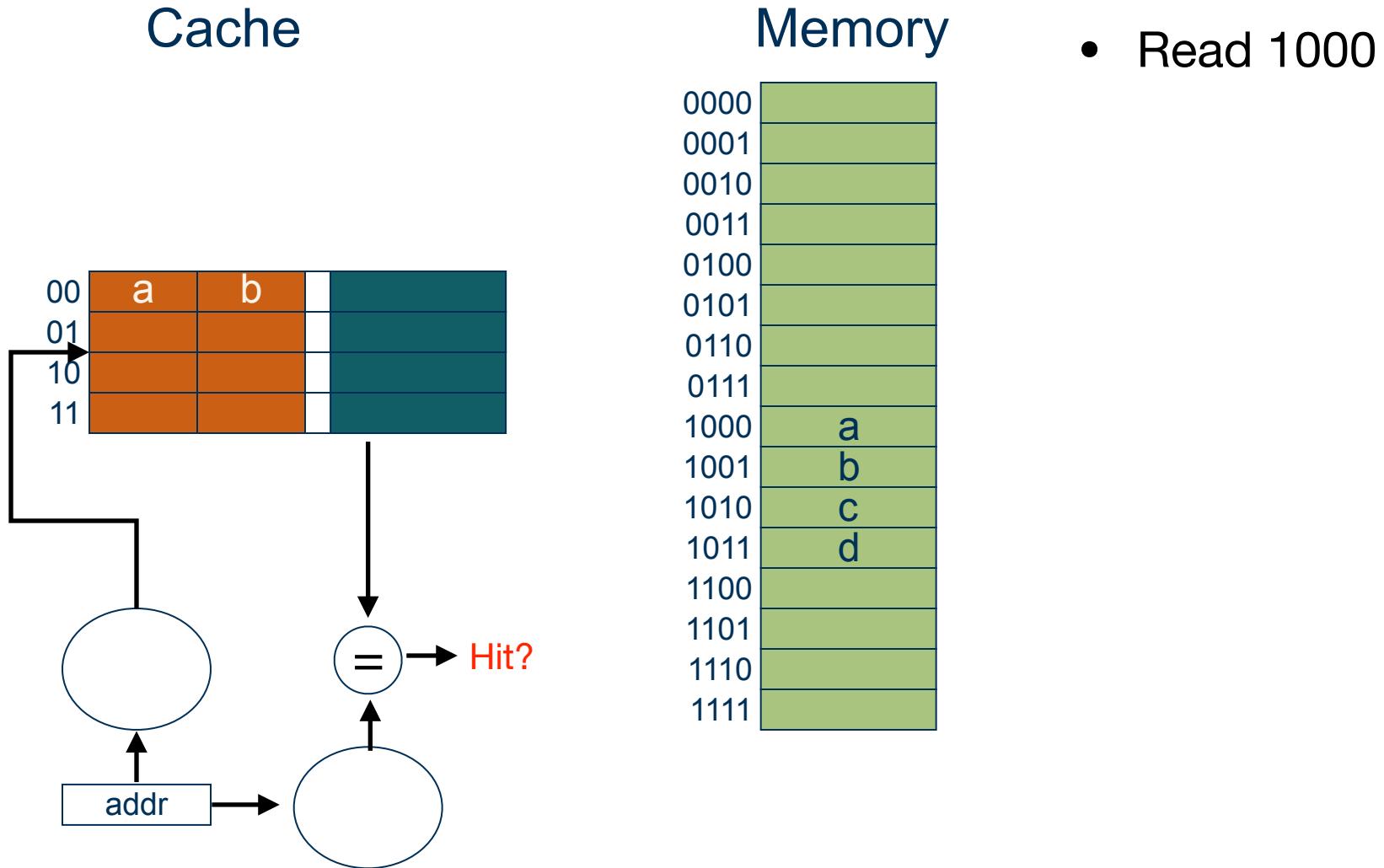
# Cache-Line Size of 2



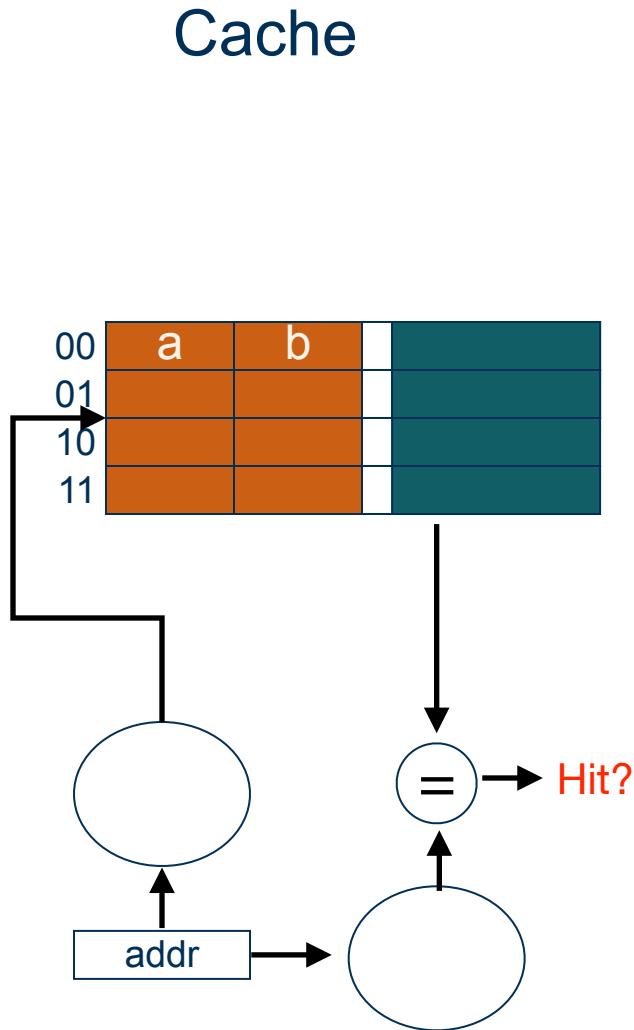
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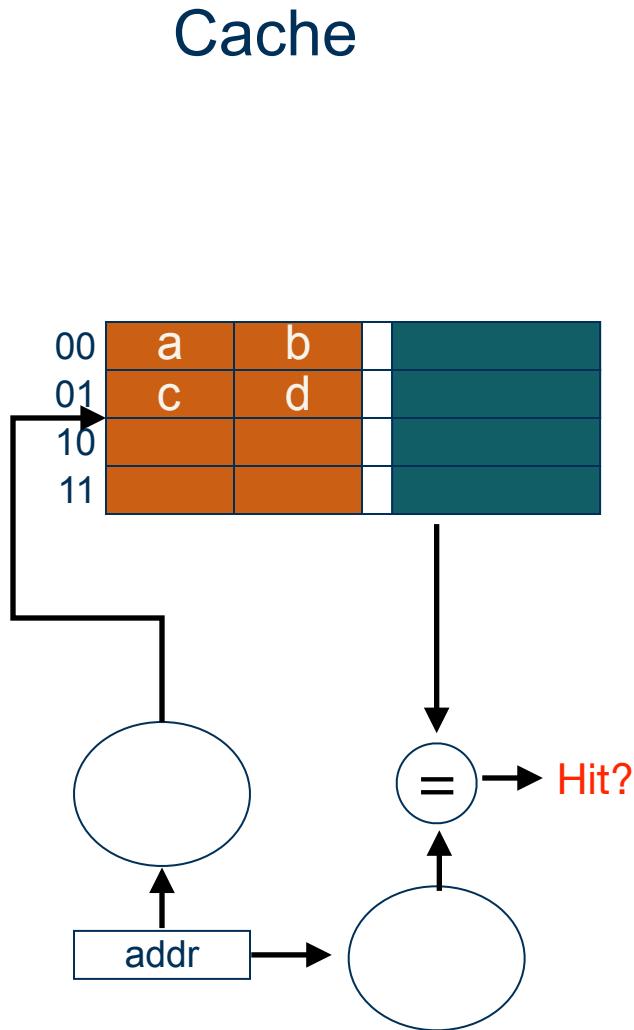


# Cache-Line Size of 2



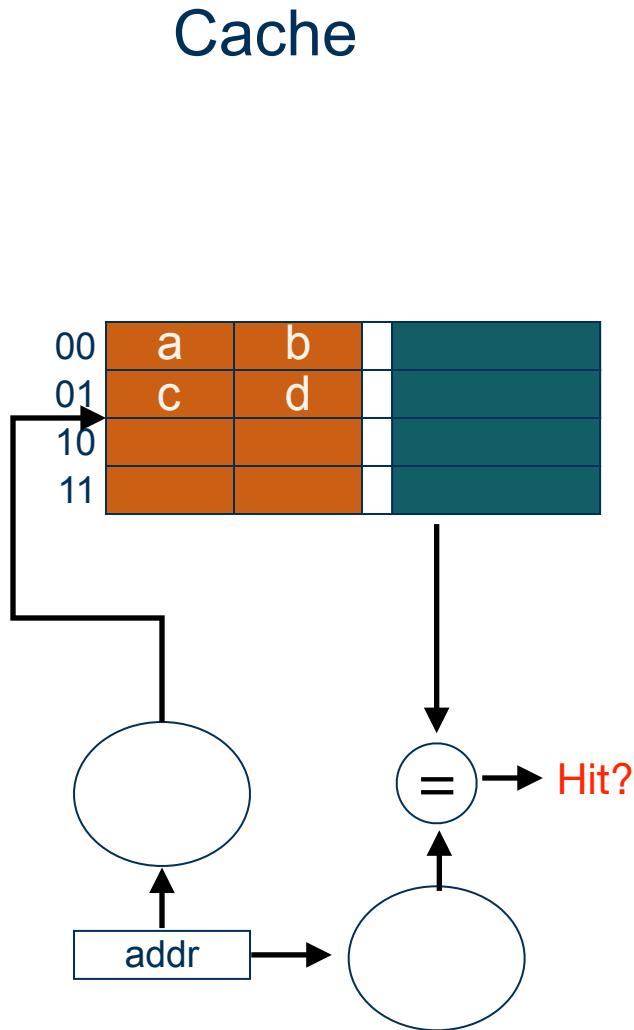
- Read 1000
- Read 1001 (**Hit!**)

# Cache-Line Size of 2



- Read 1000
- Read 1001 (**Hit!**)
- Read 1010

# Cache-Line Size of 2



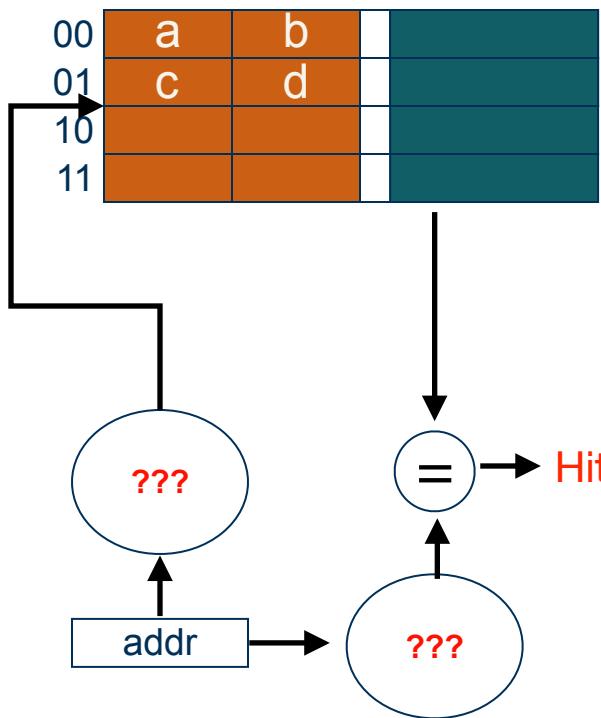
Memory

0000	
0001	
0010	
0011	
0100	
0101	
0110	
0111	
1000	a
1001	b
1010	c
1011	d
1100	
1101	
1110	
1111	

- Read 1000
- Read 1001 (**Hit!**)
- Read 1010
- Read 1011 (**Hit!**)

# Cache-Line Size of 2

Cache

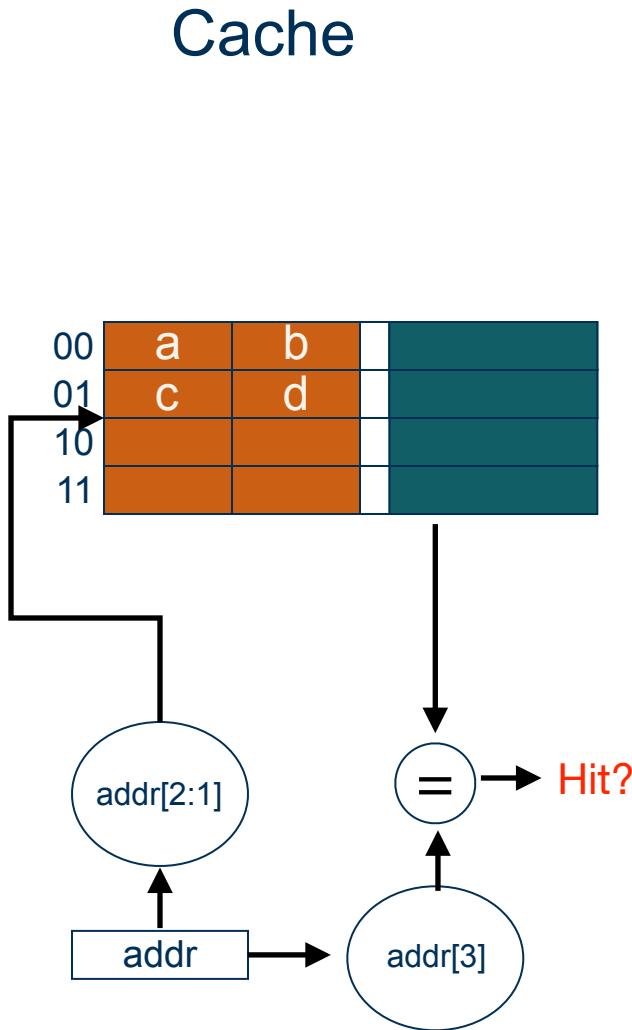


Memory

0000	
0001	
0010	
0011	
0100	
0101	
0110	
0111	
1000	a
1001	b
1010	c
1011	d
1100	
1101	
1110	
1111	

- Read 1000
- Read 1001 (**Hit!**)
- Read 1010
- Read 1011 (**Hit!**)
- **How to access the cache now?**

# Cache-Line Size of 2

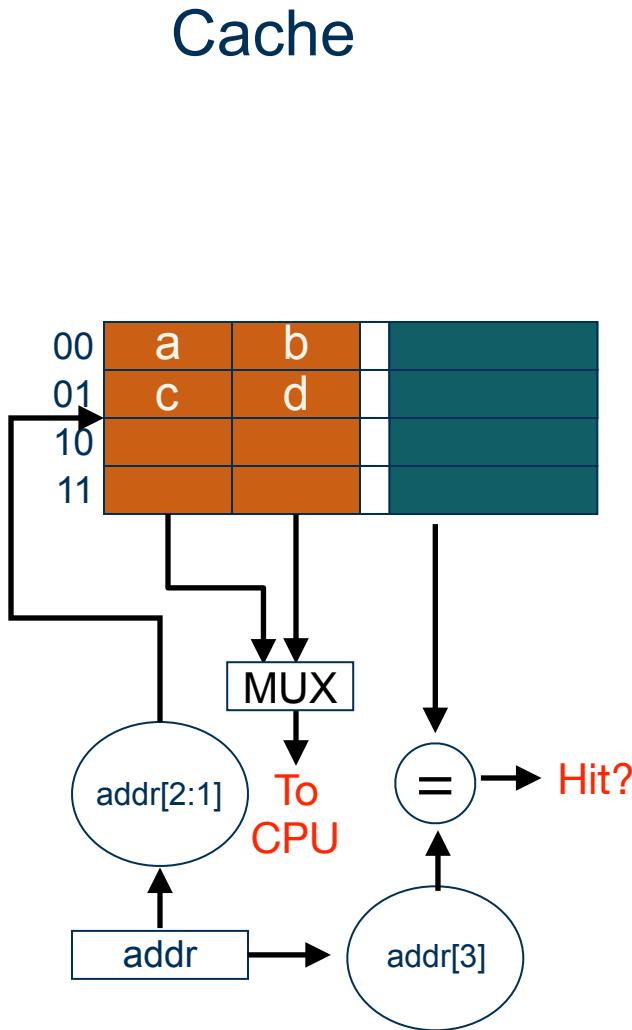


Memory

0000	
0001	
0010	
0011	
0100	
0101	
0110	
0111	
1000	a
1001	b
1010	c
1011	d
1100	
1101	
1110	
1111	

- Read 1000
- Read 1001 (**Hit!**)
- Read 1010
- Read 1011 (**Hit!**)

# Cache-Line Size of 2



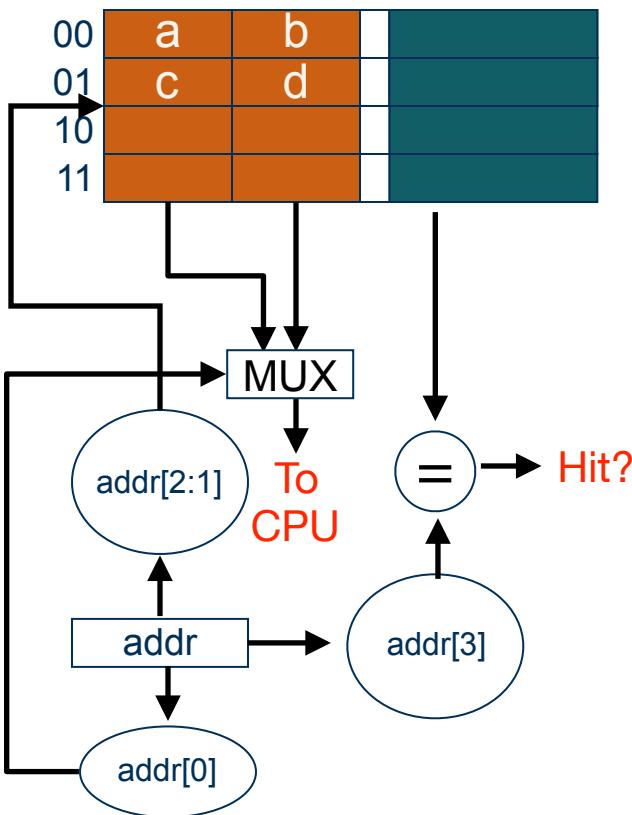
Memory

0000	
0001	
0010	
0011	
0100	
0101	
0110	
0111	
1000	a
1001	b
1010	c
1011	d
1100	
1101	
1110	
1111	

- Read 1000
- Read 1001 (Hit!)
- Read 1010
- Read 1011 (Hit!)

# Cache-Line Size of 2

Cache



Memory

0000	
0001	
0010	
0011	
0100	
0101	
0110	
0111	
1000	a
1001	b
1010	c
1011	d
1100	
1101	
1110	
1111	

- Read 1000
- Read 1001 (**Hit!**)
- Read 1010
- Read 1011 (**Hit!**)

# Cache Access Summary

- Assuming  $b$  bits in a memory address
- The  $b$  bits are split into three fields:
  - Lower  $l$  bits are used for byte offset within a cache line. Cache line size  $L = 2^l$
  - Next  $s$  bits used as index to find a set. Total sets  $S = 2^s$
  - The higher  $(b - l - s)$  bits are used for the tag
- Associativity  $n$  is independent of the the split between index and tag



# Handling Reads

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- Read miss: Put into cache

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  - Any reason not to put into cache?

# Handling Reads

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  - Any reason not to put into cache?
  - What to replace? Depends on the replacement policy. More on this later.

# Handling Reads

- Read miss: Put into cache
  - Any reason not to put into cache?
  - What to replace? Depends on the replacement policy. More on this later.
- Read hit: Nothing special. Enjoy the hit!

# Handling Writes (Hit)

- Intricacy: data value is modified!
- Implication: value in cache will be different from that in memory!
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  - - Requires transfer of the whole cache line (although only one byte might have been modified)

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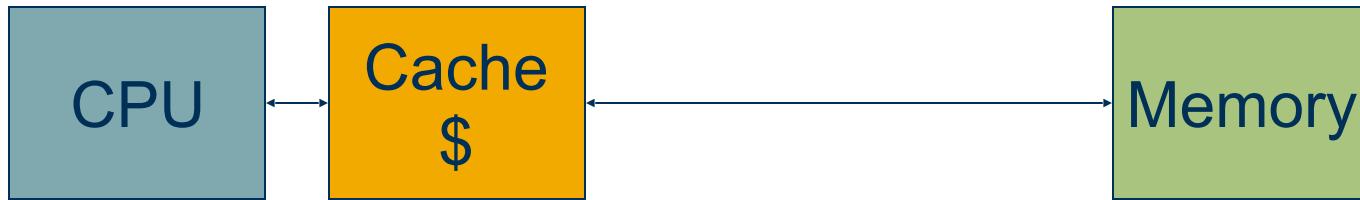
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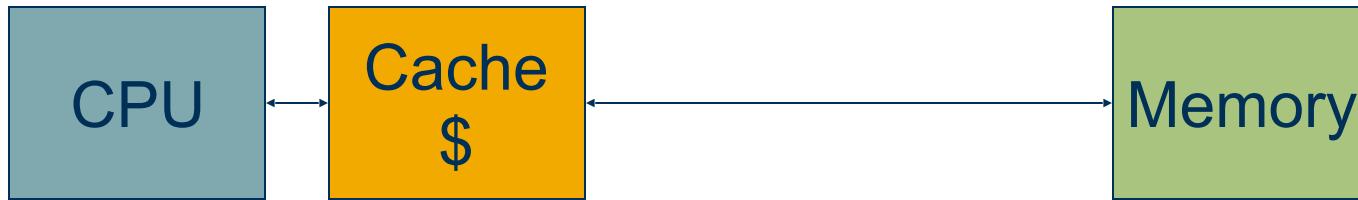
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Where do we place the unified cache for fast access?
- First level caches are almost always split
  - Mainly for the last reason above
- Second and higher levels are almost always unified

# General Rule: Bigger == Slower



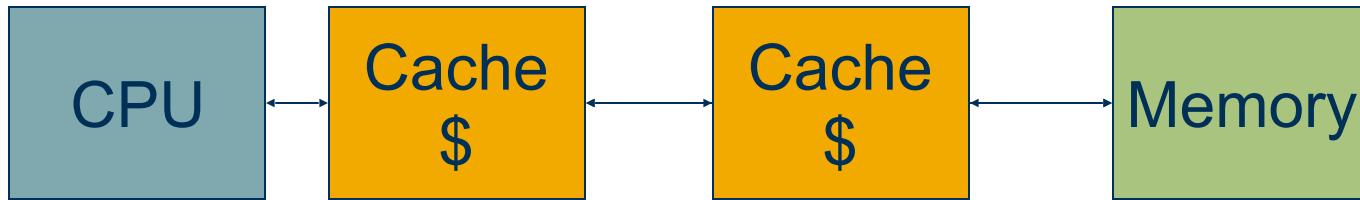
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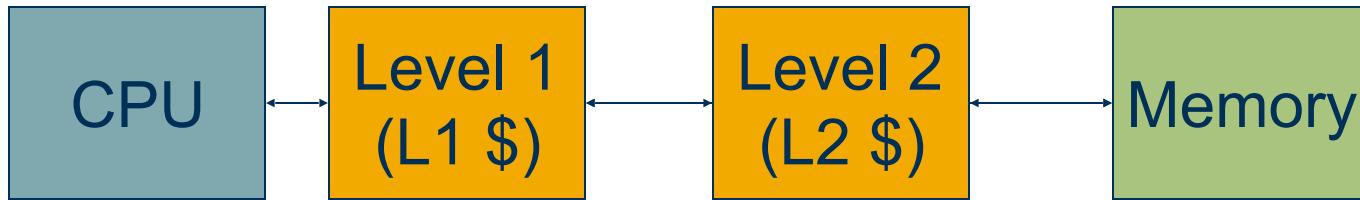
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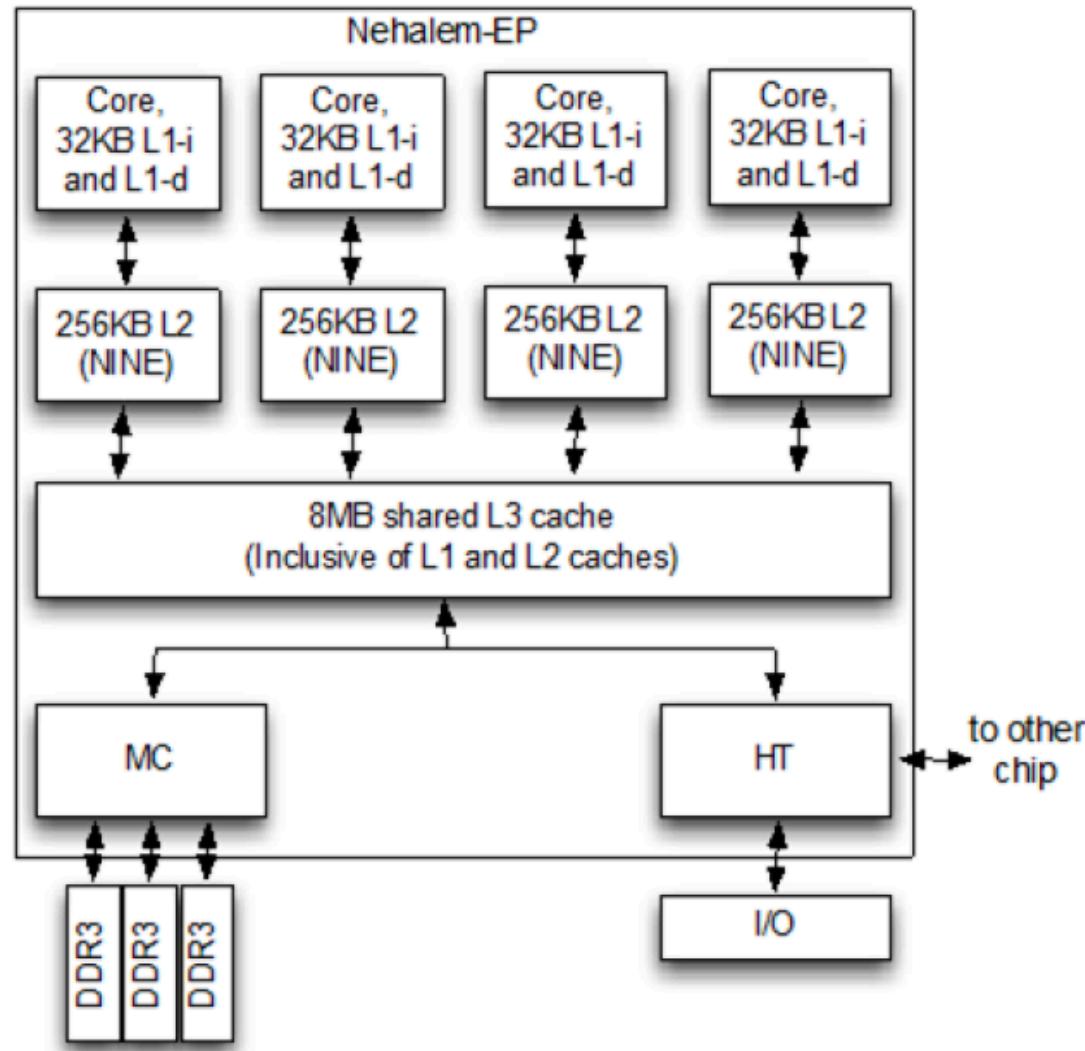
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# A Real Intel Processor



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    - Approximation: Least recently used (LRU)

# Implementing LRU

- Idea: Evict the least recently accessed block
- Challenge: Need to keep track of access ordering of blocks
- Question: 2-way set associative cache:
  - What do you need to implement LRU perfectly? One bit?

Cache Lines



LRU index (1-bit)



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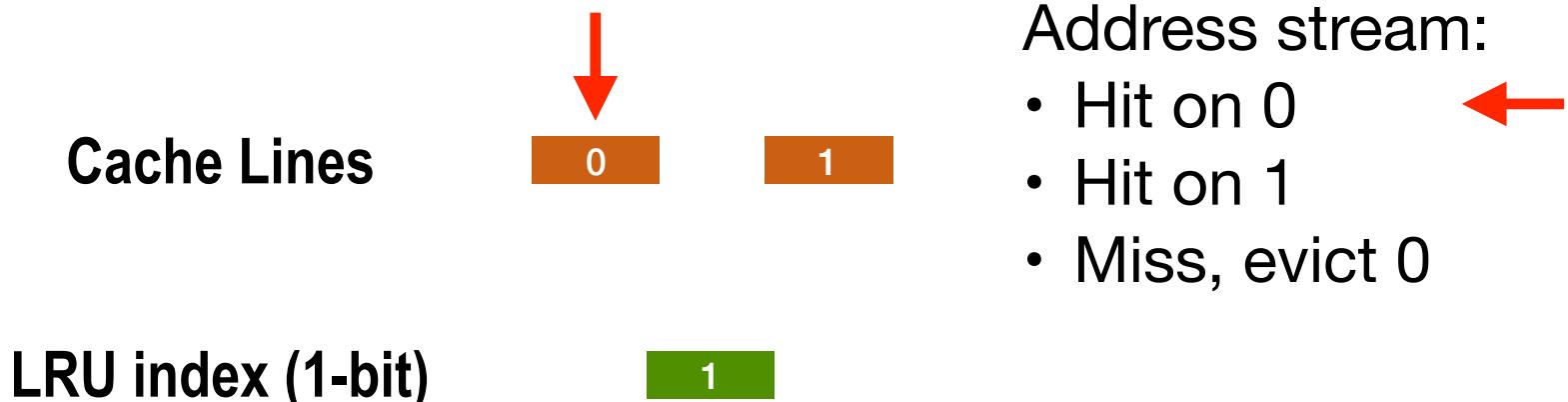


Address stream:

- Hit on 0
- Hit on 1
- Miss, evict 0

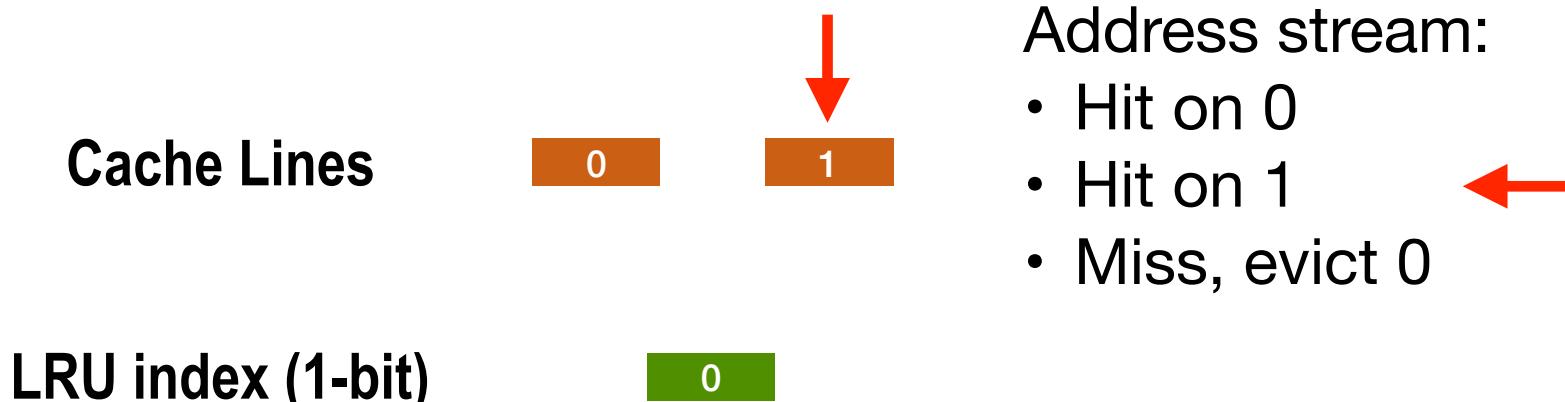
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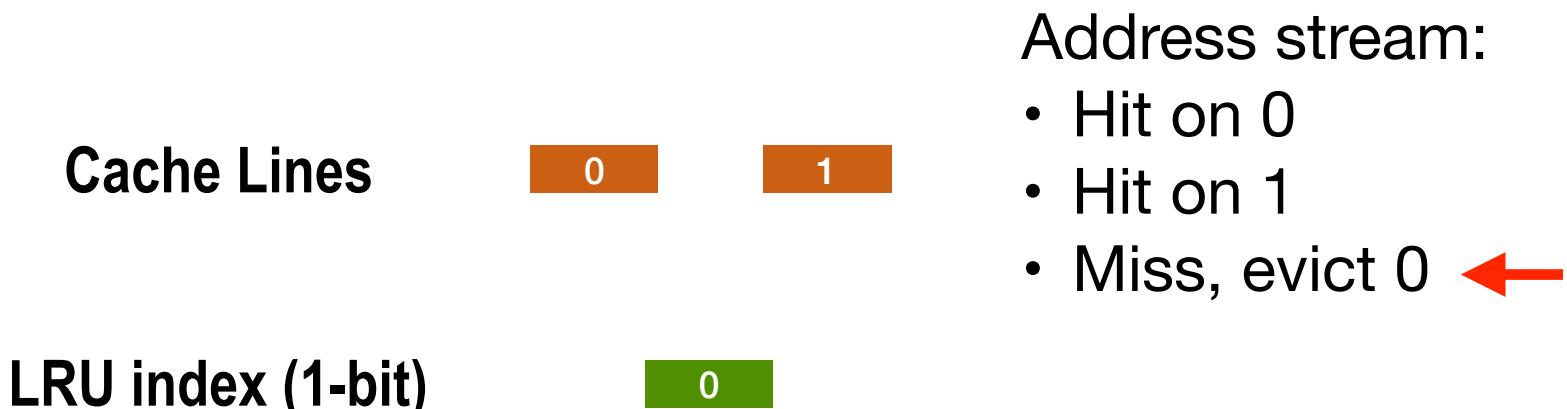
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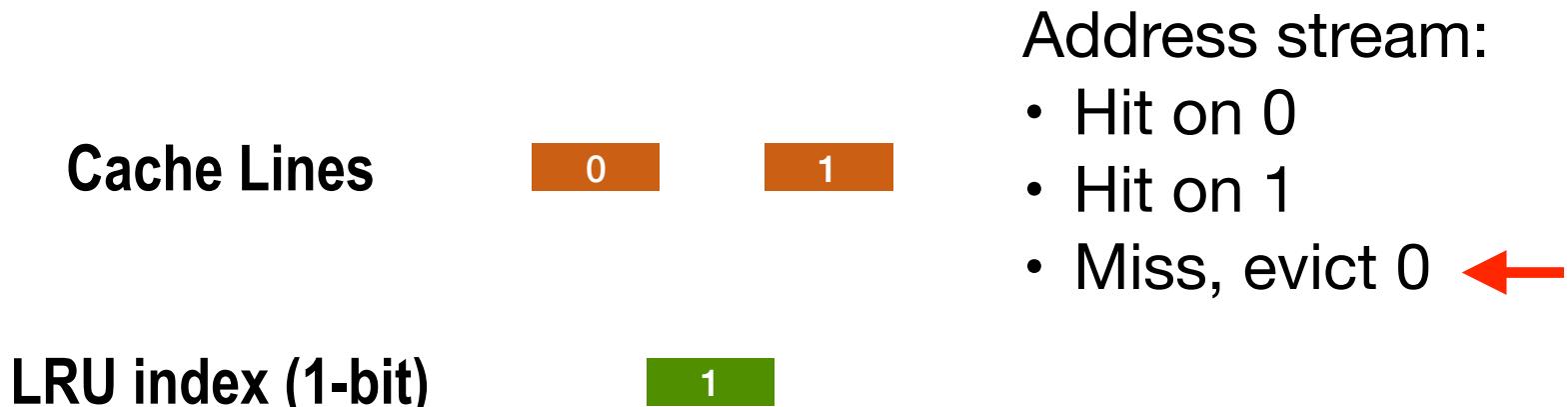
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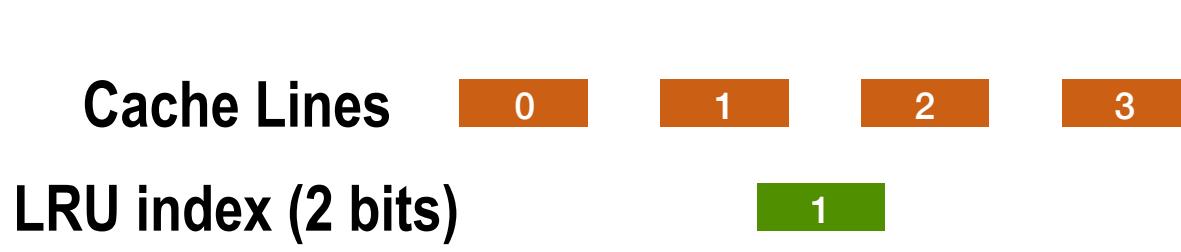
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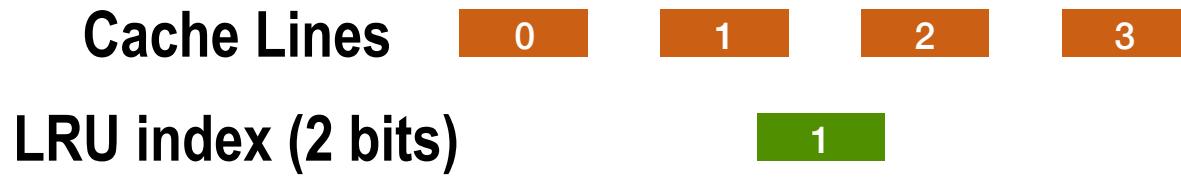


Address stream:

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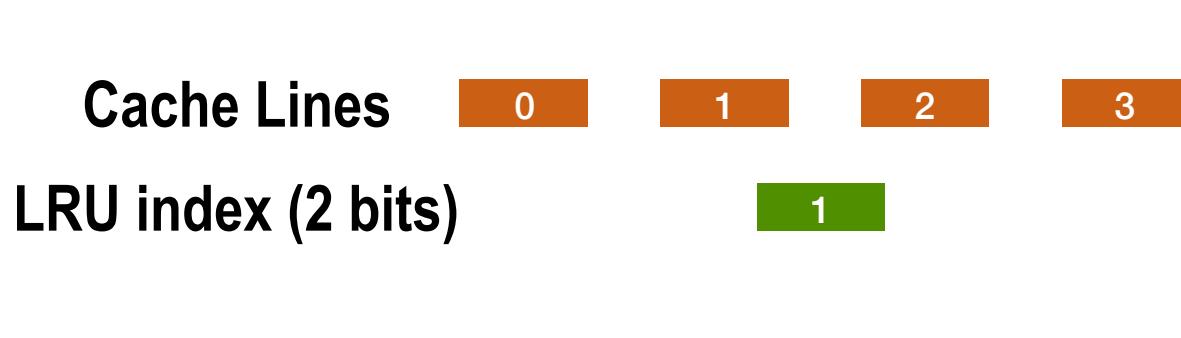
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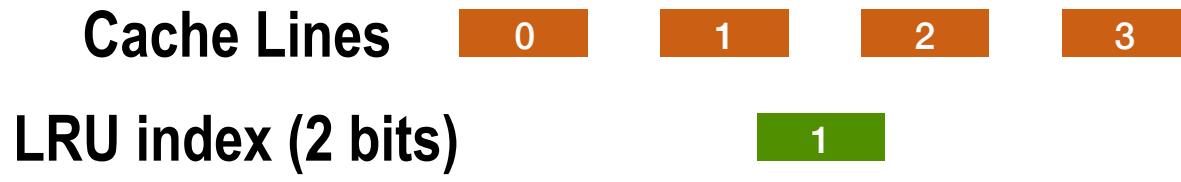
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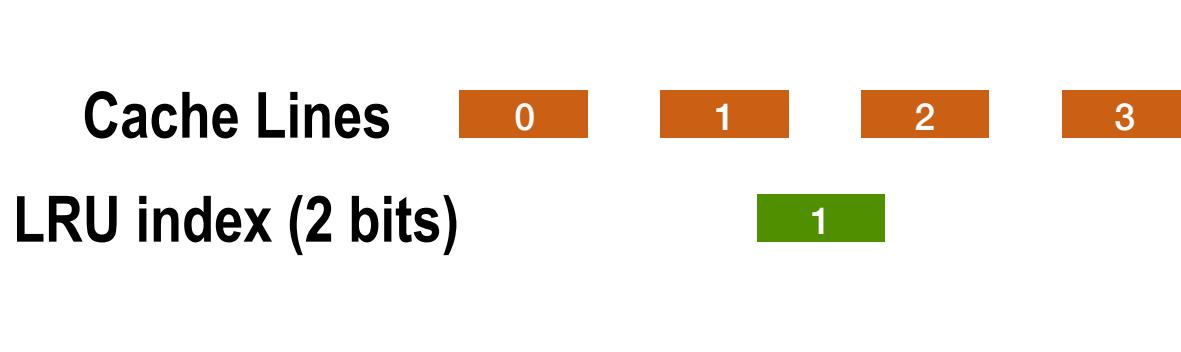
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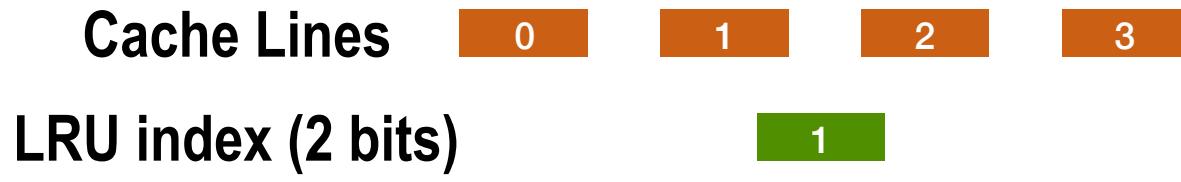
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  - “Pseudo-LRU” is usually used in real processors.

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