

History of Information

Geometric Science of Information



Georg F. B. Riemann
(1826–1866)
metric tensor (1854)
 $g = g_{ij} d\theta_i \otimes d\theta_j$
Riemannian manifold (M, g)



$ds^2 = g_{ij} dx^i dx^j$



Élie Joseph Cartan
(1869–1951)
affine connections
differential forms ω



Blaise Pascal
(1623–1662)
Aleae Geometria
Probability
Thermodynamics (pressue Pa.)
Computer (Pascaline)



Rabindra Nath Sen
(1896–1974)
dual parallel transports
(ca 1945–1950)



Sir Ronald A. Fisher
(1890–1962)
Mathematical statistics
Fisher information, MLE
 $I(\theta) = E_{p_\theta} [(\nabla_\theta \log p_\theta)(\nabla_\theta \log p_\theta)^T]$



Sir Harold Jeffreys
(1891–1989)
Jeffreys prior $\propto \sqrt{|g|}$
J-divergence



Alexander P. Norden
(1904–1993)
conjugate connections wrt g
Affinely connected spaces



Harold Hotelling
(1895–1973)
Econometrician
Fisher metric
(1930)



Maurice R. Fréchet
(1878–1973)
Metric spaces
Fréchet barycenter
Fréchet CR bound
Legendre-Clairaut structure



Wilhelm J. E. Blaschke
(1885–1962)
Affine differential geometry



Claude E. Shannon
(1916–2001)
Information theory
Entropy:
 $h(p) = - \int p \log p d\mu$




Imre Csiszár
(1938–)
information projections
f-divergences
 $I_f[p : q] = \int p f(\frac{p}{q}) d\mu$



C. R. Rao
(1920–)
Fisher-Rao distance
Cramér-Rao lower bound
(1945)



Solomon Kullback
(1907–1994)
KL divergence
 $D_{KL}[p : q] = \int p \log \frac{p}{q} d\mu$



Richard A. Leibler
(1914–2003)
KL divergence
 $D_{KL}[p : q] = \int p \log \frac{p}{q} d\mu$



Ernest B. Vinberg
(1937–2020)
characteristic functions
on homogeneous cones



Harald Cramér
(1893–1985)



Nikolai N. Chentsov
(1930–1992)
statistical invariance
geometrostatistics
Gen. Pythagoras theorem



$D(P : Q) + D(Q : R) = D(P : R)$



Bradley Efron
(1938–)
statistical curvature
E-connection
Lev M. Bregman
(1941–)
Bregman divergence
Bregman projections



Ole E. Barndorff-Nielsen
(1935–)
Exponential families
observed information geometry



Jean-Louis Koszul
(1921–2018)
Hessian Geometry
Symmetric Homogeneous Bounded Domains
Koszul forms, Fisher metric extension for sharp convex cones
Lie Algebra Cohomology, Koszul Complex, Koszul duality, Koszul connection
homogeneous bounded domains



Philip Dawid
(1946–)
decision theory
proper scoring rules



Steffen Lauritzen
(1947–)
statistical manifold
graphical models



Shun-ichi Amari
(1936–)
Information geometry
dualistic structure (M, g, ∇, ∇^*) :
 $Zg(X, Y) = g(\nabla_Z X, Y) + g(X, \nabla_Z^* Y)$
dual $\pm\alpha$ -connections
 $(M, g_F, \nabla^{-\alpha}, \nabla^\alpha)$



Jean-Marie Souriau
(1922–2012)
Lie Groups Thermodynamics
Souriau 2-form, Moment map
Fisher metric extension on
Homogeneous Symplectic Manifolds
Lie Groups Statistics, Entropy as Casimir Function
Fisher Metric as calorific capacity

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<https://franknielsen.github.io/GSI/>

information theoretic lower bounds via fano's lemma

the wasserstein autoencoder paper

use of martingale inequalities to prove some contextual bandit stuff

History of statistics

Countrarywise, there is a yuuge branch of Phil. of Statistics:
[from Memory]
De Finetti
Jeffreys
Levi
Kyburg
Good
Nagel
Hacking
Salmon
Hintikka
Suppes
Smolburg
von Wright [Inductive Logic],
+ Reichenbach, Popper, Carnap, Von Mises (R.),
Keynes, Fine, Peirce,
...even Laplace!

