## **History of Information**



## Geometric Science of Information



Georg F. B. Riemann (1826 - 1866)metric tensor (1854)  $g = g_{ij}d\theta_i \otimes d\theta_j$ Riemannian manifold (M, g) dx

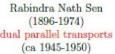


Élie Joseph Cartan (1869-1951)affine connections differential forms  $\omega$ 



Blaise Pascal (1623-1662)eae Geometria Probability

Thermodynamics (pressue Pa.) Computer (Pascaline)





Sir Ronald A. Fisher (1890-1962)Mathematical statistics Fisher information, MLE  $I(\theta) = E_{p\theta} \left[ (\nabla_{\theta} \log p_{\theta}) (\nabla_{\theta} \log p_{\theta})^{T} \right]$ 



Sir Harold Jeffreys (1891-1989)Jeffreys prior  $\propto \sqrt{|g|}$ J-divergence



Alexander P. Norden (1904-1993)conjugate connections wrt g Affinely connected spaces



Harold Hotelling (1895-1973)Econometrician Fisher metric (1930)



Maurice R. Fréchet (1878-1973)Metric spaces Fréchet barycenter Fréchet CR bound Legendre-Clairaut structure



Wilhelm J. E. Blaschke (1885-1962)Affine differential geometry



laude E. Shannon (1916-2001)information theory Entropy:  $(p) = - \int p \log p d\mu$ 



Imre Csiszár (1938-)information projections f-divergences  $I_f[p:q] = \int pf(\frac{q}{p})d\mu$ 



C. R. Rao (1920-)Fisher-Rao distance Cramér-Rao lower bound (1945)





Solomon Kullback (1907-1994)Richard A. Leibler (1914-2003)KL divergence  $D_{KL}[p:q] = \int p \log \frac{p}{a} d\mu$ 



Ernest B. Vinberg (1937-2020)characteristic functions on homogeneous cones

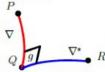


Harald Cramér (1893-1985)





Nikolai N. Chentsov (1930-1992)statistical invariance geometrostatistics Gen. Pythagoras theorem D(P : Q)



= D(P:R)



Bradley Efron (1938-)tatistical curvature E-connection Lev M. Bregman (1941-)Bregman divergence Bregman projections





Ole E. Barndorff-Nielsen (1935-)Exponential families observed information geometry



Jean-Louis Koszul (1921-2018)Hirohiko Shima Hessian Geometry

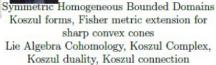








Steffen Lauritzen (1947-)tatistical manifold graphical models



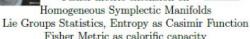
homogeneous bounded domains



Jean-Marie Souriau (1922-2012)



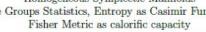
Lie Groups Thermodynamics Souriau 2-form, Moment map Fisher metric extension on







Shun-ichi Amari (1936-)Information geometry dualistic structure( $M, g, \nabla, \nabla^*$ ):  $Zg(X,Y) = g(\nabla_Z X, Y) + g(X, \nabla_Z^* Y)$ dual  $\pm \alpha$ -connections  $(M, g_F, \nabla^{-\alpha}, \nabla^{\alpha})$ 



information theoretic lower bounds via fano's lemma

the wasserstein autoencoder paper

use of martingale inequalities to prove some contextual bandit stuff

## History of statistics

Countrarywise, there is a yuuge branch of Phil. of

Statistics:

[from Memory]

De Finetti

Jeffreys

Levi

Kyburg

Good

Nagel

Hacking

Salmon

Hintikka

Suppes

Smolburg

von Wright [Inductive Logic],

+ Reichenbach, Popper, Carnap, Von Mises (R.),

Keynes, Fine, Peirce,

...even Laplace!

