Less likely to get half, more likely to get near half

"Near" in terms of percentages, not absolute differences.

https://www.johndcook.com/blog/2016/09/12/less-likely-to-get-half-more-likely-to-get-near-half/



Simply, the average converges to $\frac{1}{2}$, with a variance prop to $\frac{1}{n^2}$. But the exact probability of getting $\frac{1}{2}$ decreases, as the PDF of the binomial dist[n,p],p= $\frac{1}{2}$, n even decreases with n.

In[e]:= DiscretePlot[2⁻ⁿ Binomial[n, 1 / 2], {n, 2, 20, 2}, PlotRange \rightarrow All, PlotStyle \rightarrow Red]

