

Ex06

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- Given an ideal low-pass filter frequency response

$$H(\omega) = \begin{cases} 1, & |\omega| < \omega_c \\ 0, & |\omega| > \omega_c \end{cases} \quad (0-1)$$

1. Find its impulse response $h[n]$

Hint:

1. use inverse Fourier transform definition to find $h[n]$
2. sinc function is defined in MATLAB as $\text{sinc}(t) = \begin{cases} \frac{\text{sinc}(\pi t)}{\pi t}, & t \neq 0 \\ 1, & t = 0 \end{cases}$

Answer:

$$h[n] = \frac{1}{2\pi} \int_{-\infty}^{\infty} H(\omega) e^{j\omega n} d\omega \quad (0-2)$$

$$= \frac{1}{2\pi} \int_{-\omega_c}^{\omega_c} e^{j\omega n} d\omega \quad (0-3)$$

$$= \frac{1}{2\pi} \frac{1}{jn} (e^{j\omega_c n} - e^{-j\omega_c n}) \quad (0-4)$$

$$= \frac{1}{2\pi} \frac{1}{jn} 2j \sin(\omega_c n) \quad (0-5)$$

$$= \frac{1}{\pi n} \sin(\omega_c n) \quad (0-6)$$

$$= \frac{\omega_c}{\pi} \frac{\sin(\omega_c n)}{\omega_c n} \quad (0-7)$$

$$= \frac{\omega_c}{\pi} \text{sinc}(\omega_c n) \quad (0-8)$$