Goodness of Fit: R² vs. Adjusted R²

You can think of the difference between R² and adj. R² this way.

- The R² assumes that *every* independent variable in the model helps to explain variation in the DV. So, it tells you the percentage of explained variation as if *all* IVs in the model affect the DV (as if each IV passes the t-test.)
- The adj. R²
 - o tells you the percentage of variation explained by only those IVs that truly affect the DV (only those IVs that pass the t-test) **AND**
 - o penalizes you for adding independent variable(s) that do not belong in the model
- So, you can expect that the value of the adj. R^2 will be \leq value of R^2 .

Notice what happens to R^2 and adj. R^2 as add an independent variable.

Model #1.

Dependent Variable: SALARY

Included observations: 20

| Variable | Coefficient | Std. Error | t-Statistic | Prob. |
|--------------------|-------------|------------|-------------|--------|
| С | 73.98441 | 4.010613 | 18.44716 | 0.0000 |
| EXPERIENCE (years) | 0.945455 | 0.470826 | 2.008077 | 0.0608 |
| GENDER (0, 1) | -12.2012 | 2.854127 | -4.274932 | 0.0005 |

 R-squared
 0.750652
 F-statistic
 25.5889

 Adjusted R-squared
 0.721317
 Prob(F-statistic)
 0.000007

Model #2. (Add SCORE to Model #1)

Dependent Variable: SALARY

Included observations: 20 Variable Coefficient Std. Error Prob. t-Statistic 62.90383 16.68642 3.769763 0.0017 EXPERIENCE (years) 0.950914 0.478424 1.987597 0.0642 GENDER (0, 1) 0.0044 -11.06503 3.340895 -3.311995 0.5033 SCORE (0 -100) 0.124637 0.18201 0.684779

 R-squared
 0.797752
 F-statistic
 16.68265

 Adjusted R-squared
 0.67233
 Prob(F-statistic)
 0.000035

SALARY = annual salary in \$1000 EXPERIENCE = years in industry

GENDER = 1 if female, 0 if male SCORE = score on programmer's antity

GENDER = 1 if female, 0 if male $\frac{1}{1}$ SCORE = score on programmer's aptitude $\frac{1}{1}$ test $\frac{1}{1}$ (0 – 100)