

Answer 1 →

$$\text{Given} = \sigma(z) = \frac{1}{1 + e^{-z}}$$

$$h_1 = \frac{1}{1 + e^{-w_1 x_1 - w_2 x_2}}$$

$$L(y, \hat{y}) = \| \hat{y} - y \|^2$$

$$(x_1, x_2, x_3, x_4) = (0.7, 1.2, 1.1, 1.2)$$

$$y = 0.5$$

$$\begin{aligned} S_1 &= x_1 w_1 + x_2 w_2 \\ &= (0.7)(-1.7) + (1.2)(0.1) \\ &= (-1.19) + (0.12) \\ &= -1.07 \end{aligned}$$

$$\boxed{S_1 = -1.07}$$

$$\begin{aligned} S_2 &= x_3 w_3 + x_4 w_4 \\ &= (1.1)(-0.6) + (2)(-1.8) \\ &= (-0.66) + (-3.6) \\ &\therefore \boxed{S_2 = -4.26} \end{aligned}$$

$$\text{Now } h_1 = \frac{-1}{1 + e^{-1.07}}$$

$$\boxed{h_1 = 0.255}$$

$$\begin{aligned} \text{Let calculate } S_3 &= h_1 w_5 + h_2 w_6 \\ &= (0.255)(-0.2) + (0.0139)(0.5) \\ &\boxed{S_3 = -0.0441} \end{aligned}$$

$$\hat{y} = \frac{1}{1 + e^{-S_3}} = \frac{1}{1 + e^{0.0441}} = [0.4889]$$

Back Propagation :

$$\frac{\partial E}{\partial w_1} = \frac{\partial E}{\partial \hat{y}} \cdot \frac{\partial \hat{y}}{\partial S_3} \cdot \frac{\partial S_3}{\partial h_1} \cdot \frac{\partial h_1}{\partial S_1} \cdot \frac{\partial S_1}{\partial w_1}; \quad \frac{\partial S_3}{\partial h_1} = w_5 \quad \left| \frac{\partial S_1}{\partial w_1} = x_1 \right.$$

$$\begin{aligned} \frac{\partial E}{\partial w_1} &= 2 ||\hat{y} - y|| \cdot \sigma'(S_3) \cdot w_5 \cdot \sigma'(S_1) \cdot x_1 \\ &= 2 ||0.4889 - 0.5|| \times \sigma'(-0.441) \cdot (-0.2) \\ &\quad \times \sigma'(-1.07) (0.7) \end{aligned}$$

$$\sigma(S_3) = \frac{1}{1 + e^{-(0.0441)}} = [0.4884]$$

$$\sigma(S_1) = \frac{1}{1 + e^{(-1.07)}} = [0.2554]$$

$$\begin{aligned} \frac{\partial E}{\partial w_1} &= [2 ||0.4889 - 0.5||] \times [(0.4884)(1 - 0.4884)] (0.7) \\ &\quad \times [(0.2554)(1 - 0.2554)] (0.1) \\ &= [2 (-0.107)] \times [(0.4889)(0.5116)] \end{aligned}$$

$$\boxed{\frac{\partial E}{\partial w_1} = -0.0014}$$