

CSC446 ASS3

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1. Named random.java

Output is:

```
E:\csc446>java random
X0 is 5.52
the null hypothesis is not rejected since X0<16.9

E:\csc446>java random
X0 is 13.42
the null hypothesis is not rejected since X0<16.9

E:\csc446>java random
X0 is 9.02
the null hypothesis is not rejected since X0<16.9

E:\csc446>java random
X0 is 11.959999999999999
the null hypothesis is not rejected since X0<16.9
```

2.

A. Kolmogorv method:

Named q2.java

```
E:\csc446>java q2
Random numbers in java:
0.048207132492562144
0.7349731062737864
0.823012118762264
0.3978771627093538
0.5732833506127893
0.8769321430099684
0.6558575862542575
0.08950358333761399
0.6178006265337461
0.3545755421217991

D= 0.17328335061278932
H0 is not rejected since d<D(0.05,10)=0.410
```

B. Chi-Square test:

Named q2b.java

Assume $\alpha=0.05$, the test case $n=10$;

```
E:\csc446>java q2b
After generating 1000 random numbers in java:
X0 is 14.179999999999998
the null hypothesis is not rejected since  $X_0 < X_{(0.05,9)} = 16.9$ 

E:\csc446>java q2b
After generating 1000 random numbers in java:
X0 is 15.280000000000001
the null hypothesis is not rejected since  $X_0 < X_{(0.05,9)} = 16.9$ 

E:\csc446>java q2b
After generating 1000 random numbers in java:
X0 is 4.159999999999999
the null hypothesis is not rejected since  $X_0 < X_{(0.05,9)} = 16.9$ 
```

3.

	A	B	C	D	E	F
1	i	0	1	2	3	4
2	X0	7	13	15	5	7
3	X1	8	8	8	8	8
4	X2	7	1	7	1	7
5	X3	8	8	8	8	8

Since $c=0$; Max period $= 16/4=4$;

So we conclude that if X_0 is odd and $a=3+8k$, then the maximum period is achieved, otherwise the period is less than maximum period.

4.

CDF:

$$F(x) = e^{-(2x)/2} \quad x < 0$$

$$= 1 - e^{-(2x)/2} \quad x > 0$$

Let $F(x)=R$, we get:

$$X = \ln(2R)/2 \quad 0 < R \leq 1/2$$

$$= -\ln(2-2R)/2 \quad 1/2 < R < 1$$

5. We get $i=1$; $m=3$; $N=20$; $M=5$;

Define $R(X,Y)=R_X * R_Y$;

$$P_{13} = 1/6(R(1,4)+R(4,7)+R(7,10)+R(10,13)+R(13,16)+R(16,19))-0.25$$

$$= 1.216918/6 - 0.25$$

=-0.04718

$\hat{O}p13=0.11785$

$Z0= P13/\hat{O}p13=-0.4$

Since $z0.025=1.96$ and $Z0$ is between $-z0.025$ and $z0.025$, the hypothesis is not rejected;

6.

Named q6.c

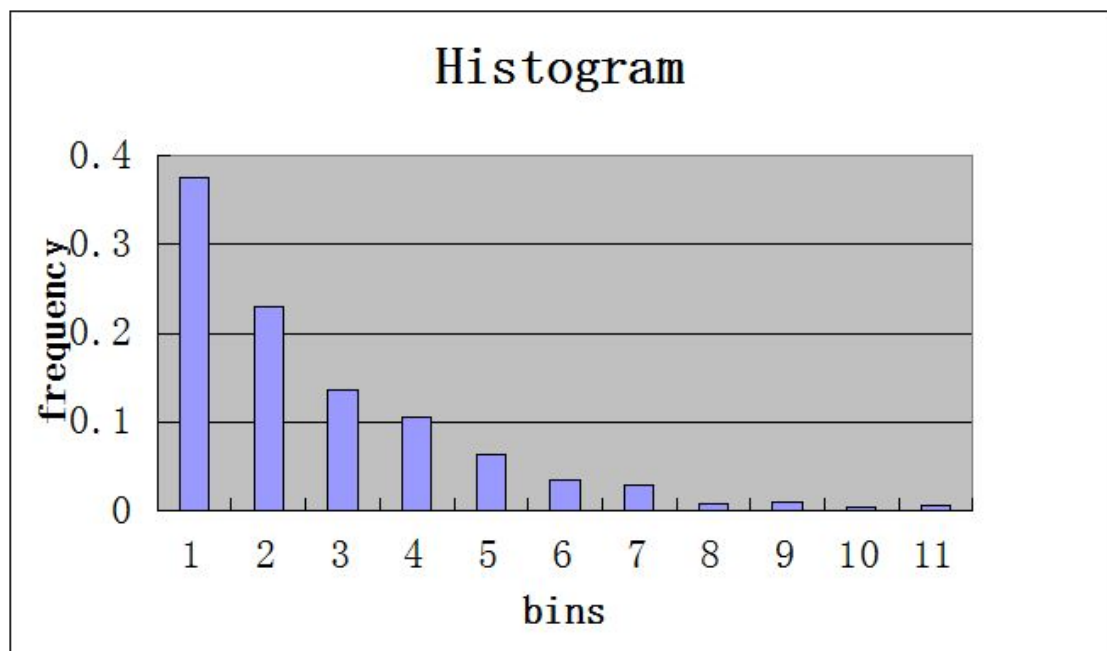
7.

Named q7.c (worked in some software):

```
int main()
{
    int n=3;
    int k=0;
    int i;
    int j;
    double x[1000], r[1000];
    int g[11];
    srand((unsigned)time(NULL));
    for (i=0; i<1000; i++) {
        r[i]=rand()/(float) RAND_MAX;
        //printf("%12f ", r[i]);
        x[i]=-log(1-r[i]);
        // printf("X[%d] is %12f. ", i, x[i]);
    }
    for (j=0; j<11; j++) {
        for (i=0; i<1000; i++) {
            if (j==10) {
                if (2*x[i]>=j) {
                    g[j]++;
                }
            }
            else {
                if (2*x[i]>=j && 2*x[i]<j+1) {
                    g[j]++;
                }
            }
        }
        printf("%d ", g[j]);
    }
    return 0;
}
```

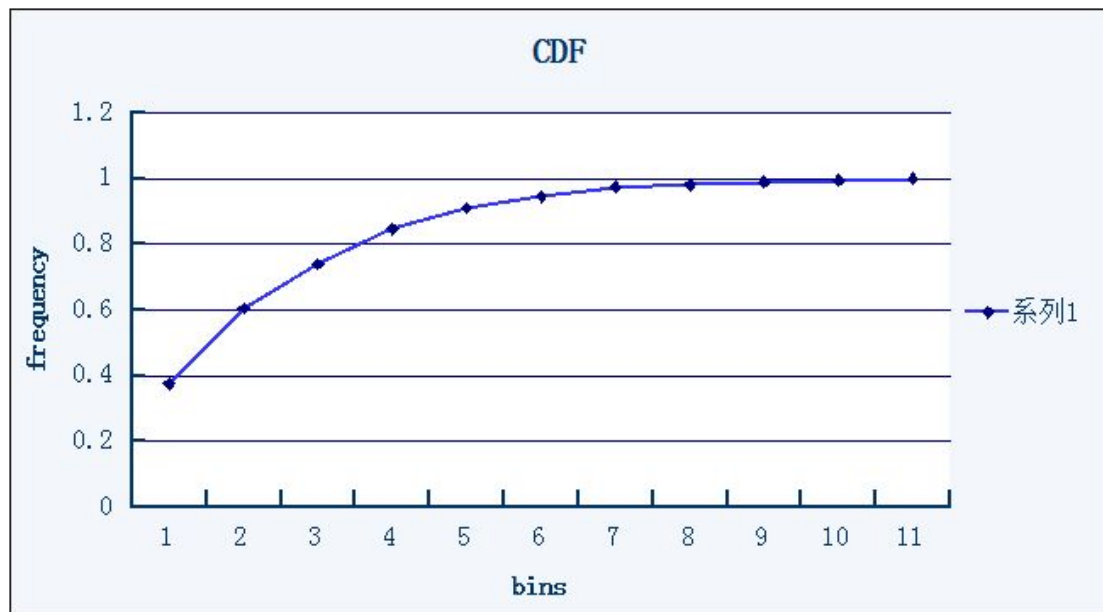
376 229 136 106 64 35 29 7 9 4 5

The data are: 376 229 136 106 64 35 29 7 9 4 5 in 11bins.

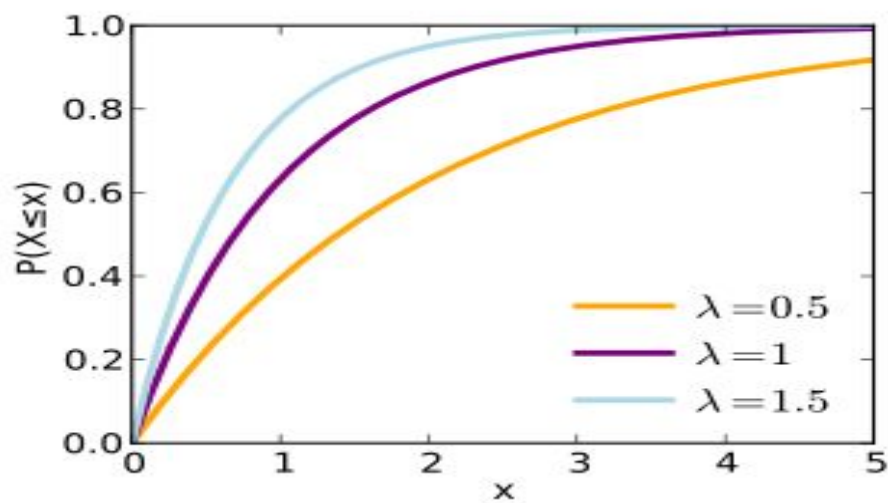


The mid point of bins are slowly decreasing from 1-11 bins.

Actual CDF:



exponential CDF:



Conclusion: They are similar in the CDF.

8.

Procedures:

Step1: Generate $R \sim U[0,1]$

Step2: If $R \geq p$, accept $X=R$

Step3: If $R < p$, reject R , return to Step1