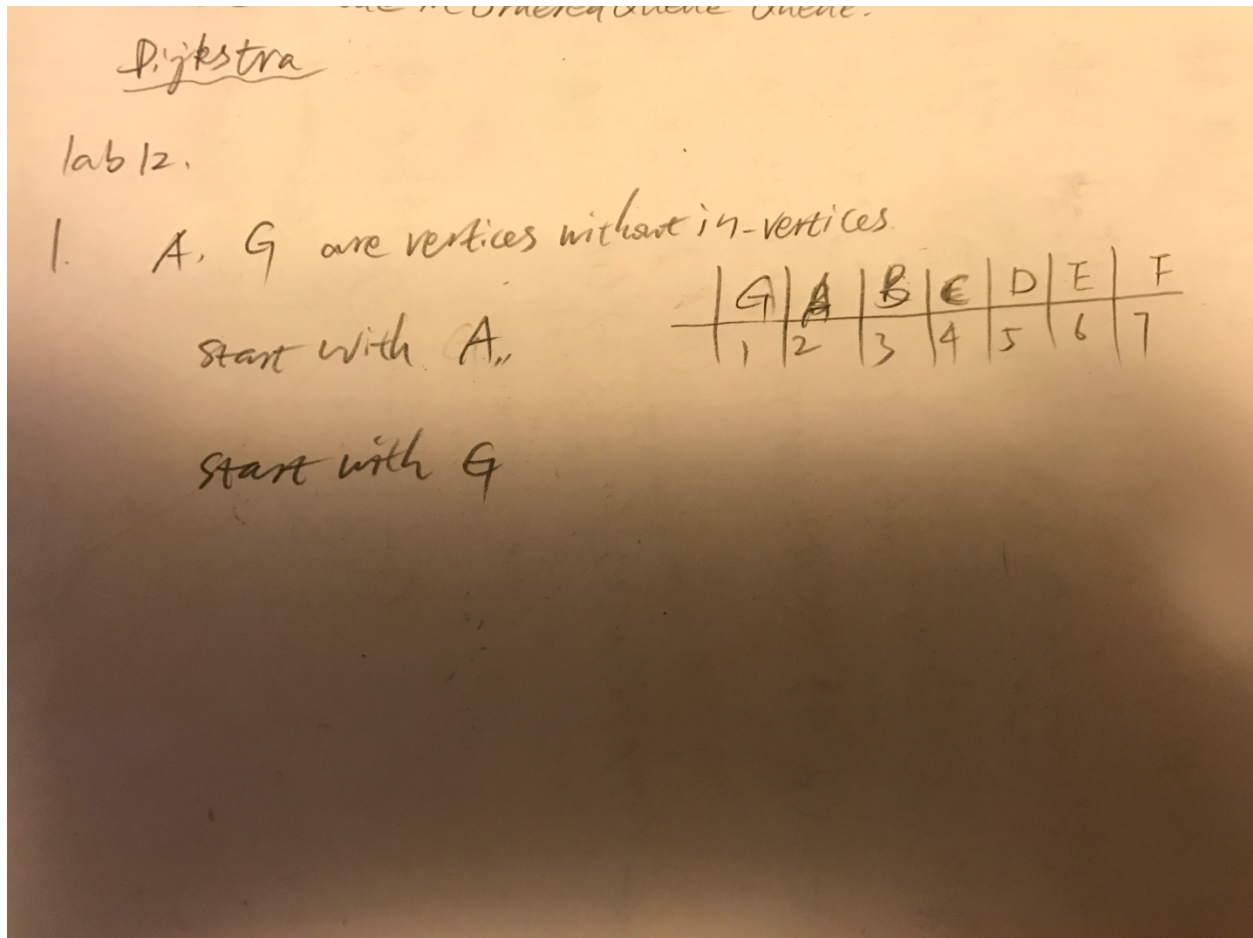


Lab 12 YuliangJin 986381

Problem 1

Perform the General Topological Sort algorithm on the following graph.



Problem 2

Devise an algorithm for the following problem. Then give the asymptotic running time of your algorithm, including an explanation of how you arrived at this running time.

Algorithm: IsReachableFrom(G, u, v) Input: A directed graph G , vertices u, v in G

Output: TRUE if there is a directed path from u to v in G , false

otherwise.

Algo: $\text{isReachableFrom}(G, u, v)$

Input: A directed graph G , vertices u, v in G .

Output: true if there is a directed path from u to v in G , false otherwise.

Create a Queue Q , and offer u to Queue.

While (Q is Empty) do

$n = Q.size()$;

for ($i = 0$ to n)

$v' = Q.poll()$;

mark v' as visited

put all v' out adjacent vertices into the Queue.

if $v' = v$ { return true; }

return false;

Conclusion. We use BFS to search reachable vertices from u ;

Running time: For the worst case, all vertices should be searched for each vertex. enqueue takes $O(1) \rightarrow n O(1)$, dequeue takes $O(1)$. $n O(1)$, so the running time is $O(n)$.