

Geographical-based Friendship Network

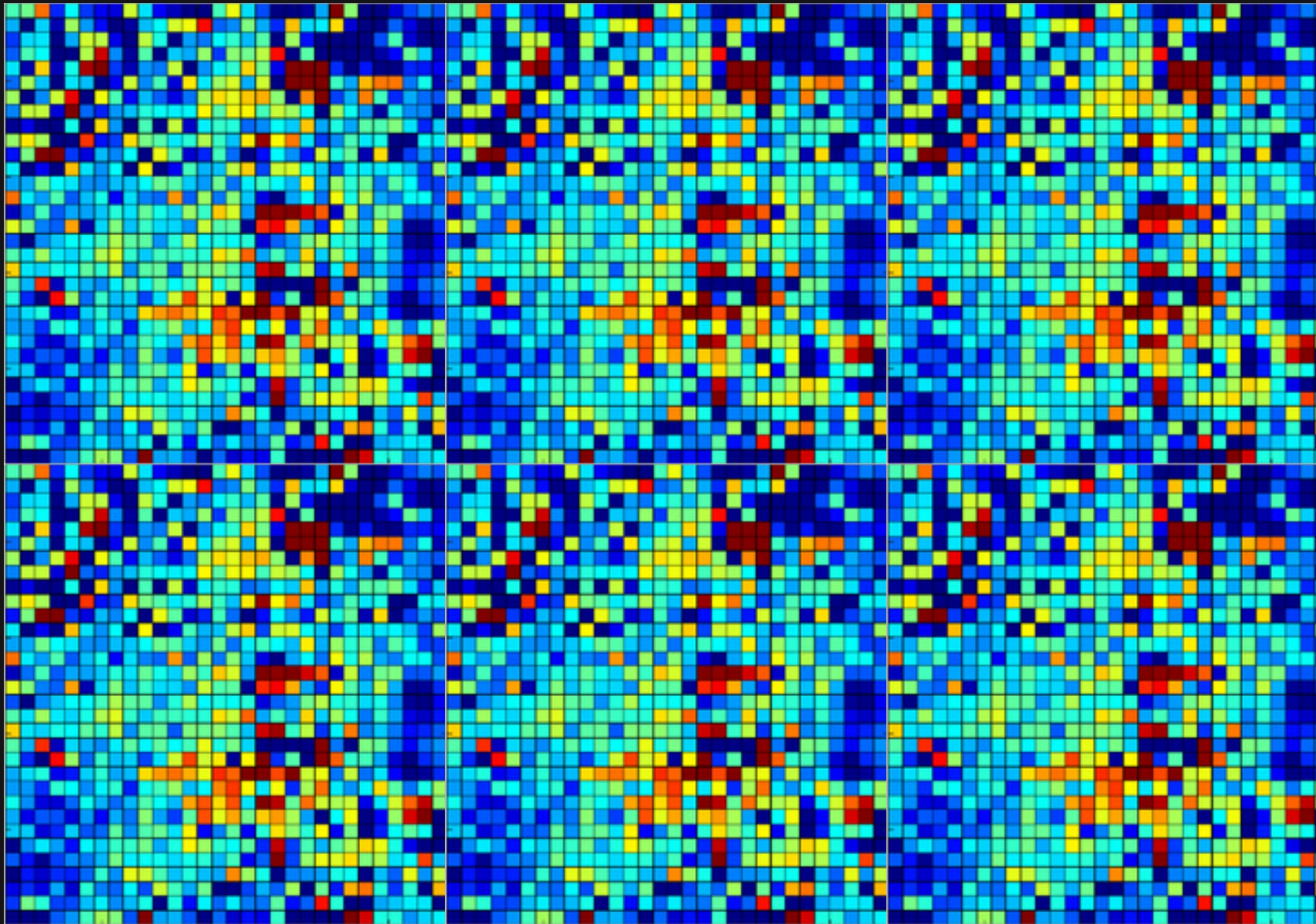
Assignment 1d

Probability & Statistics SA 2023-2024

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Inhabitant Map

1. Purely Random Map



1000 individuals within a unit square, $[0, 1]^2$

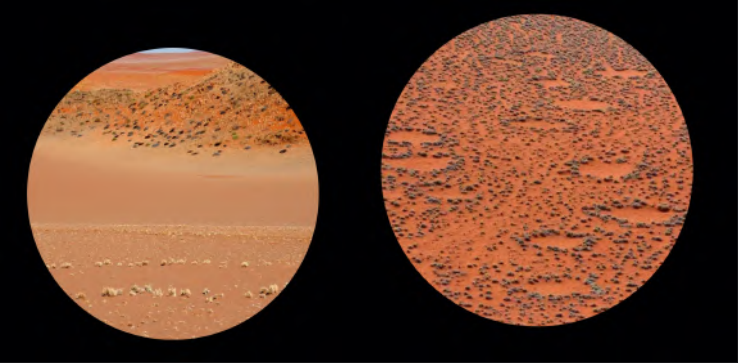
Each individual is represented
by coordinates (x, y)

Inhabitant Map

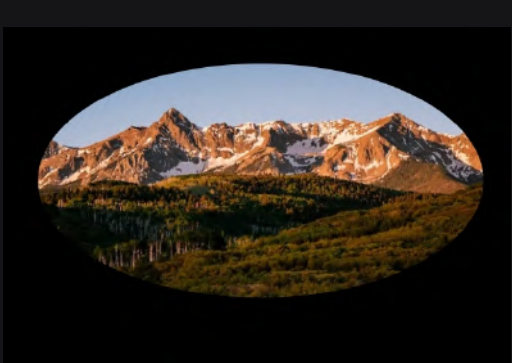
2.Geographical based Random Map

Each individual
in this case is
characterized
by coordinates (x, y)

f (x, y) = geographical
feature f
characterizing (x, y)



Circular deserts



Elliptical mountain ranges



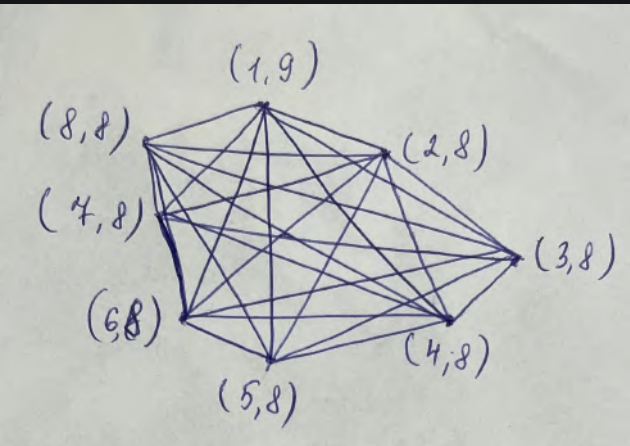
Winding rivers



Rectangular cities

1.Friendship Network

- a)nf (number of features = 8 (2 examples of each feature)
- Feature 1 (Desert1): 9.2
- Feature 2 (Desert2): 8.8
- Feature 3 (Mountain Range1): 8.7
- Feature 4 (Mountain Range2): 8.5
- Feature 5 (Winding River1): 8.4
- Feature 6 (Winding River2): 8.6
- Feature 7 (City1): 8.3
- Feature 8 (City2): 8.9



Erdos–Rényi model

$$P[\text{random person settles in } (x,y)] = \frac{s_{f(x,y)}}{\sum_{(x',y') \in \text{Map}} s_{f(x',y')}} = 0.11$$

$$P(A - B) = \exp \{-\beta * \text{dist}[(x_A, y_A), (x_B, y_B)]\} = 0.1$$

Scenario 1

```
1 #Scenario 1
2 i)def SamplingIndividuals(n):
3     points = []
4     for i from 1 to n:
5         x = random value between 0 and 1
6         y = random value between 0 and 1
7         add (x, y) to points
8     return points
9
10 ii)def euclDistMatrix(individuals):
11     n = number of individuals
12     distance = n x n
13     for i from 1 to n:
14         for j from 1 to n:
15             if i == j:
16                 distance[i][j] = 0
17             else:
18                 distance[i][j] = euclidean_distance(individuals[i], individuals[j])
19     return distance
20
21 ----- def euclidean_distance(individuals[i], individuals[j]): -----
22     dx = individuals[i]
23     dy = individuals[j]
24     distance = sqrt( (xi-xj)^2 + (yi-yj)^2 )
25     return distance
26
27 iii)def distMatrixFromN(n):
28     for iteration from 1 to 100:
29         individuals = SampleIndividuals(n)
30         distance_matrix = euclDistMatrix(individuals)
31         summary_info = compute_summary(distance_matrix)
32         for measure in summary_measures:
33             summary_measures[measure].append(summary_info[measure])
34     return summary_measures
35
36 ----- def compute_summary(distance): -----
37     min, max, average, total = 0
38     for i from 1 to n:
39         for j from i+1 to n:
40             distance = distance[i][j]
41             average = total / n
42             if distance < min:
43                 min = distance
44             if distance > max:
45                 max = distance
46
47 iv)def erdosRenyiFromP(n, p):
48     for i from 1 to n:
49         for j from i+1 to n:
50             if (random value between 0 and 1) < p:
51                 add an edge between node i and node j in graph
52     return graph
53
```

c) i) In my opinion, ErdosRenyiFromP model can be realistic for Friendship Network, because If look at this globally, people's communication in real life or online looks like a threads, which are connected and develop, and make a new nodes and edges from it.

Scenario2

```
1 #Scenario 2
2 i)def geographicalFeatureMap(n):
3     map = nxn
4     circularDesert(map)
5     ellipsoidalMountain(map)
6     sinusoidalRiver(map)
7     rectangularCity(map, 3)
8     return map
9
10 ii)def geographicalFeatureProbability(map):
11     probability_value = nxn
12     for each point in map:
13         probability_value[point] = probability(point)
14     return value
15
16 iii)def geographicalSample(map, n):
17     individuals = n
18     probability = geographicalFeatureProbability(map)
19     for i from 1 to n:
20         individual = mapIndividual(probability)
21         individuals.append(individual)
22     return individuals
23
24 iv)def euclDistMatrix(individuals):
25     matrix_distance = nxn
26     for i from 1 to n:
27         for j from 1 to n:
28             matrix_distance[i][j] = distance(individuals[i], individuals[j])
29     return matrix_distance
30
31 v)def adjMatrixFromDist(matrix_distance, beta):
32     adjacencyMatrix = nxn
33     for A from 1 to h:
34         for B from 1 to n:
35             u = uniform[0, 1]
36             probability = probability_A_B(matrix_distance[A][B], beta)
37             if u < probability:
38                 adjacencyMatrix[A][B] = 1
39             else:
40                 adjacencyMatrix[A][B] = 0
41     return adjacencyMatrix
42
43 vi)def degreeFromAdjMatrix(adjacencyMatrix):
44     total = 0
45     for i from 1 to n:
46         total = sum(adjacencyMatrix[i])
47         totalDegree += degree
48     meanDegree = total / n
49     return meanDegree
50
```

c)Relationship between the geographical features and the groupings of friends in the network: probabilities values of individuals on the grid, which based on different factors, comparison.

It looks more realistic because based on individuals's values, limited applicability and show on the graphs all probabilities of forming friendship network.



Pitch

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