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Evolution of Moisture Transport Patterns in the North Atlantic in different Climate scenarios

Masterarbeit

Leipzig, Mai 2024

vorgelegt von

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Abstract

The distribution and variability of precipitation in Europe are significantly influenced by moisture transport over the north(east)ern Atlantic. The objective of my master thesis is to analyze the evolution of moisture transport patterns in various future climate scenarios. The foundation of this research lies in the MPI-GE, the Max Planck Institute Grand Ensemble Dataset, comprising an ensemble of 100 members for different RCP (climate) scenarios up until 2100. Each member provides multiple fields of relevant climate data. A challenge will be the visualization of uncertainty stemming from 100 different simulations, which will not be straightforward.

To quantify moisture transport, an integrated water vapor transport (a combination of wind and specific moisture) scalar/vector field will be generated from the MPI-GE. Windowed Empirical Orthogonal Functions (EOFs) will be used to extract spatial-temporal patterns and simplify the data, making it easier to evaluate pattern evolution over time.

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1 Introduction and Motivation

1.1 Motivation

Since the discovery (and further confirmation) of the greenhouse effect in the years from 1824 to 1900 [6, 7] humans came a long way of fighting the consequences of the increased greenhouse gas concentration in earth's atmosphere. In 1972 Sawyer summarized the knwoledge and predicted quite accurately the warming at the end of the century [18] Especially the last decades the climate crisis gained more and more attention, leading to the creation of multiple international organizations and institutions (e.g. the International Panel on Climate Change (IPCC) in 1988).

In 2019 more than 11,000 scientists from around the world released a declaration [16], calling governments from around the world to action. The mid and long-term consequences are manyfold and go far beyond the general rising of the worlds' average temperature (see Figure 1.1), e.g. shifts in circulation systems like the North Atlantic Oscillation (NAO) [25], which in turn also have varying consequences. Understanding what consequences may lay ahead of us is a crucial step in tackling these challanges, and this thesis aims to follow up on the research of Vietinghoff et al., trying to evaluate in a similar manner the systemic changes of moisture transport patterns in Europe and the northern Atlantic.

1.2 Climate and Climate Research

This section should give an introduction to the current state of climate research. Therefor it should explain what the current way of future climate predictions is (Coupled Models), how they work, and It should explain some part of the politics, who is involed in what and what the backroud of the most important projects (CMIP, ScenarioMIP ...). It should be explained that the data used is the one that the highest council of fighting climate change uses for its report.

1.

IPCC and the Coupled Model Intercomparison Project (CMIP)

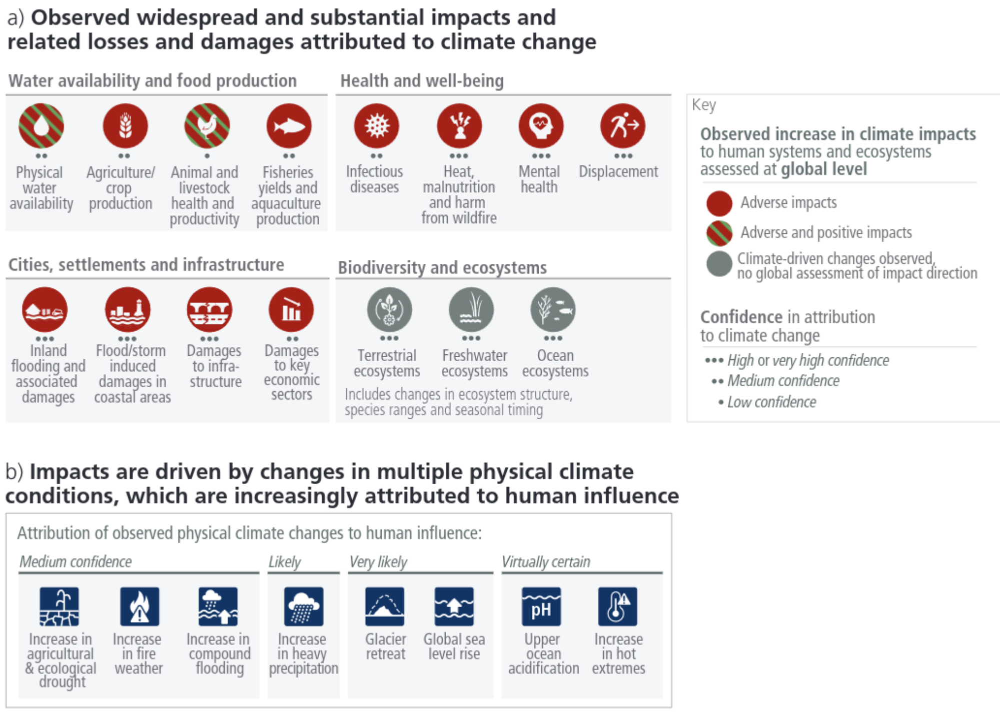

Figure 1.1: Impact of Climate Change for Humans, taken from [9]

The reason for the endorsement of the IPCC by the UN General Assembly 1988 was to prepare comprehensive reviews and report about the current state of scientific knowledge and research. Since then there were six assement cycles and six reports were published, condensing the research of the scientific community. Figure 1.1 is a graphic from the latest report for policy makers from 2023 [9], displaying the probable consequences for humans in climate change. A main source for such figures in the reports are so-called Global Coupled Models (GCM), trying to model the state and evolution of certain fields of earth data . They consist of multiple Models, each representing a major part of Earth's complex climate system (like atmosphere, hydrosphere, etc.), also allowing to model the dynamic interactions between these parts. In the mid 90s the Coupled Model Intercomparison Project (CMIP) was brought to life, with the aim of streamlining results of GCMs and making them compareable. CMIP provides the outer structure, amongst others what kind of simulations to produce (e.g. preindustrial control simulations, future scenarios etc.), what kinds of fields should be generated, what kind of resolutions to provide and also how these results should be serialized. Since then the results of CMIP played an increasingly major part in the reports of the IPCC [23], and are now even called "... one

back up with sources and better writing

of the foundational elements of climate science" [4]. CMIP is currently in its 6th phase, corresponding to the recently finished 6th Assessment Report of the IPCC [9].

The North Atlantic Oscillation

1.3 Research Questions and Thesis Structure

Structure:

1. **Preliminaries**: explain what climate simulations are, what cmip(6) is and its relation to the IPCC reports and what that means for the global fight against the climate crisis. This chapter should prepare the reader to understand all the related work in Chapter 4.
2. **Problem Analysis**: explain what I want to do using the CMIP6 simulations: Describe what the general plan is: Visualization of the moisture transport in Europe with the help. Also define what the goals of the visualizations are: Visualize different scenarios for comparison, visualize uncertainties of different members, visualize evolution over time, also try combining those. Here should be a graphic that explains the workflow that transforms a simulation into some nice pictures
3. **Related Work**: Show what efforts have already been done regarding analysis of moisture transport, future and past. Maybe preparing a comparison table would be good.
4. **Realization**: Describe in a step by step way what measures had been taken.
5. **Evaluation**: A little bit unsure how far I (as a CS person) can evaluate this, have to come up with a concept
6. **Conclusion**: Same as step before, but there will be something to write about after everything else is written

2 Basics

This section should explain the basic math to understand the aforementioned topics, not that much needed but still needs to be there.

2.1 (Uncertain) Fields

2.2 Empirical Orthogonal Functions

3 MPI GE CMIP6

The Max Planck Institute Grand Ensemble CMIP6 (MPI GE CMIP6) is a Single-model initial-condition large ensemble (in short: SMILE) [14]. This means that a single model was run with different initial condiditions but the same external forcings (e.g. greenhous gasses) mutiple times (⇒ ensemble). This makes it possible to seperate the internal variability from the responses to the external forcing, enabling researchers to better quantify the consequences of climate change (for example) . Additionally it makes the research of extreme weather phenomena (e.g. droughts, floods etc.) more robust in spite of their rare occurences [11]. As described in Section 1.2, Coupled models

The dataset chosen for this project is the *Max Planck Institute Grand Ensemble CMIP6* (from now on MPI-GE CMIP6), presented by Olonscheck et al. [14]. The reasons for choosing this dataset are manifold:

1. It uses the latest (6th) phase of the Coupled Model Intercomparison Project (CMIP6)
2. Compared to its predecessor (MPI-GE [12]) it provides high frequency output (6 hour intervals vs. monthly means), which enables taking short-lived weather events and structures (e.g. atmospheric rivers) into account which would be lost in the calculation of the mean
3.

This section should explain what datasets are available and why I chose the MPI-GE CMIP6 [14]

Maybe but the comparison table from [14] here and expand it a bit.

4 Related Work

This section outlies the current state-of-the-art in the main parts of this thesis explained in Section 1.3: Quantifying Moisture (Transport), extracting spatio-temporal patterns, tracking their change over time and visualizing the uncertain results in the end.

4.1 Motivation

As explained in Chapter 1, the approach of this thesis is motivated by the approach of Vietinghoff et al. in [25] and the affiliated dissertation [24], which tackles the issue of detecting critical points in unstable scalar fields. Hereby [25] analyzes the MPI GE [12] from the 5th phase of CMIP, an ensemble simulation with 50 members. The goal was to find the probable centers of pressure high/lows in the NAO pattern (see Section 1.2) and to track their shift over time. They employed a sliding window approach, computing the dominant pattern (see Section 2.2) for each window and member, and determine the likely areas of critical points by merging the results of different memebers per timestep. The centers of mass of these critical areas are then tracked over time to visualize the shift of the pressure high and low. The results show that the patterns do change, and this change is more pronounced if climate change is stronger. Also, there is no significant change if the climate remains stable.

4.2 Uncertainty Visualisation

4.3 Moisture Transport

To computationally extract any spatio-temporal patterns of moisture (transport), it first needs to be quantified in any way. The variable from the MPI GE CMIP6 used for this task is the *specific humidity*, which has no unit and is a float value between 0.0 and 1.0, denoting the percentage of water in the air at a specific gridpoint. The vast majority of literature regarding moisture transport use some form of vertically integrated humidity and the variants will be explained in the following section. A popular usage of these quantifications was to find a filamentary weather structure called "Atmospheric Rivers"[1], a prominent way of water vapor transportation in the extratropic regions [8].

The most straightforward way of quantifying moisture is **Vertically Integrated Water Vapor (IWV)** [2, 8, 13, 19, 27], which is essentailly the vertical integral of the specific humidity q over the pressure levels p from earth's surface P_S to some upper limit in the atmosphere:

$$IWV = \frac{1}{g} \int_0^{P_s} q \, \mathrm{d}p \tag{4.1}$$

Similar to Equation 4.1, Zhu and Newell proposed in [28] **Vertical Integrated Moisture Transport (IVT)**, a way of moisture transport by vertically integrating over the different pressure levels the zonal (along latitude lines) and meridional (along longitude lines) fluxes. It became a popular metric for finding atmospheric rivers [8], sometimes alongside IWV [3]. IVT has the unit $\frac{kg}{ms}$ and is usually defined with

$$\overrightarrow{IVT} = \frac{1}{g} \int_0^{P_s} q \begin{pmatrix} u \\ v \end{pmatrix} \mathrm{d}p \tag{4.2}$$

or in a mathematically equivalent form [5]. Here u and v stand for the zonal and meridional components of the horizontal wind vector. While Equation 4.2 yields a vector field, the euclidian norm of said vector field

$$\|IVT\| = \frac{1}{g} \sqrt{(\int_0^{P_s} qu \, \mathrm{d}p)^2 + (\int_0^{P_s} qv \, \mathrm{d}p)^2} \tag{4.3}$$

is also a popular choice in detecting atmospheric rivers [15, 21] and other use cases [1].

Also, this paper lists some other methods of moisture transportation which are also used

The IVT is also part of the atmospheric moisture budget [26] (and similar in [20]) given by

$$\frac{1}{g} \frac{\delta}{\delta t} \int_0^{P_s} q \, \mathrm{d}p = -\nabla \cdot \frac{1}{g} \int_0^{P_s} q \begin{pmatrix} u \\ v \end{pmatrix} \mathrm{d}p + E - P$$

With E being the total evaporation and P the precipitation. Yang et al. showed in their report [26] the directions of moisture flux and its evolution in the last three decades. The analysis was done for all continental borders based on the big ERA5 reanalysis. The metrics used for this analysis were mostly the evaporation E, precipitation P and the moisture transport convergence $VIMC = \frac{1}{g} \int_0^{P_s} \nabla \cdot q \binom{u}{v} \mathrm{d}\, p$ from Equation 4.3.

[1]earlier or alternative name: "Tropospheric Rivers"

There are also some other notable other algorithms, namely stable oxygen isotope investigation [10] and langragian backwards trajectories [27], but both rather look for the origin of the water vapor instead of its destination and are therefor out of scope for this thesis.

4.4 Pattern analysis regarding IVT

While there are many areas of interest for the application of EOF, this Section will give an overview what kind of pattern analysis has been performed in relation with IVT data. An overview of datasets, timescopes and other metadata is given in Table TODO

Although most found related work uses EOF analysis, Teale and Robinson employ an approach using Self Organizing Maps (SOMs) to detect patterns of moisture tronsport in the eastern United States. SOMs are a machine learning approach to reduce data dimensionality, producing a 2D map of higher dimensional data. While they acknowledge the efficiency of EOF to extract dominant patterns, they emphasize the problem of required orthogonality of modes, which is not given for SOMs. The results show that fluxes with the highest moisture content occur less frequently than those with less moisture. But despite the higher moisture content, fluxes with lower moisture transport dominate water vapor movement due to their prevalence. Many of these fluxes meet typical criteria for atmospheric rivers, with varying trajectories and sources suggesting diverse mechanisms of formation. The temporal variability in monthly flux frequencies correlates with regional precipitation patterns, indicating that this approach is a valuable framework for studying precipitation changes [22].

CITE?

Ayantobo et al. analysed the primary six modes of EOF in China, which was grouped in deifferent regions for comparison. While the variances of IVT in eastern to southern China were quite high, the variances in northern China were quite low. It was shown by comparing the temporal patterns of the primary mode of EOF with the ENSO, that these patterns were related. The cross-wavelet coherence revealed that IVT and ENSO timeseries were coherent, which implies that increased IVT was prevalent linked to increased ENSO activities [1].

Published in 1982, Salstein et al. provided the first example of calculating EOF on IVT. Based on data from 91 weather stations, they computed the IVT of the whole northern hemisphere. Statistical siginificance was determined by employing a Monte Carlo testing method. EOF was computed on the IWV, the zonal and meridional IVT fields respectively, but they also evaluated an approach of combining both IVT components in one data vector.

They reported the significance of the primary mode of IWV, encoding nearly half (44 %) of variance of the data.

5 Methodology

5.1 Overview

Explain what I want to do using the CMIP6 simulations: Describe what the general plan is: Visualisation of the moisture transport in Europe with the help . Also define what the goals of the visualisations are: Visualize different scenarios for comparison, visualize uncertainties of different members, visualize evolution over time, also try combining those. Here should be a graphic that explains the workflow that transforms a simulation into some nice pictures

5.2 Preprocessing

The goal of this step is to generate an IVT field (see Chapter 4) from the MPI GE CMIP6 (see Chapter 3). The steps to complete this task are quite straight forward:

1. Load four different fields for each time period in each member in each szenario: Specific humidity *hus*, eastward horizontal wind *ua*, northward horizontal wind *va* and surface pressure *ps*. Here the geographical box around the area of interest is cut out: Europe and the North Atlantic (Longitude: $-90 \rightarrow 40$, Latitude: $20 \rightarrow 80$, based on [25])

2. For each geographical gridpoint (lon, lat) and timestep: Calculate the integrals of hte product of wind components and specific humidity over the vertical pressure levels $\frac{1}{g}\int_{ps}^{0} hus * ua$ and $\frac{1}{g}\int_{ps}^{0} hus * va$, with g being the gravitational acceleration ($9.806\frac{m}{s}$)

3. Save the results for each time period in each member in each szenario in a NetCDF file for the further steps.

The calculations were performed on the high performance computing cluster[1] of the German Climate Calculations Center (DKRZ), due to the MPI GE CMIP6 is saved there and downloading the data would take a lot of time. This also result in the goal of this step

[1]https://docs.dkrz.de/doc/levante/

to minimize the hours on the HPC system since they get billed by the time using nodes. Although these steps seem easy, due to the large sizes of the datasets and other issues many challenges were met. In the following those will be explained with regard to the step they ocurred in.

1. **Data Loading**

   - cutting out geobox
   - slow IO → started using dask+xarray

2. **Vertical integration**

   - calculate hybrid sigma pressure levels for each gridpoint and timestep to get the x values for integration
   - describe my idea of testing the integration

6 Results

7 Conclusions and Future Work

7.1 Conclusions

7.2 Future Work

Acronyms

PCA	Principal component analysis
SNF	Smith normal form
TDA	Topological data analysis

Glossary

LaTeX	A document preparation system
$\mathbb{R}$	The set of real numbers

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