

# (LLM) Multi-Agent

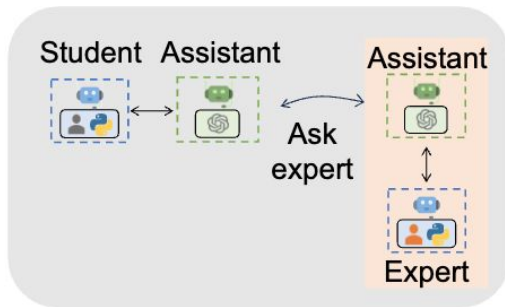
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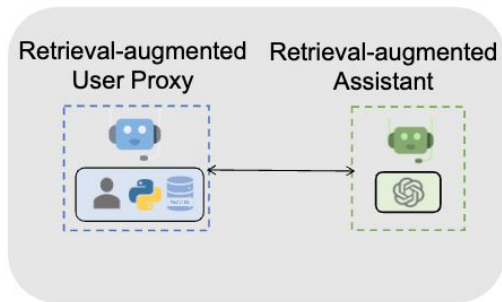
Presented by Jiaming Shen

Nov. 15th, 2024

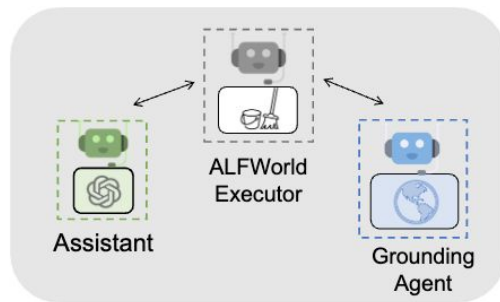
# From Language Agent to (LLM-powered) Multi-Agent Paradigm



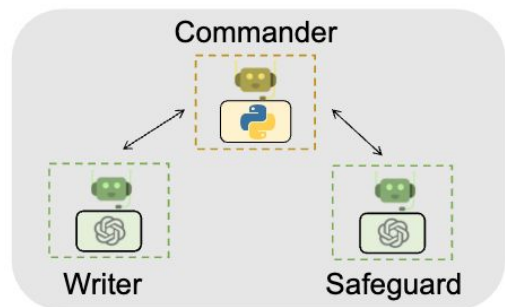
A1. Math Problem Solving



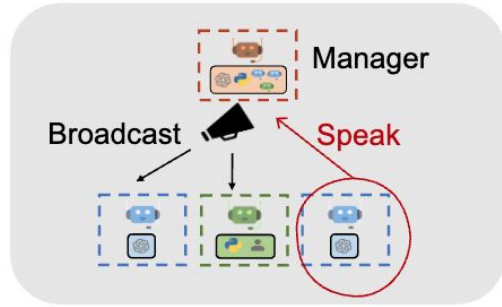
A2. Retrieval-augmented Chat



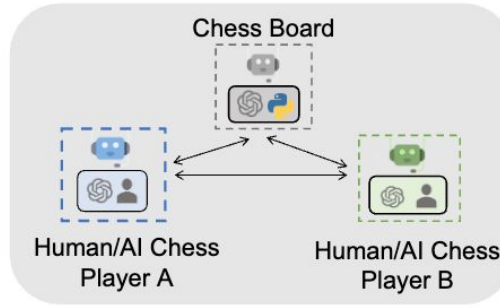
A3. ALF Chat



A4. Multi-agent Coding



A5. Dynamic Group Chat

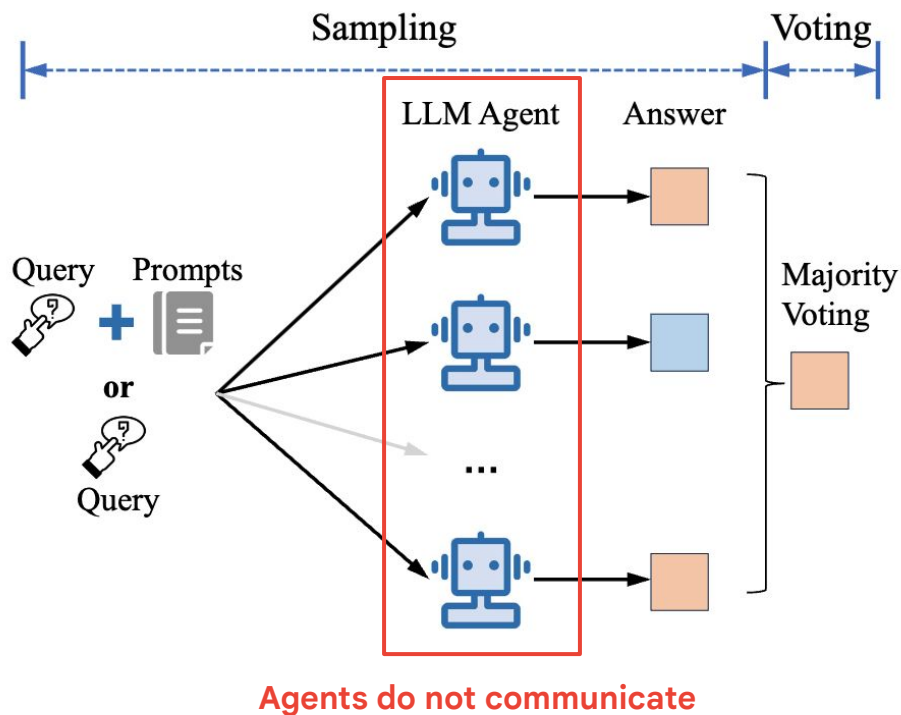


A6. Conversational Chess

# Outline

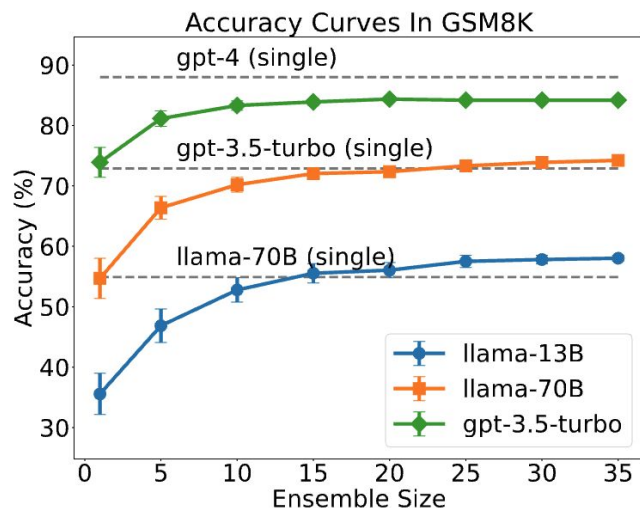
- **Multi-agent Methods**
  - Late-stage Ensemble
  - Mixture-of-Agents
  - Multi-Agent Debate
- Multi-agent Ecosystems

# Multi-agent Method 1 – Late-stage Ensemble



- 1: Initialize an empty set for samples  $S \leftarrow \emptyset$
- 2: **for**  $i = 1$  to  $N$  **do**
- 3:   Generate sample  $s_i \leftarrow \mathcal{M}(x)$  or  $s_i \leftarrow f_{\mathcal{M}}(x)$
- 4:   Add sample to the set  $S \leftarrow S \cup \{s_i\}$
- 5: **end for**
- 6: **for** each sample  $s_i$  in  $S$  **do**
- 7:   Initialize similarity scores  $V(s_i) \leftarrow 0$
- 8:   **for** each sample  $s_j$  in  $S$  **do**
- 9:     **if**  $i \neq j$  **then**
- 10:        $V(s_i) \leftarrow V(s_i) + \text{sim}(s_i, s_j)$
- 11:     **end if**
- 12:   **end for** Task-specific sim
- 13: **end for**
- 14:  $A \leftarrow \arg \max_{s_i \in S} V(s_i)$
- 15: **return**  $A$

# Multi-agent Method 1 – Late-stage Ensemble



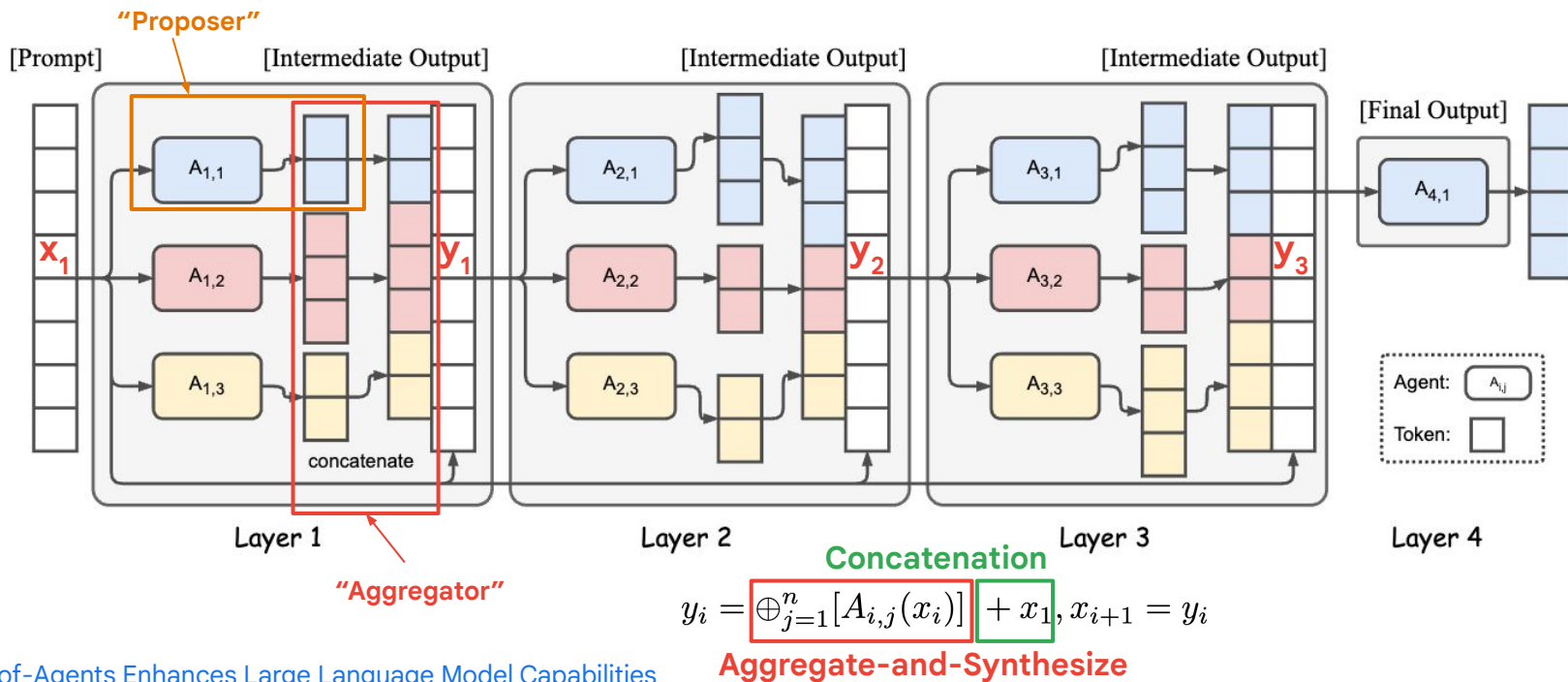
[More Agents Is All You Need](#)

General Reasoning    Code Generation

Model	Method	MMLU		HumanEval	
		Standalone	+Ours	Standalone	+Ours
Llama2-13B <a href="#">Touvron et al. (2023)</a>	<a href="#">COT Wei et al. (2022)</a>	0.42	0.43 (+0.01)	0.13	0.20 (+0.07)
	<a href="#">ZS-COT Kojima et al. (2022)</a>	0.42	0.48 (+0.06)	0.15	0.22 (+0.07)
	<a href="#">SPP Wang et al. (2023c)</a>	0.32	<b>0.53</b> (+0.21)	0.03	0.08 (+0.05)
	<a href="#">Debate Du et al. (2023)</a>	0.37	0.39 (+0.02)	0	0
	<a href="#">Reflection Shinn et al. (2023)</a>	0.45	0.50 (+0.05)	0.06	0.13 (+0.07)
	<b>Ours</b>	<u>0.51</u>		<b>0.25</b>	
Llama2-70B <a href="#">Touvron et al. (2023)</a>	<a href="#">COT Wei et al. (2022)</a>	0.56	0.57 (+0.01)	0.30	0.32 (+0.02)
	<a href="#">ZS-COT Kojima et al. (2022)</a>	0.54	<b>0.65</b> (+0.11)	0.23	0.29 (+0.06)
	<a href="#">SPP Wang et al. (2023c)</a>	0.49	0.63 (+0.14)	0.15	0.20 (+0.05)
	<a href="#">Debate Du et al. (2023)</a>	0.56	0.58 (+0.02)	0	0
	<a href="#">Reflection Shinn et al. (2023)</a>	0.42	0.55 (+0.13)	0.16	0.26 (+0.10)
	<b>Ours</b>	<u>0.60</u>		<b>0.33</b>	
GPT-3.5-Turbo <a href="#">OpenAI (2022)</a>	<a href="#">COT Wei et al. (2022)</a>	0.61	0.64 (+0.03)	0.70	<b>0.75</b> (+0.05)
	<a href="#">ZS-COT Kojima et al. (2022)</a>	0.58	0.69 (+0.11)	0.67	0.74 (+0.07)
	<a href="#">SPP Wang et al. (2023c)</a>	0.53	0.68 (+0.15)	0.57	0.64 (+0.07)
	<a href="#">Debate Du et al. (2023)</a>	0.56	0.67 (+0.11)	0.18	0.24 (+0.06)
	<a href="#">Reflection Shinn et al. (2023)</a>	0.39	0.44 (+0.05)	0.58	0.73 (+0.15)
	<b>Ours</b>	<b>0.70</b>		<u>0.73</u>	

# Multi-agent Method 2 – Mixture-of-Agents

- Enable cross-layer agent communications



## Multi-agent Method 2 – Mixture-of-Agents

Table 1: Aggregate-and-Synthesize Prompt to integrate responses from other models.

You have been provided with a set of responses from various open-source models to the latest user query. Your task is to synthesize these responses into a single, high-quality response. It is crucial to critically evaluate the information provided in these responses, recognizing that some of it may be biased or incorrect. Your response should not simply replicate the given answers but should offer a refined, accurate, and comprehensive reply to the instruction. Ensure your response is well-structured, coherent, and adheres to the highest standards of accuracy and reliability.

Responses from models:

1. [Model Response from  $A_{i,1}$ ]
2. [Model Response from  $A_{i,2}$ ]
- ...
- $n$ . [Model Response from  $A_{i,n}$ ]

$$y_i = \bigoplus_{j=1}^n [A_{i,j}(x_i)] + x_1, x_{i+1} = y_i$$

**Aggregate-and-Synthesize**

# Multi-agent Method 2 – Mixture-of-Agents

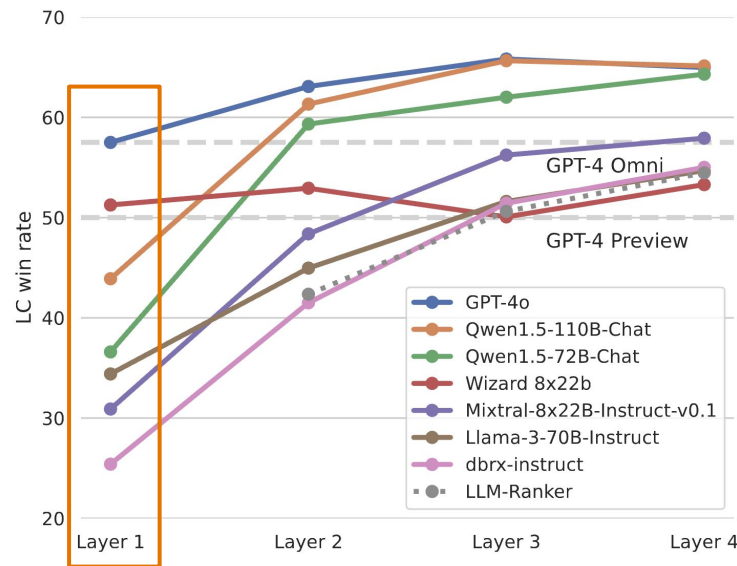
## General ChatBot

(a) AlpacaEval 2.0

3 layers, 6 LLMs in  
each layer, use  
GPT-4o/Qwen1.5  
110B as aggregator

Model	LC win.	win.
MoA w/ GPT-4o	$65.7 \pm 0.7\%$	$78.7 \pm 0.2\%$
MoA	$65.1 \pm 0.6\%$	$59.8 \pm 0.3\%$
MoA-Lite	$59.3 \pm 0.2\%$	$57.0 \pm 0.7\%$
GPT-4 Omni (05/13)	57.5%	51.3%
GPT-4 Turbo (04/09)	55.0%	46.1%
WizardLM 8x22B <sup>†</sup>	51.3%	62.3%
GPT-4 Preview (11/06)	50.0%	50.0%
Qwen1.5 110B Chat	43.9%	33.8%
Qwen1.5 72B Chat	36.6%	26.5%
GPT-4 (03/14)	35.3%	22.1%
Llama 3 70B Instruct	34.4%	33.2%
Mixtral 8x22B v0.1	30.9%	22.2%

2 layers, 6 LLMs in  
each layer, use  
Qwen1.5 72B as  
aggregator





# Multi-agent Method 3 – Multi-Agent Debate

## Counter-Intuitive Question

The two circles are externally tangent and there is no relative sliding. The radius of circle A is  $\frac{1}{3}$  the radius of circle B. Circle A rolls around circle B one trip back to its starting point. How many times will circle A revolve in total?

## Chain-of-Thought

Let the radius of circle A be  $r$  and the radius of circle B be  $3r$ . The distance circle A travels along the circumference of circle B is equal to the circumference of circle B, which is  $6\pi r$ . The number of revolutions =  $(6\pi r) / (2\pi r) = 6\pi r / 2\pi r = 3$ . So, circle A will revolve 3 times in total as it rolls around circle B once. ❌

## Self-Reflection

### Reflection:

- (1) I have a clear understanding of the problem.
- (2) I have used the correct formula for the circumference of a circle and applied it to both circles to find the number of revolutions.
- (3) I have correctly calculated the number of revolutions of circle A.

Based on the results of my self-reflection, I am confident that my answer is correct. Therefore, circle A will revolve 3 times in total as it rolls around circle B once. ❌

## Motivation – “Degeneration-of-Thought” Issue

Once the LLM-based agent has established confidence in its answers, it is unable to generate novel thoughts later through self-reflection even if **the initial stance is incorrect**.

# Multi-agent Method 3 – Multi-Agent Debate

## Counter-Intuitive Question

The two circles are externally tangent and there is no relative sliding. The radius of circle A is 1/3 the radius of circle B. Circle A rolls around circle B one trip back to its starting point. How many times will circle A revolve in total?

## Chain-of-Thought

Let the radius of circle A be  $r$  and the radius of circle B be  $3r$ . The distance circle A travels along the circumference of circle B is equal to the circumference of circle B, which is  $6\pi r$ . The number of revolutions =  $(6\pi r) / (2\pi r) = 6\pi r / 2\pi r = 3$ . So, circle A will revolve 3 times in total as it rolls around circle B once. ❌

## Self-Reflection

### Reflection:

- (1) I have a clear understanding of the problem.
- (2) I have used the correct formula for the circumference of a circle and applied it to both circles to find the number of revolutions.
- (3) I have correctly calculated the number of revolutions of circle A.

Based on the results of my self-reflection, I am confident that my answer is correct. Therefore, circle A will revolve 3 times in total as it rolls around circle B once. ❌

## Multi-Agent Debate

I disagree with you. To find the total number of revolutions, we need to consider both the rotation around circle B and the rotation of circle A itself. Therefore, circle A will revolve 3 times around its own center and 1 time around circle B, making a total of 4 revolutions.

I see your point, but...

That's a valid point, however...

The negative side correctly considers both the rotation of circle A around its own center and its rotation around circle B, while the affirmative side only considers the rotation around circle B. Therefore, the answer is 4. ✅

(1) Force multi-agent debates and rethink the initial response

(2) Use a judge to summarize the multi-agent debate

# Multi-agent Method 3 – Multi-Agent Debate

*You are a debater. Hello and welcome to the debate competition. It's not necessary to fully agree with each other's perspectives, as our objective is to find the correct answer. The debate topic is stated as follows: <debate topic>.*

- Prompt for Affirmative Debater (👤)

*You are affirmative side. Please express your viewpoints.*

- Prompt for Negative Debater (👤)

*You are negative side. You disagree with the affirmative side's points. Provide your reasons and answer.*

*You are a moderator. There will be two debaters involved in a debate competition. They will present their answers and discuss their perspectives on the <debate topic>. At the end of each round, you will evaluate both sides' answers and decide which one is correct.*

Method	ACC (%)
<b>GPT-4</b>	51.0
<b>GPT-3.5-Turbo</b>	26.0
+ CoT	28.0
+ Self-Consistency	29.5
+ Self-Reflect	27.5
+ MAD	<b>37.0</b>

Table 3: Accuracy on Counter-Intuitive AR.

**Math/Arithmetic Reasoning**  
**Challenging task**

# Multi-agent Method 3 – Multi-Agent Debate

Update prompt to include “you should agree with the other agents X% of time”

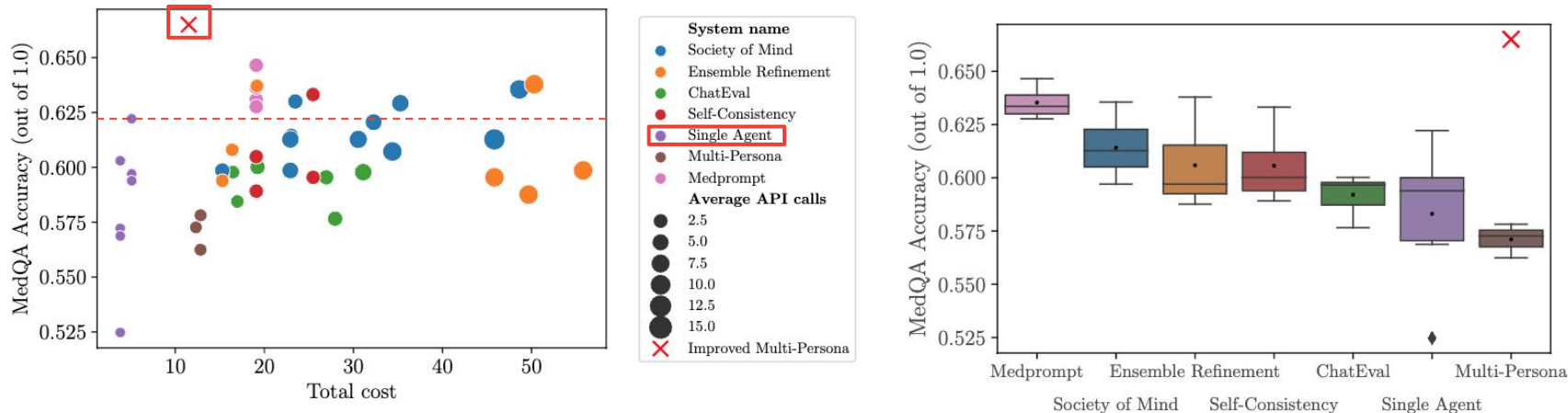


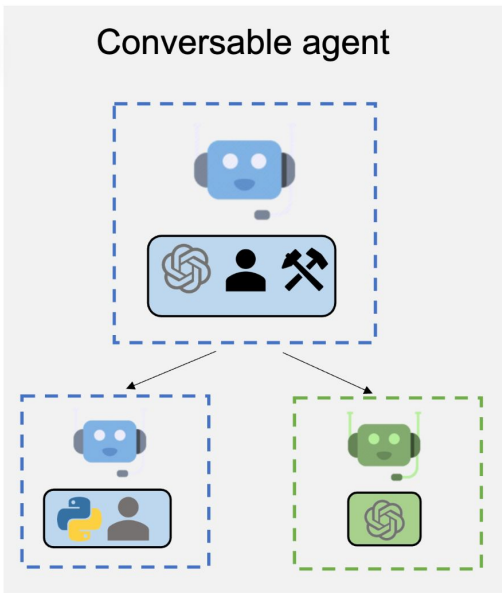
Figure 1. Benchmark of experiment configurations on MedQA dataset. **Left:** Accuracy vs average cost (\$) per question. The size of the dots reflects the average number of API calls required per question. **Right:** Summarizes accuracy grouped by strategy, sorted by average performance (black dot). The **X** represents improved performance using our proposed *agreement modulation*, described in Section 3.

# Outline

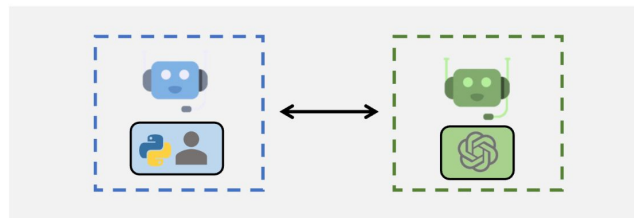
- Multi-agent Methods
  - Late-stage Ensemble
  - Mixture-of-Agents
  - Multi-Agent Debate
- **Multi-agent Ecosystems**

# Multi-Agent Ecosystems – AutoGen

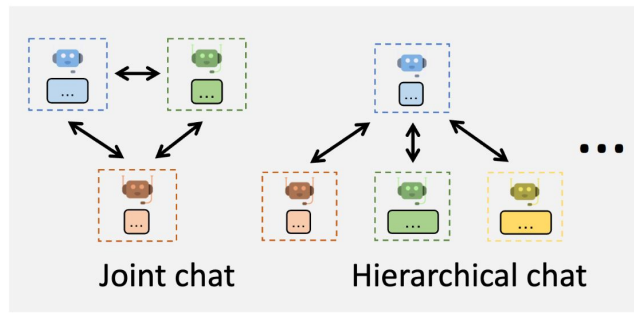
- Support diverse conversation patterns
- Code execution out-of-the box
- Native agent-human interaction workflow
- Good quantitative results on various tasks



**Agent Customization**



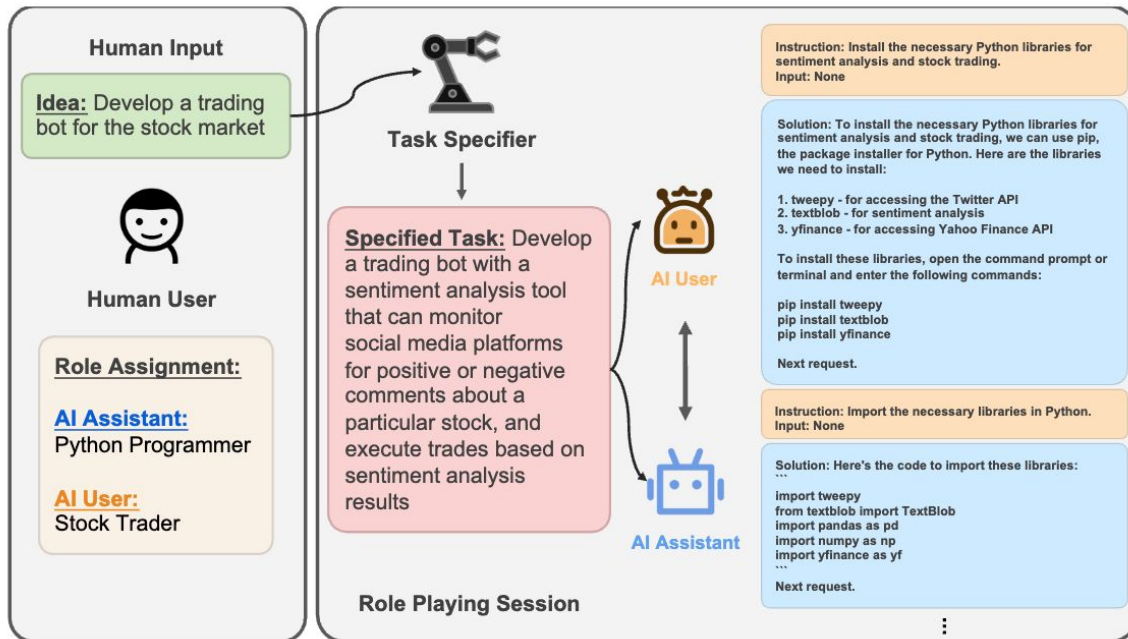
**Multi-Agent Conversations**



**Flexible Conversation Patterns**

# Multi-Agent Ecosystems – CAMEL

- Support extensive external tools
- Integrate with various LLM backends
- Less restrictive license





# Multi-Agent Ecosystems – Others



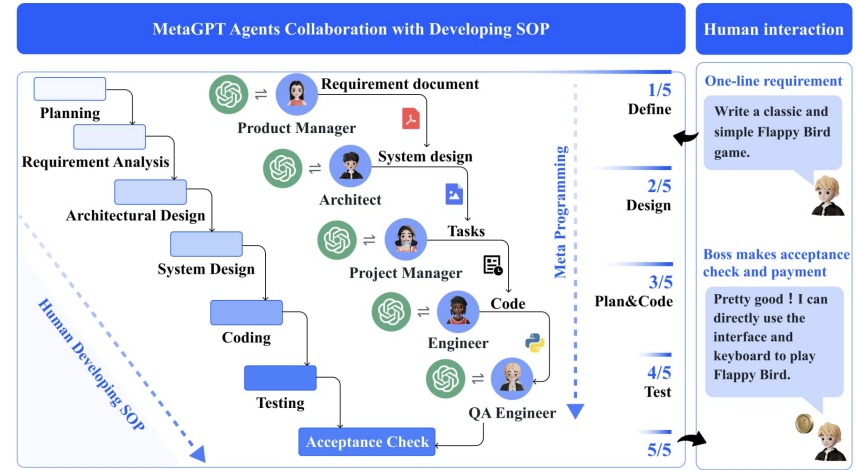
[OpenAI – Swarm](#)



[SuperAgent](#)



[CrewAI](#)



[MetaGPT](#)



# LlamaIndex

[LlamaIndex](#)