

## What you should know for the final (minimum):

- definition of continuous time MC, Markov property, transition probabilities, generator
- representations of MC: infinitesimal (generator), jump-and-hold, transition probabilities, rate diagram and relations between them (in particular  $Q$  and  $P(t)$ )
- computing absorption probabilities and mean time to absorption
- computing stationary distributions for finite and infinite state MCs and interpretation of  $(\pi_i)_{i=0}^{\infty}$
- basic properties of birth and death processes

- conditional density and conditional distribution
- computing probabilities and expectations using the law of total probability
- basic definitions related to renewal processes : renewal and interrenewal times, renewal function, age, excess life
- formula for  $E(W_{N(t)+1})$
- asymptotic distribution of  $N(t)$
- computing the asymptotic behavior of  $M(t)$  (linear and constant term)
- asymptotic distribution of age and excess life
- asymptotic behavior of  $E(\delta_t)$ ,  $E(\gamma_t)$  and  $E(\beta_t)$
- age replacement policy example

- definition of martingales
- examples of martingales (additive, multiplicative, m. transform)
- maximal inequality for nonnegative martingales
- definition of BM
- BM as a Gaussian process
- basic properties of BM
- reflection principle
- computing probabilities of events for the zeros of BM
- computing probabilities of events for the reflected BM
- computing probabilities of events for BM with drift
- computing probabilities of events for geometric BM