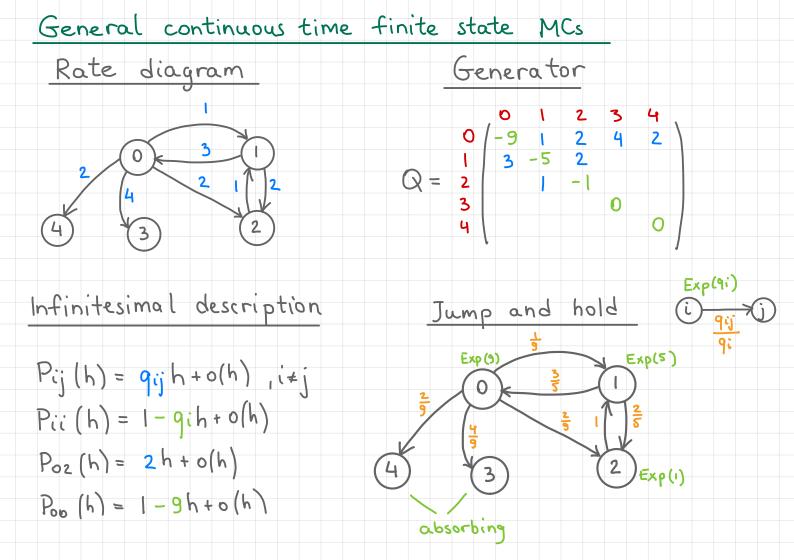
## MATH180C: Introduction to Stochastic Processes II

www.math.ucsd.edu/~ynemish/teaching/180c

# Today: FSA for general MC > Q&A: October 19 Next: PK 6.3, 6.6, Durrett 4.2

This week:

- Quiz 2 on Wednesday, October 21 (lectures 4-6)
- Homework 2 (due Friday, October 23, 11:59 PM)

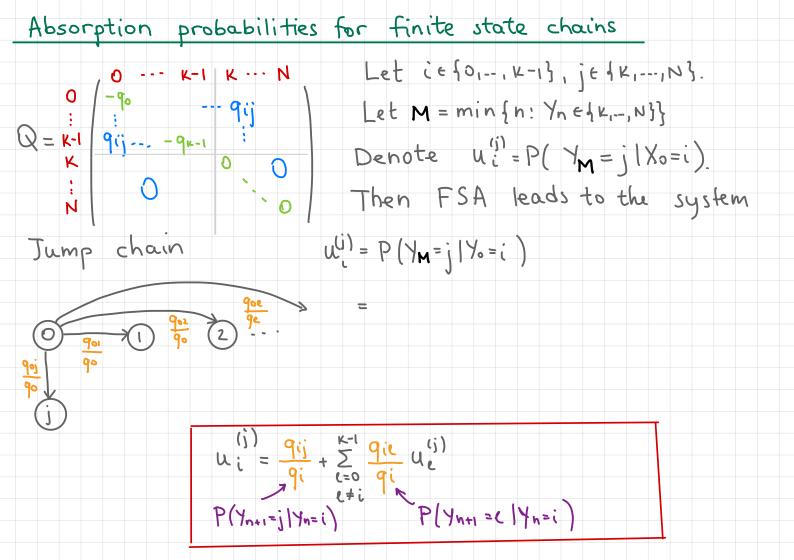


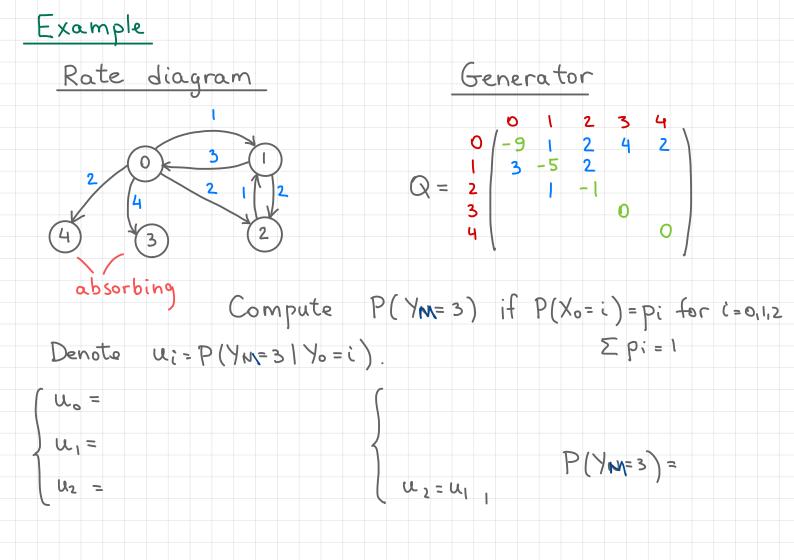
### Absorption probabilities for finite state chains

By considering the jump chain  $(Y_n)_{n\geq 0}$  with  $Y_n = X_{w_n}$  and its transition probabilities  $P(Y_{n+1}=j \mid Y_n=i) = \frac{q_{ij}}{q_i}$  we can apply the first step analysis to compute, e.g., the absorption probabilities (similarly as for B&D)

If state i is absorbing, then qij = 0 for all j ≠ i (no jumps from state i), so qi = qii = 0. Let Q be given by

$$Q = \frac{k-1}{N} = \frac{9ij}{N} - \frac{1}{N} = \frac{1}{N$$





Mean time to absorption Similar analysis as was applied to B&D processes can be used to compute the mean time to absorption: before each jump from step i to state i the process sojourns on average in state i. 0 --- K-1 K ... N Let T= min {t! Xt { {K, ..., N}} M = min {n: Yn = { k, --, N}} Denote Wi= Then FSA gives Exp(9.) Wi =

## Example Rate diagram absorbing

$$\begin{cases} W_0 = \\ W_1 = \\ W_2 = \\ \end{cases}$$

#### Generator