

# Lecture 0: Introduction

Yi, Yung (이웅)

EE210: Probability and Introductory Random Processes  
KAIST EE

MONTH DAY, 2021

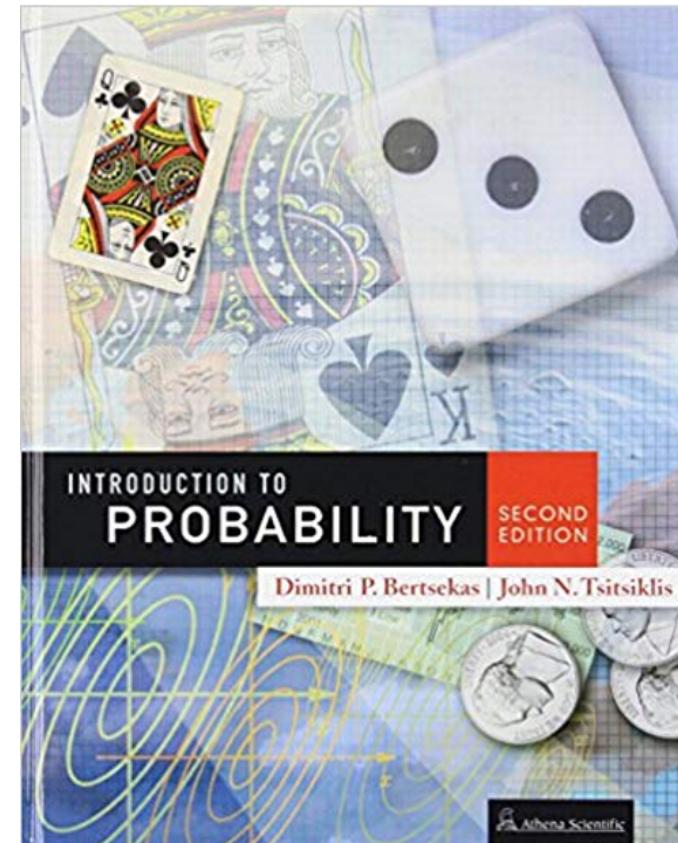
- Course logistics
- Why necessary to take the course of probability and random process?

- Yi, Yung (이융)
- Office: N1, 810
- <http://lanada.kaist.ac.kr>, [yiyung@kaist.edu](mailto:yiyung@kaist.edu)
- Computer Division
- A professor in KAIST EE since 2008
- Office hours: TBA

- A
  - B
  - C
- 
- Mailing list: ee210@lanada.kaist.ac.kr
    - Please use KLMS for the questions about the lecture contents
    - This mailing list can be used for individual issues

- <http://klms.kaist.ac.kr/>
- To download course materials
- To ask questions about everything
- To check your score on each homework/exam
- To see all the announcements about the class

- Introduction to Probability  
(2nd edition)
  - MIT course textbook
  - Dimitri P. Bertsekas and John N. Tsitsiklis



- Three Parts
  - Part I: Fundamentals of Probability
  - Part II: Inference and Limit Theorems
  - Part III: Random Processes
- On-line lectures at MIT and EdX
  - MIT: <http://bit.ly/2PkvYdr>
  - EdX: <http://bit.ly/3pHmZRd>
  - You can find older urls (2006, 2010, 2013) for this lecture, where there are many useful resources (recitation problems, homework problems, old exam problems, etc)
  - My lecture slides: based on theirs, but largely modified/reorganized/edited in many places for KAIST students

- In-class quiz (sometimes)
- Basically, weekly homework, but often bi-weekly
- 3 Exams (2 mid-terms and 1 final)
- Class participation
- Grading portions: A (X%), B (Y%), C(Z%), D(W%), F . . .
- Online lectures due to COVID-19 may change how to grade.

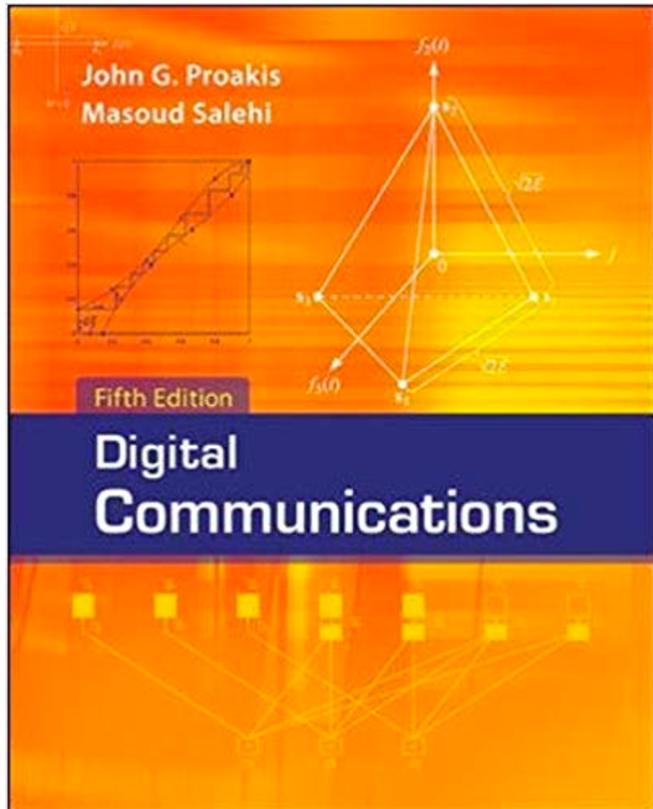
- Most should be via KLMS
  - Technical questions about lectures, homework, and etc
- Please DO NOT individually send emails to Prof. Yung Yi and TAs (or making calls or sending KakaoTalk msgs) about the technical questions (course contents, homework, etc)
  - All the questions need to be shared among the students.
  - TAs and Prof. Yung Yi will handle your questions as soon as possible.
  - But, you can send an email to Prof. Yung Yi for the things that need to be individually discussed.

Questions?

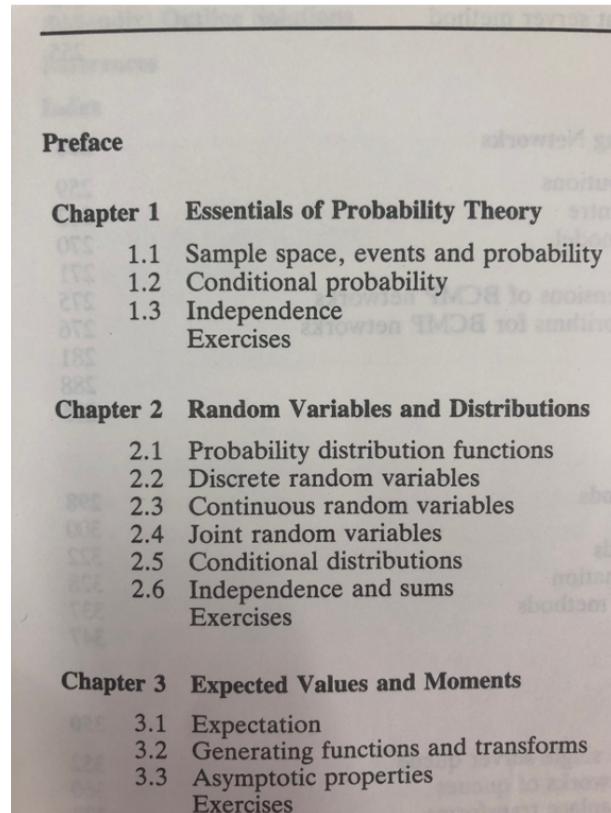
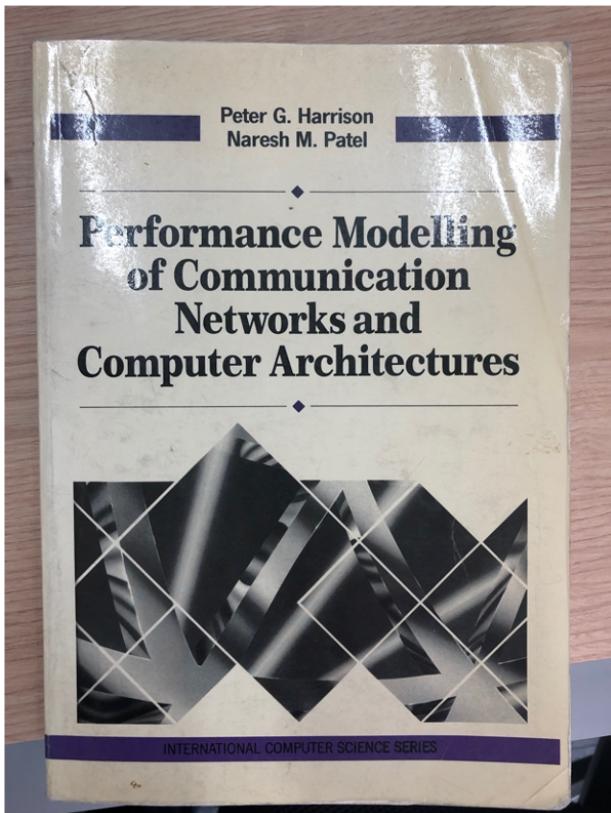
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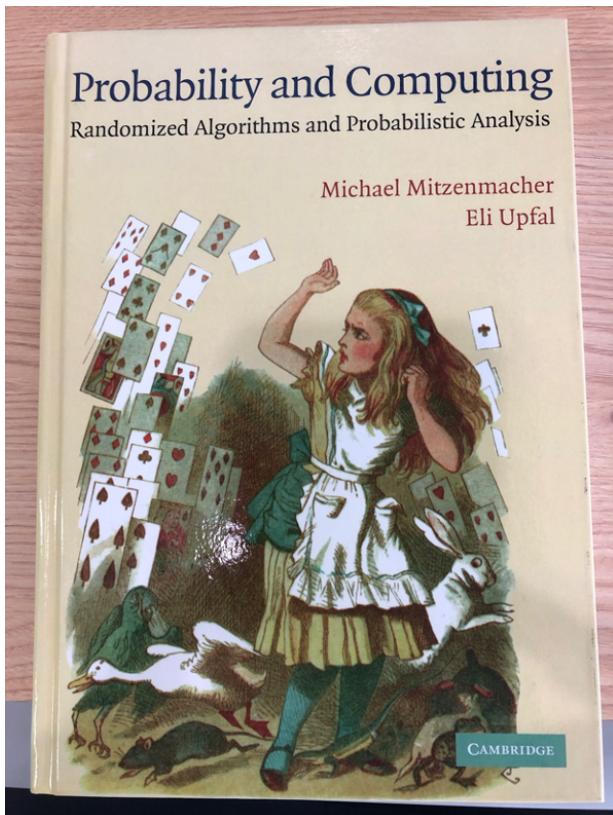
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- Assume that you are a designer of the following engineering systems. Good design?
  - a web server
  - a communication device like mobile phones
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- Many things are "probabilistic"
- Assume that you are a designer of the following engineering systems. Good design?
  - a web server
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- From an engineering point of view,
  - System input
  - Algorithms in systems
  - Analysis of systems



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*Preface*

**1 Events and Probability**

- 1.1 Application: Verifying Polynomial Identities
- 1.2 Axioms of Probability
- 1.3 Application: Verifying Matrix Multiplication
- 1.4 Application: A Randomized Min-Cut Algorithm
- 1.5 Exercises

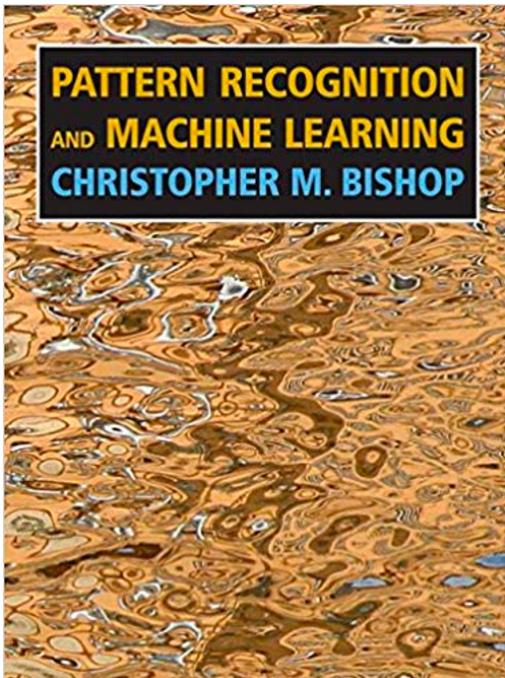
**2 Discrete Random Variables and Expectation**

- 2.1 Random Variables and Expectation
  - 2.1.1 Linearity of Expectations
  - 2.1.2 Jensen's Inequality
- 2.2 The Bernoulli and Binomial Random Variables
- 2.3 Conditional Expectation
- 2.4 The Geometric Distribution
  - 2.4.1 Example: Coupon Collector's Problem
- 2.5 Application: The Expected Run-Time of Quicksort
- 2.6 Exercises

**3 Moments and Deviations**

- 3.1 Markov's Inequality
- 3.2 Variance and Moments of a Random Variable
  - 3.2.1 Example: Variance of a Binomial Random Variable
- 3.3 Chebyshev's Inequality
  - 3.3.1 Example: Coupon Collector's Problem
- 3.4 Application: A Randomized Algorithm for Computing the
  - 3.4.1 The Algorithm
  - 3.4.2 Analysis of the Algorithm
- 3.5 Exercises

# Textbook: Machine Learning



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These days, every area in CS and EE is directly or indirectly related to machine learning!

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- We will take this exciting journey from the next lecture!

Questions?



@imagelife.xyz