

## Lecture 0: Introduction

Yi, Yung (이용)

EE210: Probability and Introductory Random Processes  
KAIST EE

August 27, 2022

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## Outline

- Course logistics
- Why this course?

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- Yi, Yung (이용)
- Office: N1, 810
- Homepage: <https://yung-web.github.io/home/>
- E-mail: [yiyung@kaist.edu](mailto:yiyung@kaist.edu)
- Computer Division
- In KAIST EE since 2008

## How to Run This Course

- All lecture videos have already been pre-recorded. Available in **YouTube**.
- **non-real-time online ( $\leq 50\%$ ) + real-time offline/online ( $\geq 50\%$ )**
- **non-real-time online:** Watch and study anytime and anywhere you like.
- **realtime offline/online:** Watch lecture videos in the classroom or in the zoom, with asking and answering questions.
- No attendance check!

# Accessing Lecture Videos and Slides



- Method 1:  
<https://yung-web.github.io/home/courses/probability.html>
- Method 2: (a) Type **Yung Yi** in the google, (b) visit his [GitHub homepage](#), (c) find the links on [Course](#).

Google search results for "yung yi":

- [yung yi - Google 검색](#)
- [\[전체\]](#)
- [이미지](#)
- [지도](#)
- [동영상](#)
- [뉴스](#)
- [더보기](#)
- [도구](#)

검색결과 약 20,600,000개 (0.62초)

도움말: 한국어 검색결과만 검색합니다. 경계설정에서 검색 언어를 지정할 수 있습니다.

<https://scholar.google.com/citations> ▾

**Yung Yi – Google Scholar**

Yung Yi, Professor of Electrical Engineering, KAIST. Verified email at kaist.edu · Homepage · Applied machine learning/computer networking/performance ...

<https://ee.kaist.ac.kr/~node/> ▾

**Yi, Yung – KAIST ELECTRICAL ENGINEERING**

Yi, Yung, Yung – Research Group: Computer · Research: Machine-learning based computer networking and communication systems, modeling, analysis, and developing ...

<https://yung-web.github.io/> ▾

**Yung Yi, KAIST – GitHub Pages**

2017.6.15. — Short Bio: Yung Yi received his B.S. and M.S. in the School of Computer Science and Engineering from Seoul National University, ...  
이 페이지를 여러 번 방문했습니다. 최근 방문 날짜: 21.8.23

<https://openreview.net/profile?id=Yung.Yii> ▾

**Yung Yi | OpenReview**

Korea Advanced Institute of Science and Technology · Names · Emails · Personal Links · Education & Career History · Advisors, Relations & Conflicts · Expertise.

<https://dl.acm.org/profile>

**Yung Yi – Home – ACM Digital Library**

Mobile networks Wireless access networks Machine learning Network protocols Sequential decision making Design and analysis of algorithms Local area networks ...



Short Bio: Yung Yi received his B.S. and the M.S. in the School of Computer Science and Engineering from Seoul National University in 1997 and 1999, respectively, and his Ph.D. in the Department of Electrical and Computer Engineering at the University of Texas at Austin in 2006. From 2006 to 2008, he was a post-doctoral research associate in the Department of Electrical Engineering at KAIST, South Korea. He is a KAIST Chair Full professor at the Department of Electrical Engineering at KAIST, South Korea. His current research interests include machine learning, design and analysis of wired/wireless networking systems. He was the recipient of two best paper awards at SECON 2013 and ACM MobiHoc 2013. He was the co-recipient of IEEE William R. Bennett Award, 2016.

LanADA (Laboratory of Network Architecture, Design, and Analysis)

LanADA is a research group which I currently lead. Currently, we do not hire new graduate students.

Students advised (PhD)

1. Jinsung Lee, 2012, Postdoc at U. of Colorado
2. Jihyeong Lee, 2014, Sony Ericsson, Sweden
3. Joohyun Lee, 2014, Hanyang Univ.
4. Hanjin Park, 2015, National Security Research Institute
5. Donghyun Kim, 2016, Naver
6. Sochwan Lee, 2016, ETRI
7. Jihyeong Lee, 2016, SK Telecom
8. Hyeyoung Jeong, 2016, Dongduk Univ.
9. Jungseok Oh, 2017, POSTECH
10. Hyojeong Lee, 2017, Samsung

Education

- Ph.D. Dept. of Electrical and Computer Engineering, University of Texas at Austin, 2006
- M.S. Dept. of Computer Science and Engineering, Seoul National University, 1999
- B.S. Dept. of Computer Science and Engineering, Seoul National University, 1997

Position

- KAIST Chair Professor (KAIST 총장(校長)) Dept. of Electrical Engineering, KAIST, 2007 – Current
- Full Professor, Dept. of Electrical Engineering, KAIST, 2018.2 – Current
- Associate Professor, Dept. of Electrical Engineering, KAIST, 2011.8 – 2018.2
- Assistant Professor, Dept. of Electrical Engineering, KAIST, 2008.8 – 2011.8
- Postdoctoral Research Associate, Dept. of Electrical Engineering Princeton University, 2006.8 – 2008.8

Courses

- Probability and Introductory Random Process (video included), Undergraduate
- Data Structures for Electrical Engineers, Undergraduate
- Mathematics for Machine learning, Undergraduate
- Computer Network, Undergraduate
- Complex Network Analysis: Epidemics and Rumours (video included), Graduate

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Memor:  
  
2020 Spring  
Office Hou

August 27, 2022

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# Using KLMS and Campuswire



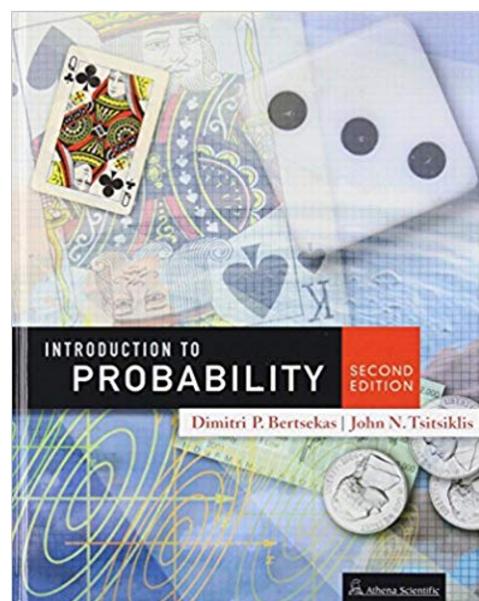
- KLMS:** All notifications and announcements (also sent to you via email)
- KLMS:** Questions about course logistics
- KLMS:** Homework upload
- KLMS:** Score upload and all the grade-related things
- Campuswire:** Questions about course contents (should be in English)
- NOT individual emails to the instructor or the TAs
- Emails to the instructor, Prof. Yung Yi, are allowed for handling private situations.

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## Textbook

- Introduction to Probability  
(2nd edition)
  - MIT course textbook
  - Dimitri P. Bertsekas and John N. Tsitsiklis
- You can order it from Yes24, Aladin, Kyobo
  - Yes24: <http://www.yes24.com/Product/Goods/3995311>
  - Aladin: <https://www.aladin.co.kr/shop/wproduct.aspx?ItemId=12945615>
  - Kyobo: <http://www.kyobobook.co.kr/product/detailViewEng.laf?ejkGb=ENG&mallGb=ENG&barcode=9781886529380&orderClick=LAG&Kc=>



- <http://athenasc.com/probbook.html>
- **Solutions for all problems** (so you have all solutions for your homework)
- Links to the old MIT courses
- You can find the urls (2006, 2010, 2013) for the MIT lectures based on the same textbook, where there are many useful resources (recitation problems, homework problems, old exam problems, etc)
- Some of my lecture slides are based on theirs, but my slides are largely modified/reorganized/edited in many places for our purpose.

## Course Contents (Guided Schedule for Your Study)

1. Probabilistic model (0.5 week)
2. Conditioning and Independence (0.5 week)
3. Random Variable, Part I (Discrete Random Variable) (1.5 week)
4. Random Variable, Part II (Continuous Random Variable) (1.5 week)
5. Random Variable, Part III (Advanced Topic on Random Variable) (1.5 week)
6. Limit of Scaled Sum of Random Variables: Central Limit Theorem and Weak Law of Large Numbers (1.5 week)
7. Random Process: Bernoulli and Poisson Processes (2 week)
8. Random Process: Markov Chain (2 week)
9. Introduction to Statistical Inference (2 week)

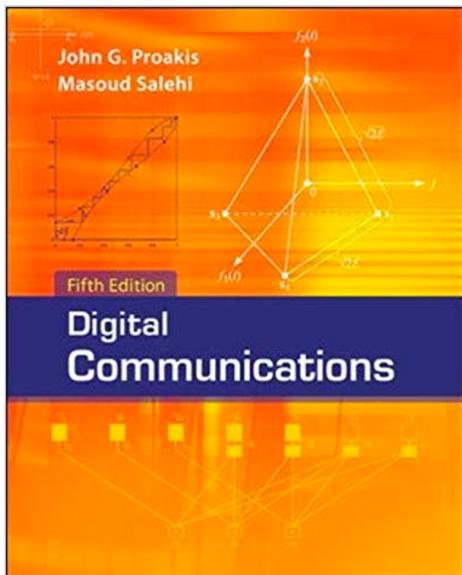
- 2 Exams (mid-term and final)
- Homeworks
  - All problems are from exercise problems in the textbook.
  - We do NOT check whether you copy your solution from the problem solutions or not.
- 9 Homeworks for each of 9 chapters.

- Read **ALL** the emails.
- Need to buy the textbook?
  - Strongly recommend it. Taking a course is NOT just solving mid-term and final exam problems and getting a good grade.
- OK not to be present in the classroom? Yes.
- OK that my homework solutions is same as those in the solutions book? Yes.
- Can I ask for a personal meeting to ask questions or get other general advices?  
Sure. Send me an email.

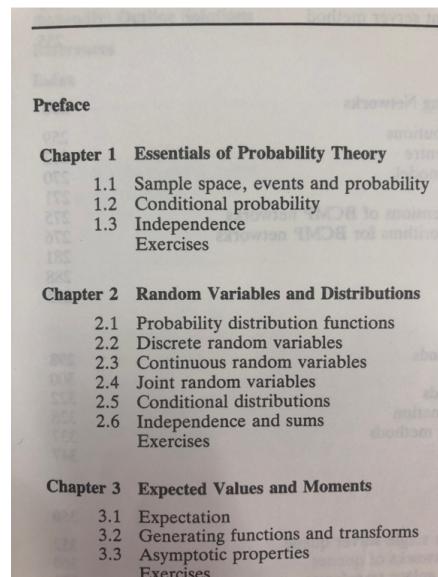
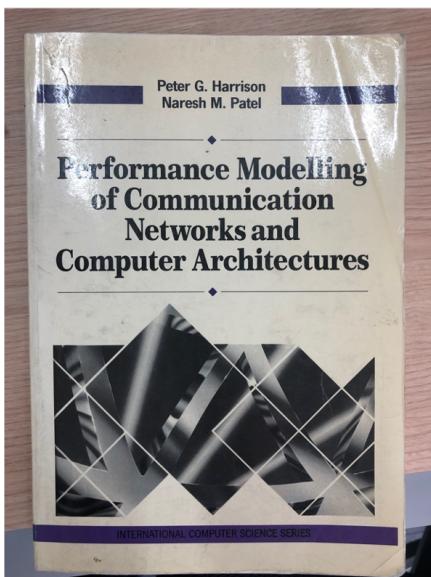
# Questions?

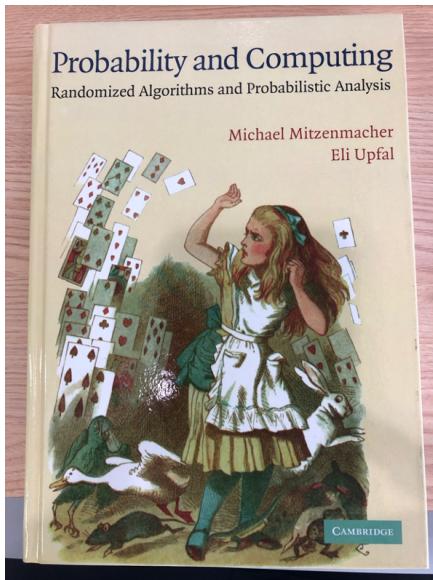
## Why Probability?

- Many things are "probabilistic"
- Assume that you are a designer of the following engineering systems. Good design?
  - a web server
  - a communication device like mobile phones
  - an AI-based image classifier
- From an engineering point of view,
  - System input
  - Algorithms in systems
  - Analysis of systems

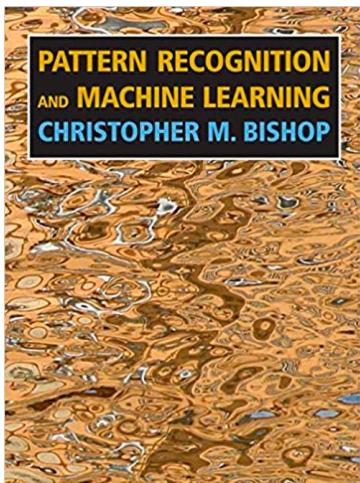


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These days, every area in CS and EE is directly or indirectly related to machine learning!

- Designer's perspective?
- In the year of 2022, suppose that unfortunately there is no theory of mathematically studying the *uncertainty* of some phenomena, events, etc.
- You have to design such a theory called "probability". How are you going to do it? Where are you going to start?
- You just have other basic mathematical theories such as set theory.
- You need to get used to the *English terms* on probability (e.g., sample space = 표본공간, probability density function = 확률밀도함수).
- We will take this exciting journey from the next lecture!

Questions?

