

AI and Deep Learning

# Multi-Layer Neural Networks and Non-linear Decision Boundary

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# Agenda

- Learning revisited
- Place holder
- Linear decision boundary and XOR problem
- Multi-layer and non-linearity
- Complex boundary as you wish

# Learning

- ① Parameters( $w, b$ ) initialization randomly
- ② Building computation graph of  $E$  by TensorFlow
- ③ Foreword propagation by putting values into the graph and calculate  $E$
- ④ Back-propagation to get the influence of  $w, b$  on the error (applying chain rules)
- ⑤ Update  $w, b$  to adjust a decision boundary
- ⑥ go to ③

# Learning

```
import tensorflow as tf
#----- training data
x_data = [-2, -1, 1, 2]
y_data = [0, 0, 1, 1]
#----- a neuron
w = tf.Variable(tf.random_normal([1])) ①
hypo = tf.sigmoid(x_data * w)
#----- learning
cost = -tf.reduce_mean(y_data * tf.log(hypo) +
                        tf.subtract(1., y_data) * tf.log(tf.subtract(1., hypo)))
train =
tf.train.GradientDescentOptimizer(learning_rate=0.01).
minimize(cost)
```

# Learning

```
sess = tf.Session()  
sess.run(tf.global_variables_initializer()) ①
```

```
②  
for i in range(1001):  
    sess.run(train) ③④⑤
```

```
        if i % 100 == 0:  
            print( ' w: ' , sess.run(w), ' cost: ' , sess.run(cost))
```

Learning finished after  
1001 times updates

```
#----- test (classification)  
x_data = [-2, 4]  
print(sess.run(hypo))
```

# Testing new data

- After learning,
- a neuron can classify new input data correctly.

`x_data = [-2, -1, 1, 2]`

```
#----- test (classification)
x_data = [-2, 4]
print(sess.run(hypo))
```

- **Failure!**
- Data is set only one time when the graph is created.
- Still old data was used.
- No feeding the new data into the predefined computational graph

# Place Holder

- **Marking** certain places in a computational graph
- and then **replace** it with real data when it runs (is evaluated).

`sess.run ( )`

# Place Holder

```
import tensorflow as tf
```

```
#----- training data
```

```
x_data = [[-2], [-1], [1], [2]]
```

```
y_data = [[0], [0], [1], [1]]
```

```
X = tf.placeholder (tf.float32)
```

```
Y = tf.placeholder (tf.float32)
```

```
#----- a neuron
```

```
w = tf.Variable (tf.random_normal([1]))
```

```
hypo = tf.sigmoid(X * w)
```

1. Place holders : X, Y
2.  $x\_data \rightarrow X$ ,  $y\_data \rightarrow Y$
3. Feeding real data when hypo, cost, and train operations are executed.



# Place Holder

```
#----- learning
```

```
cost = -tf.reduce_mean(Y * tf.log(hypo) +  
    tf.subtract(1., Y) * tf.log(tf.subtract(1., hypo)))
```

```
train =
```

```
tf.train.GradientDescentOptimizer(learning_rate=0.01).minimize(cost)
```

```
sess = tf.Session()
```

```
sess.run(tf.global_variables_initializer())
```

```
for i in range(1001):
```

```
    sess.run(train, feed_dict={X:x_data, Y:y_data})
```

```
    if i % 100 == 0:
```

```
        print(sess.run(w), sess.run(cost, feed_dict={X:x_data, Y:y_data}))
```

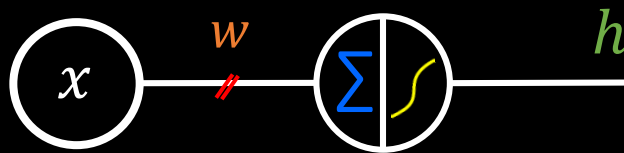
# Place Holder

```
#----- testing(classification)
x_data = [-2, 4]
result = sess.run(hypo, feed_dict={X: x_data})
print(result)
```

# Lab 15.py

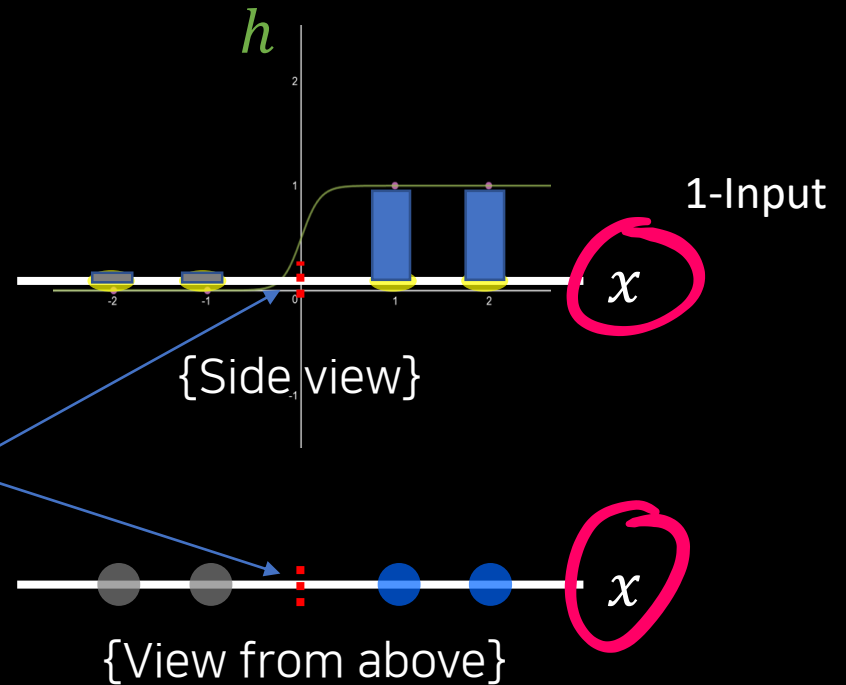
- Classification into one of **four classes**
- Using placeholders

# 1-Input Neuron

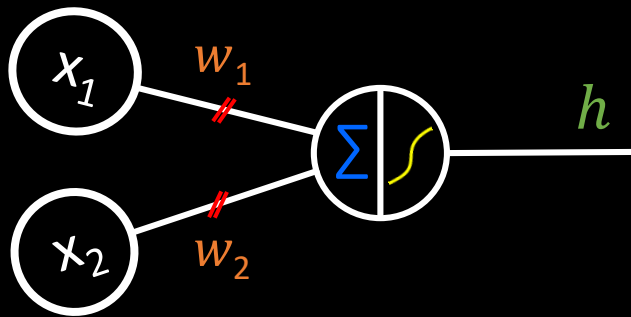


Decision boundary : Value

$$w \cdot x = 0$$
$$x = 0$$

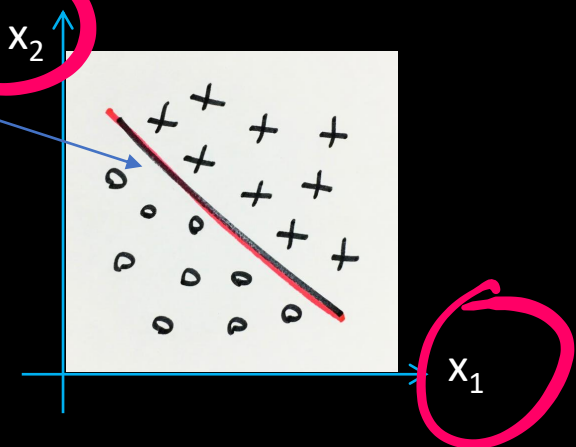
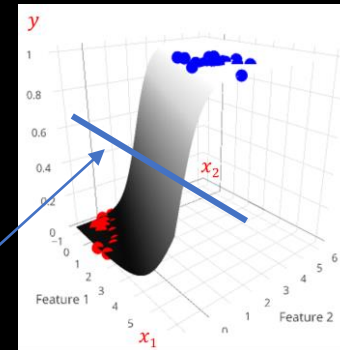


# 2-Input Neuron

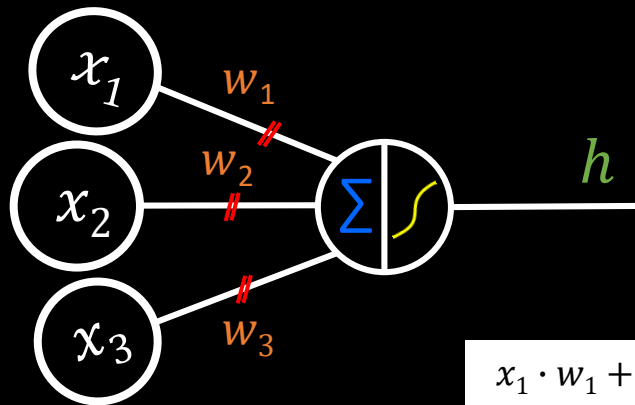


Decision boundary : Line

$$x_1 \cdot w_1 + x_2 \cdot w_2 = 0$$

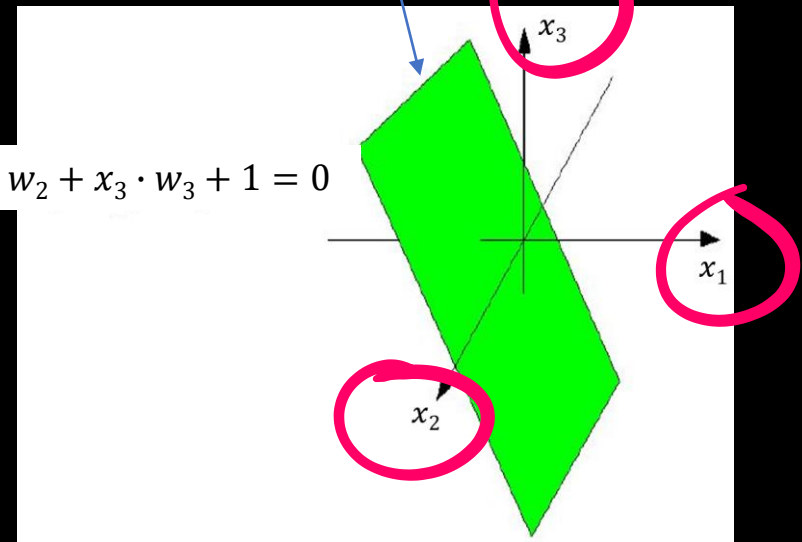


# 3-Input Neuron



Decision boundary : Plane

$$x_1 \cdot w_1 + x_2 \cdot w_2 + x_3 \cdot w_3 + 1 = 0$$



# More than 4 inputs?

$$x_1w_1 + x_2w_2 + x_3w_3 + x_4w_4 + b = 0$$

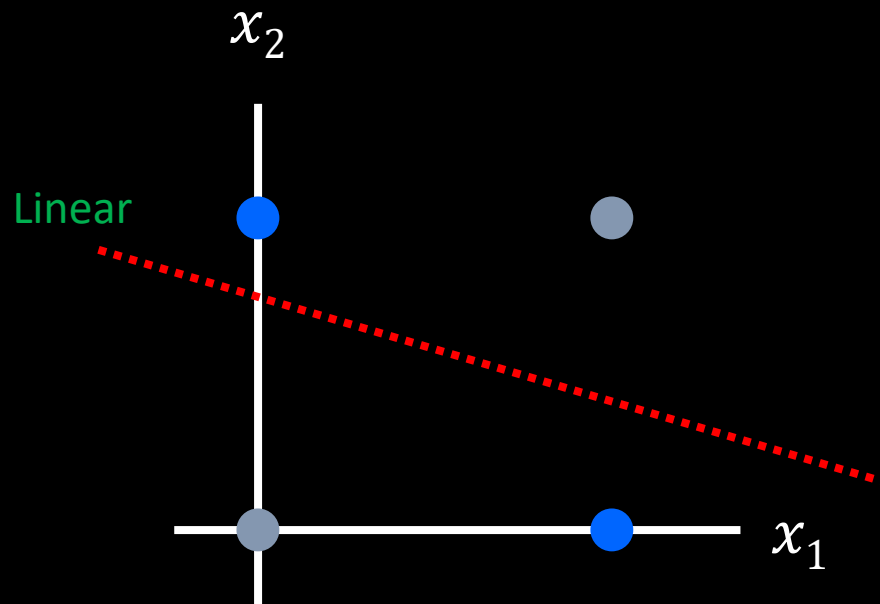
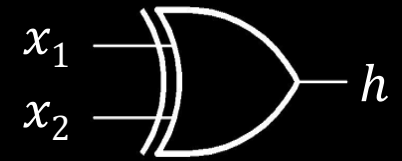
→ hyperplane

# Linear Decision Boundary

(value, line, plane, hyperplane)



# XOR



$x_1$	$x_2$	$h$
0	0	0
0	1	1
1	0	1
1	1	0

View from above

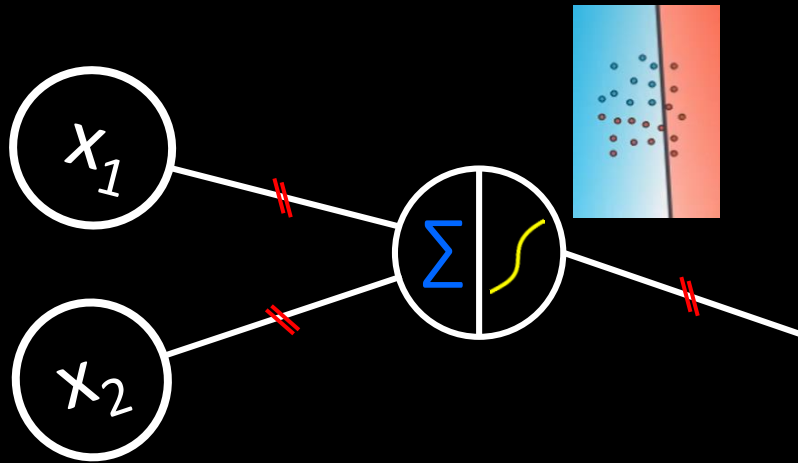
# XOR

- Number of class : 2
- 1 decision boundary for 2-class classification
- **Impossible** to classify using a linear decision boundary

# Lab 16.py

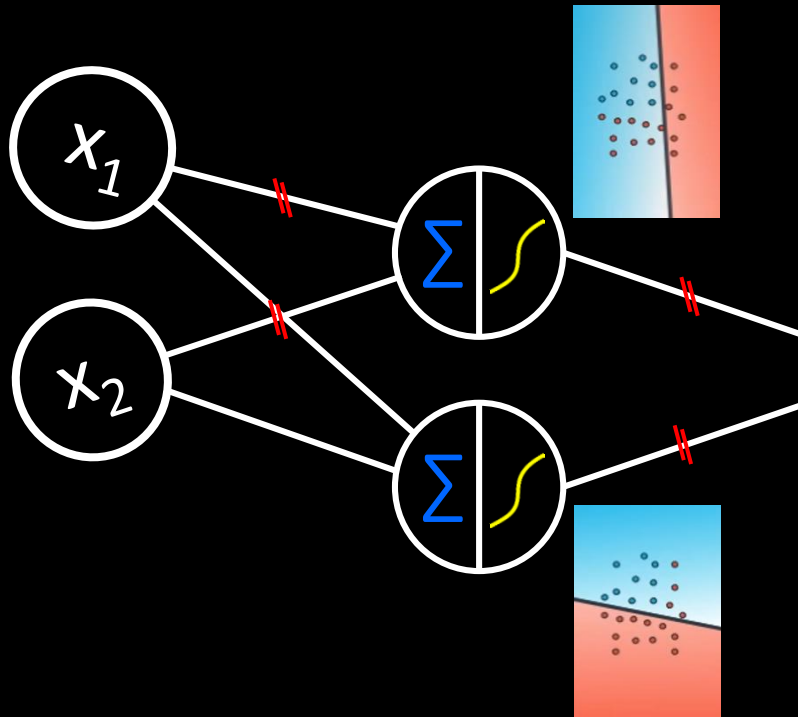
- XOR problem
- A neuron, 1 linear decision boundary
- Cannot be solved!

# How to solve



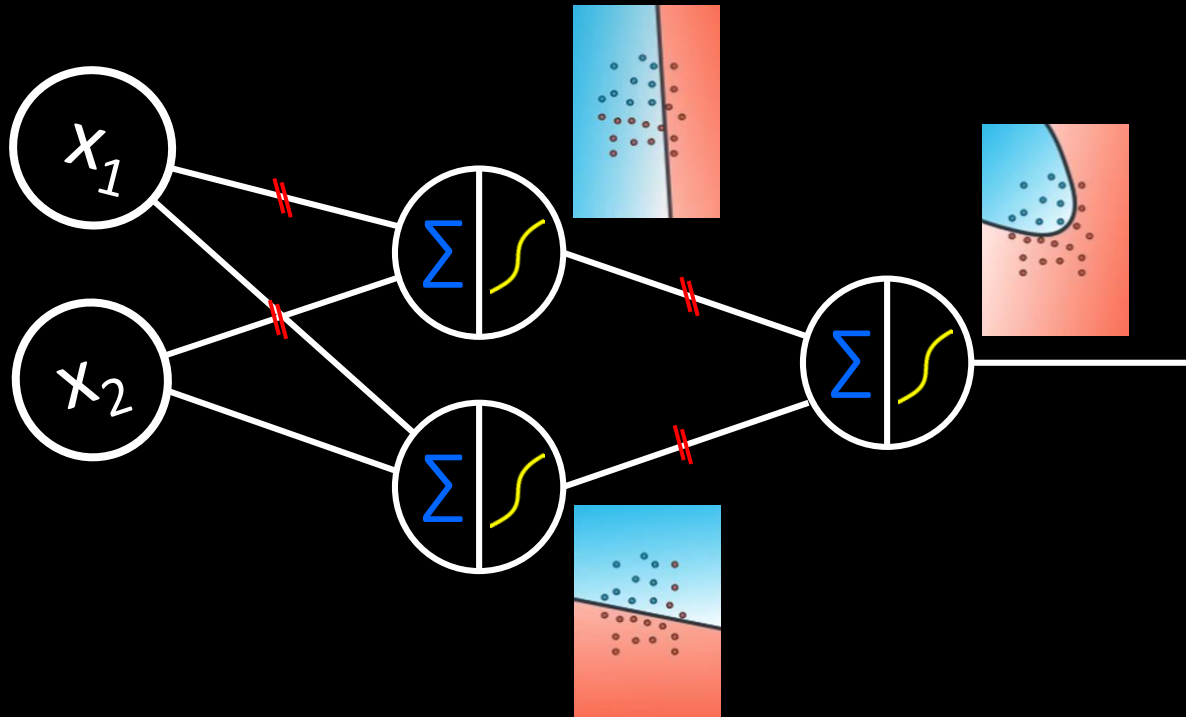
by Luis Serrano, A friendly introduction to Deep Learning, UDACITY

# How to solve



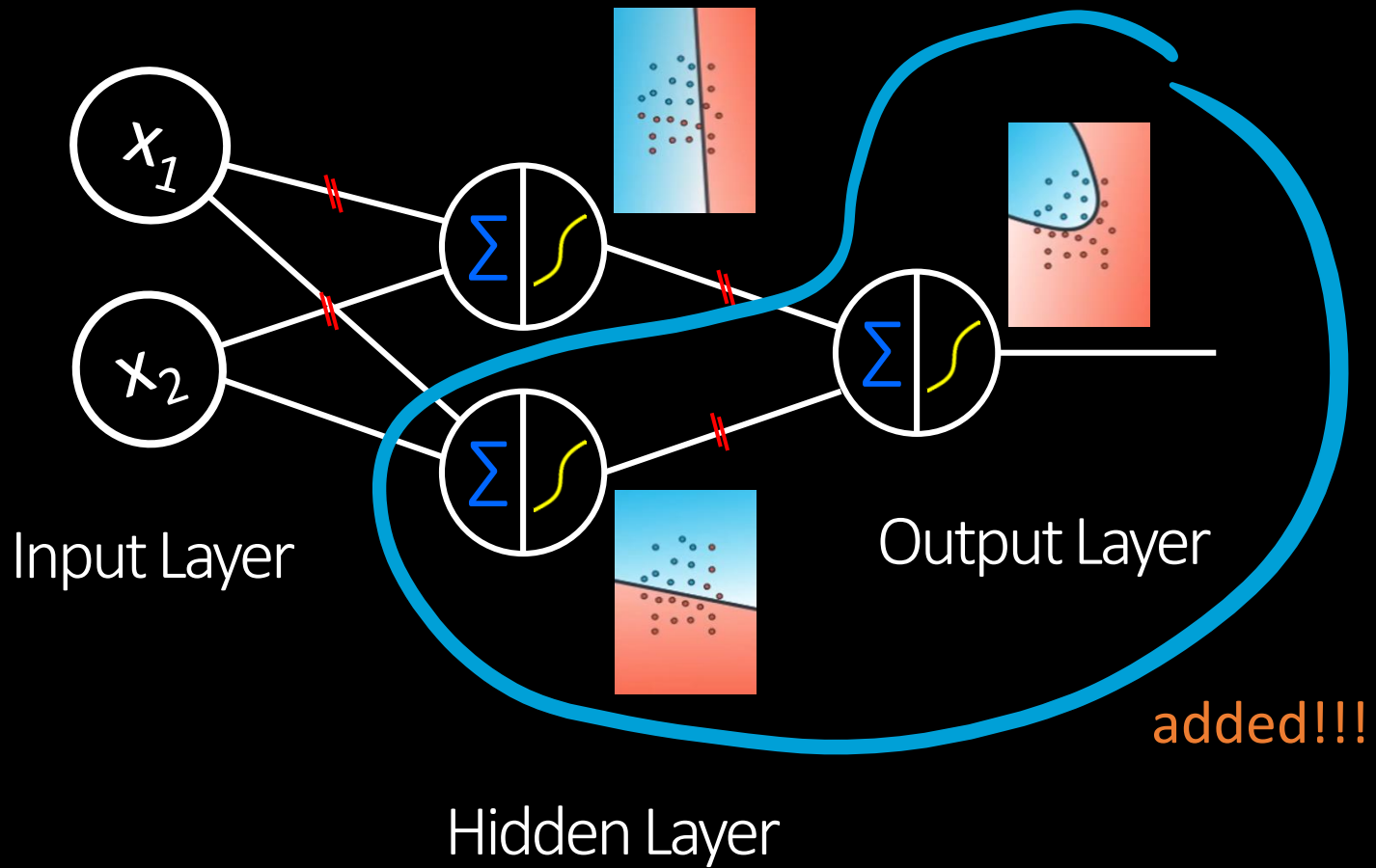
by Luis Serrano, A friendly introduction to Deep Learning, UDACITY

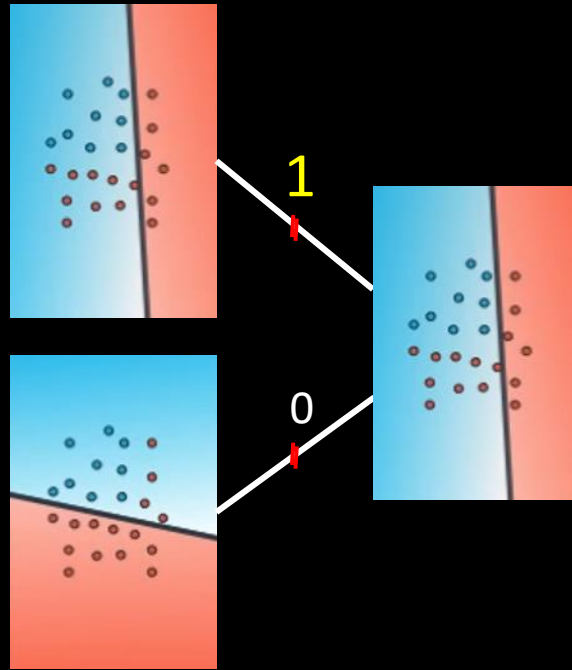
# How to solve



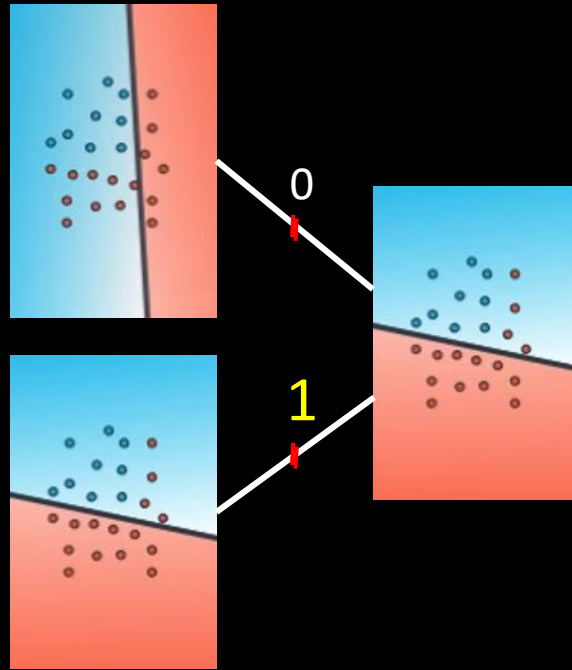
by Luis Serrano, A friendly introduction to Deep Learning, UDACITY

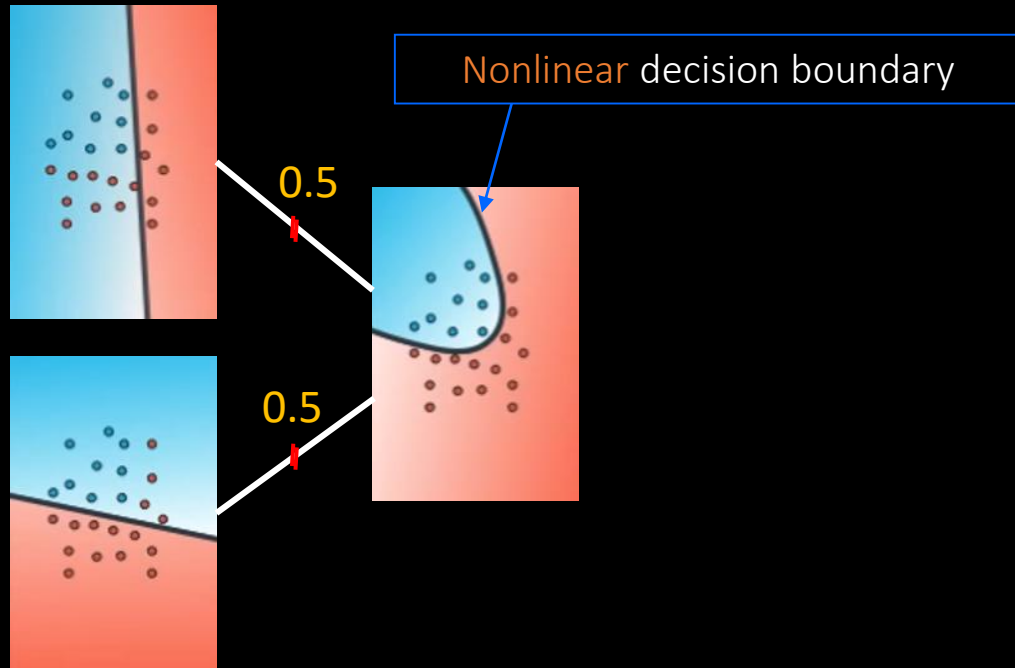
# 3-layer Neural Network





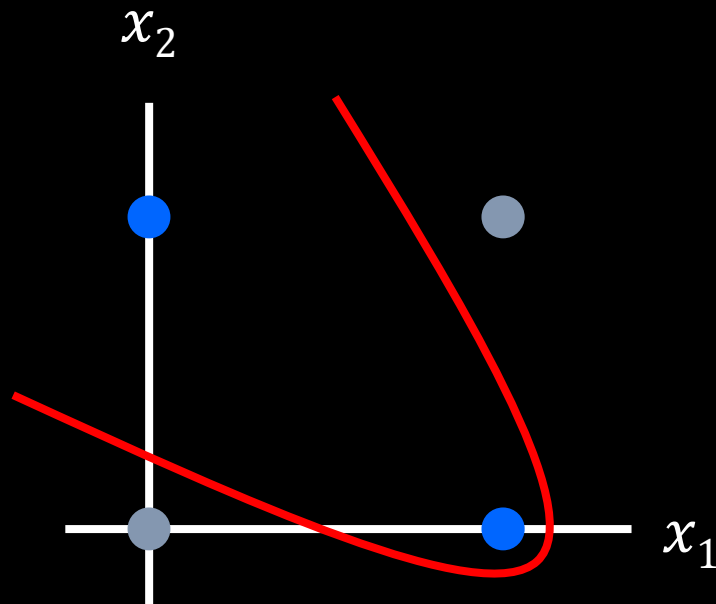






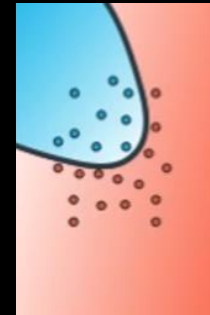
3-layer NN for nonlinear  
decision boundary

# XOR



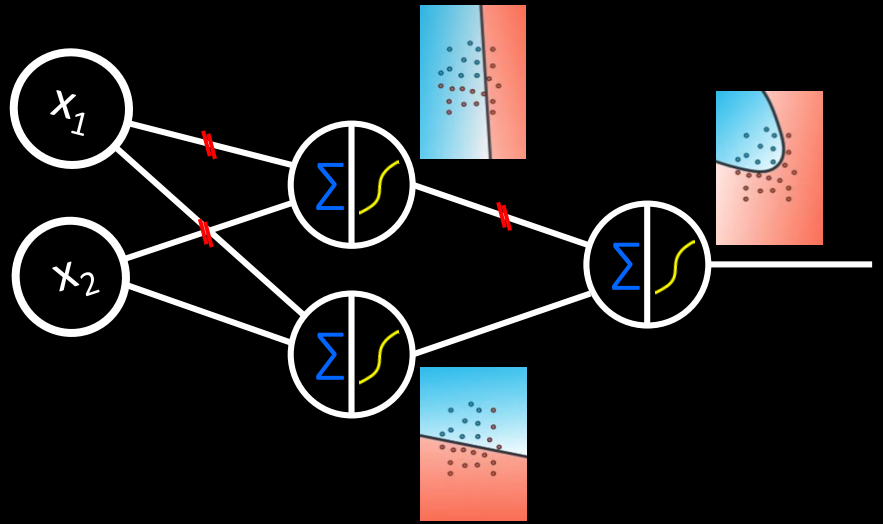
View from above

View from above

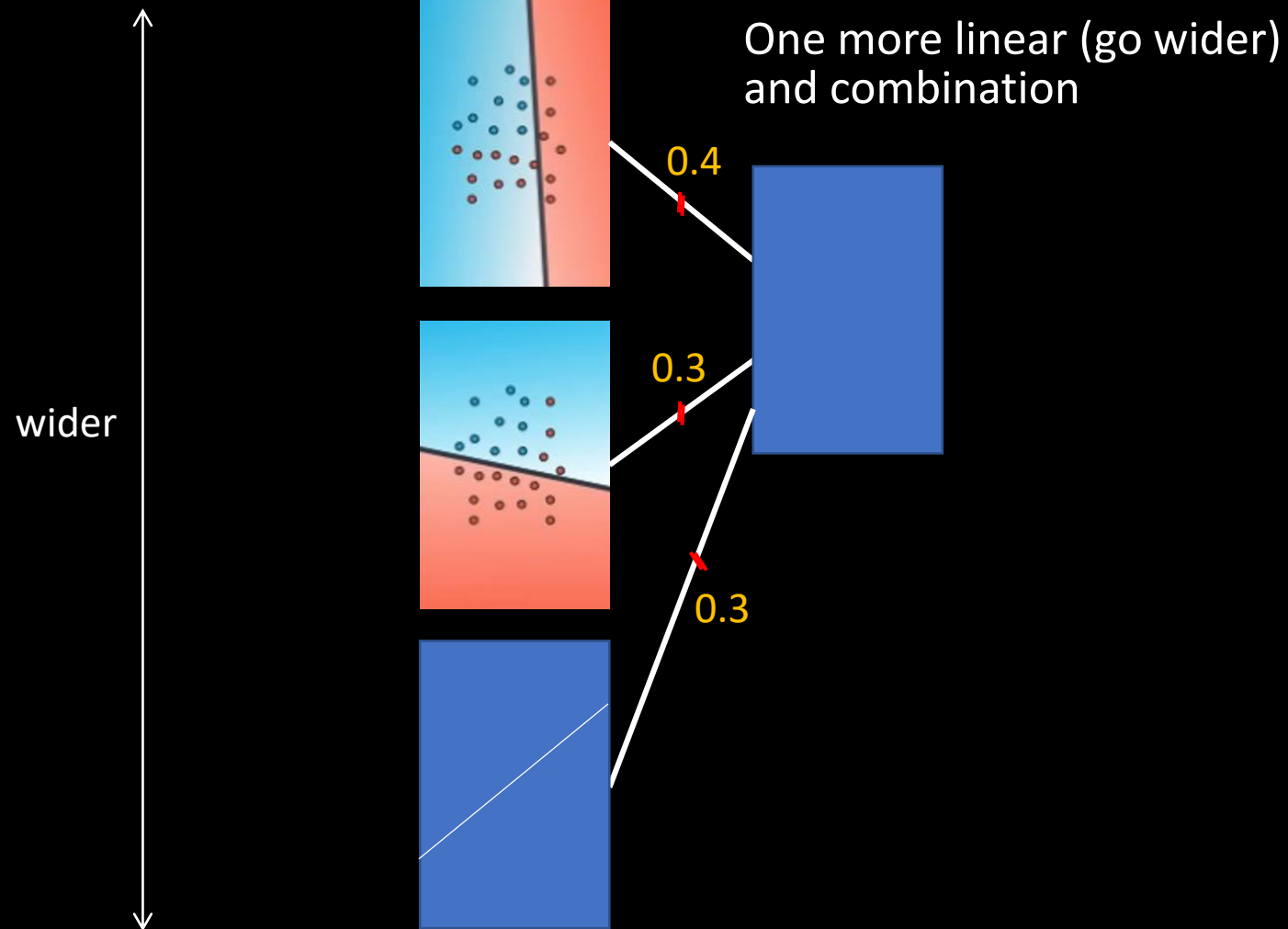


Side view

# Lab 17.py

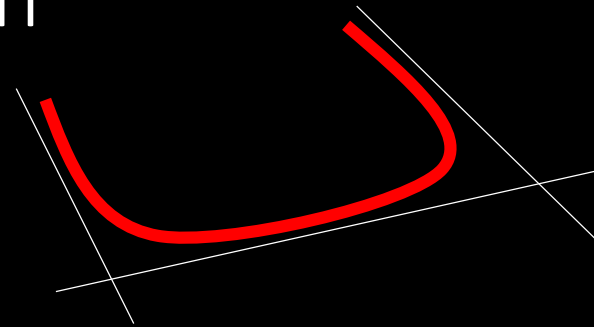


- Solving XOR gate problem using 3-layer neural network
- The way to create non-linear decision boundary



# Nonlinear Decision Boundary

- Combination of **three** linear decision boundaries

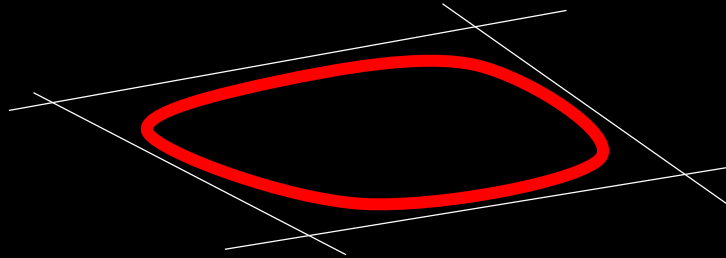






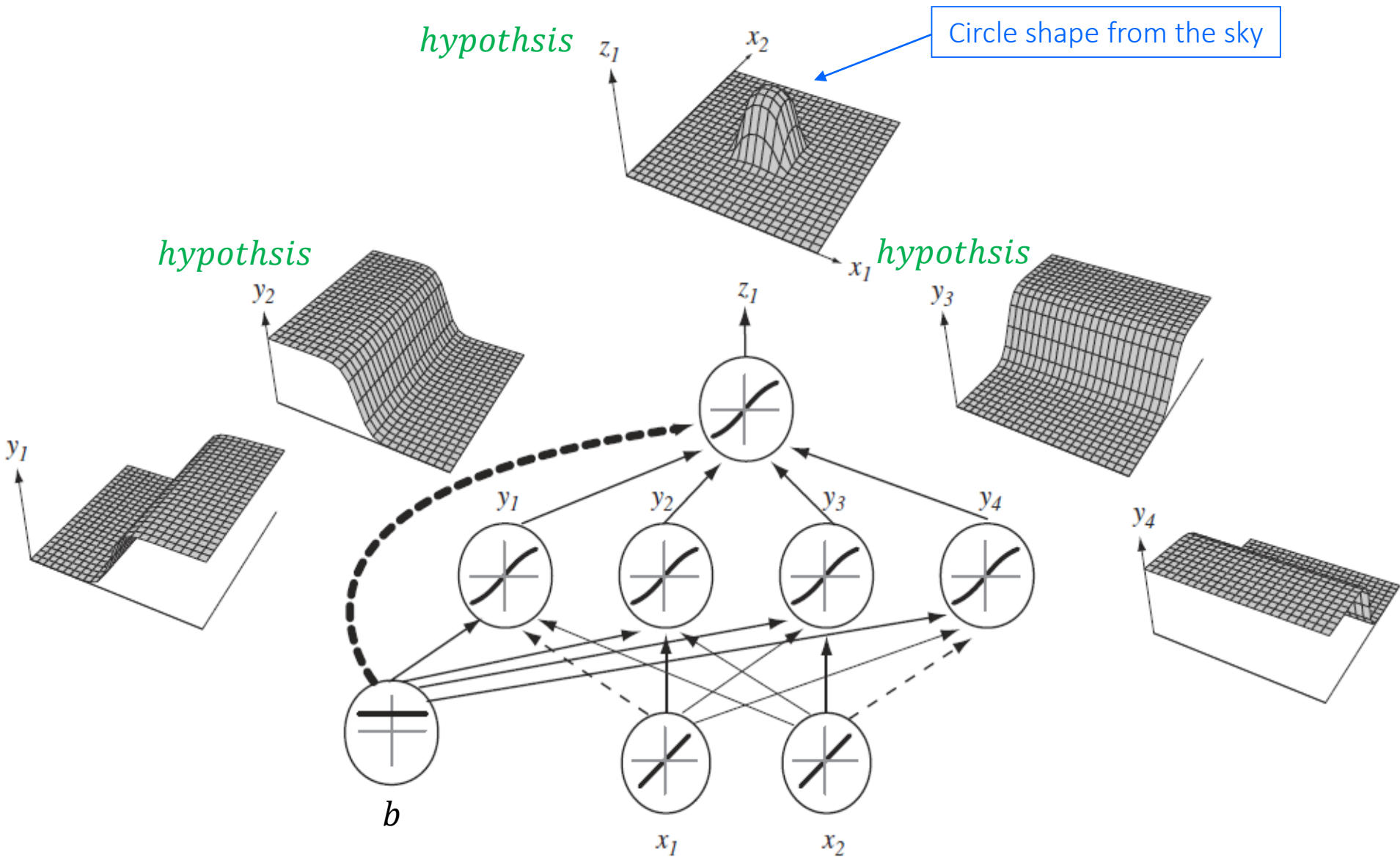
# Nonlinear Decision Boundary

- Merging **four** linear decision boundaries



View from above

# Nonlinear Decision Boundary





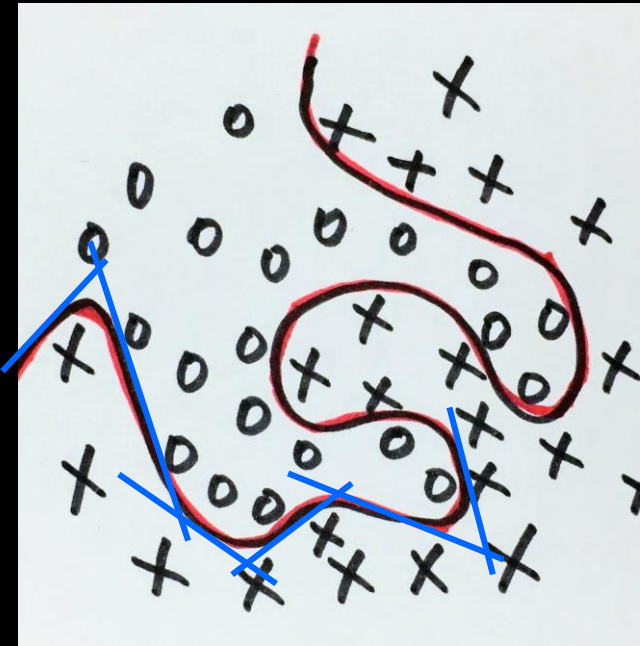
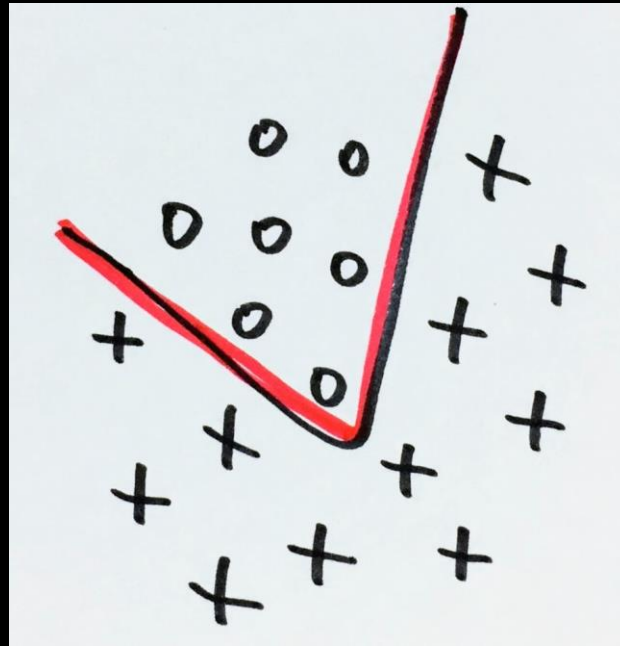
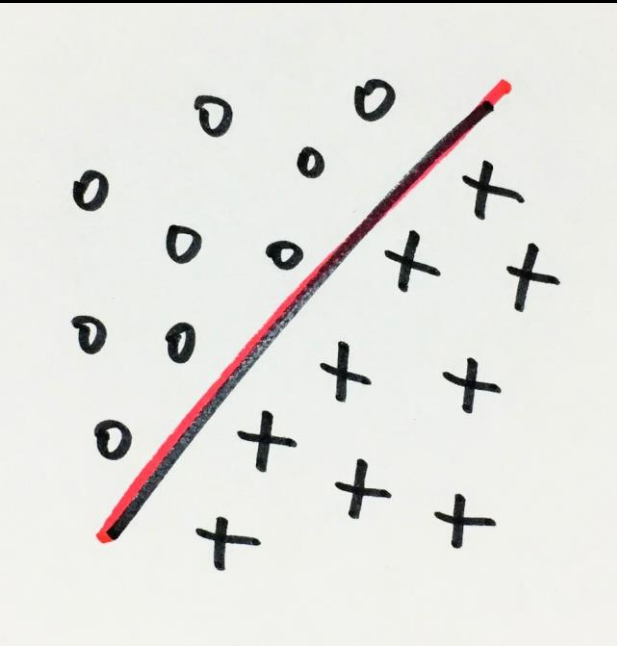
View from above



Side view

# As you wish (2 classes)

$\chi^2$

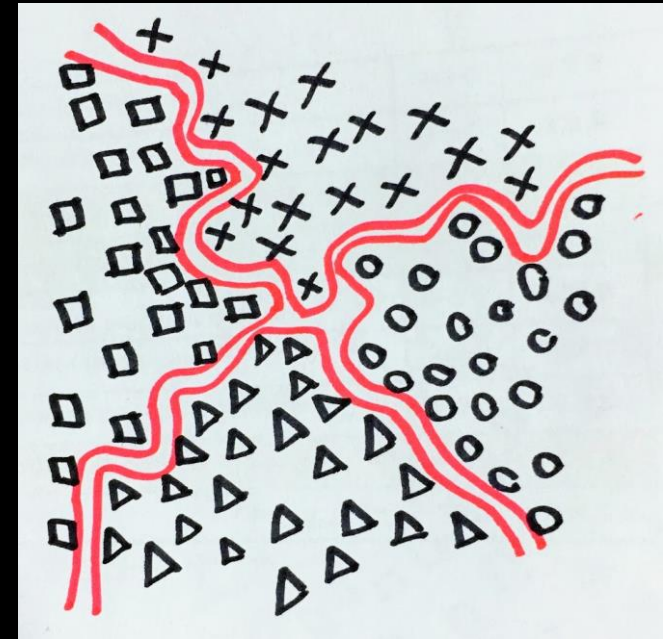
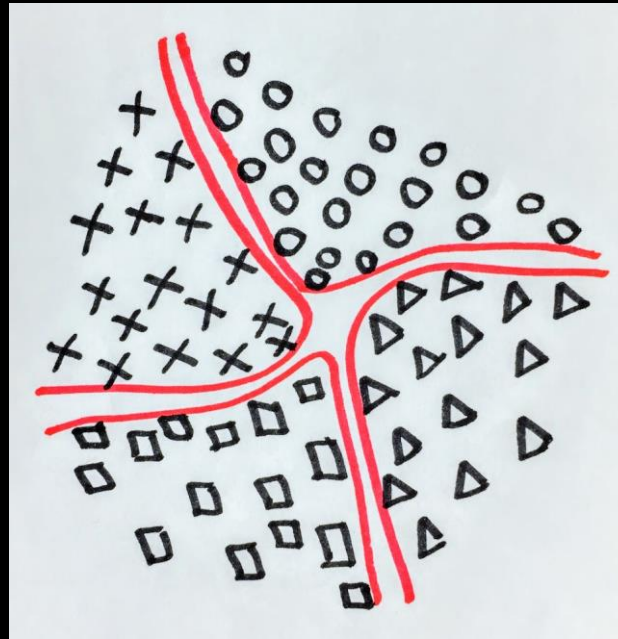
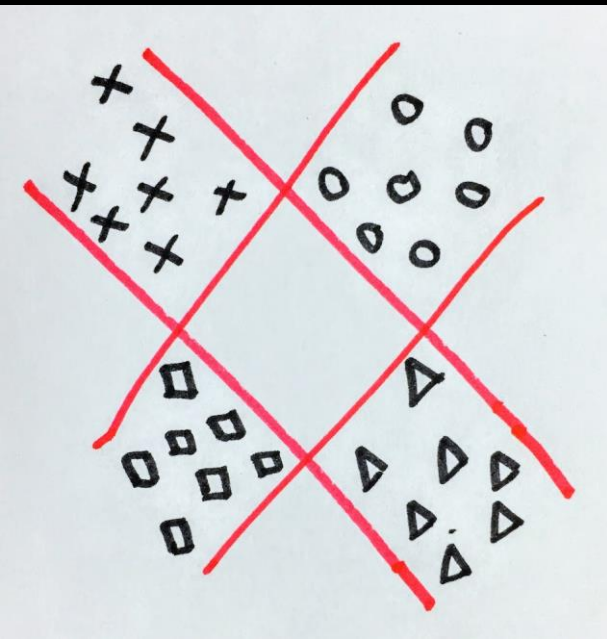


$\chi_1$

View from above



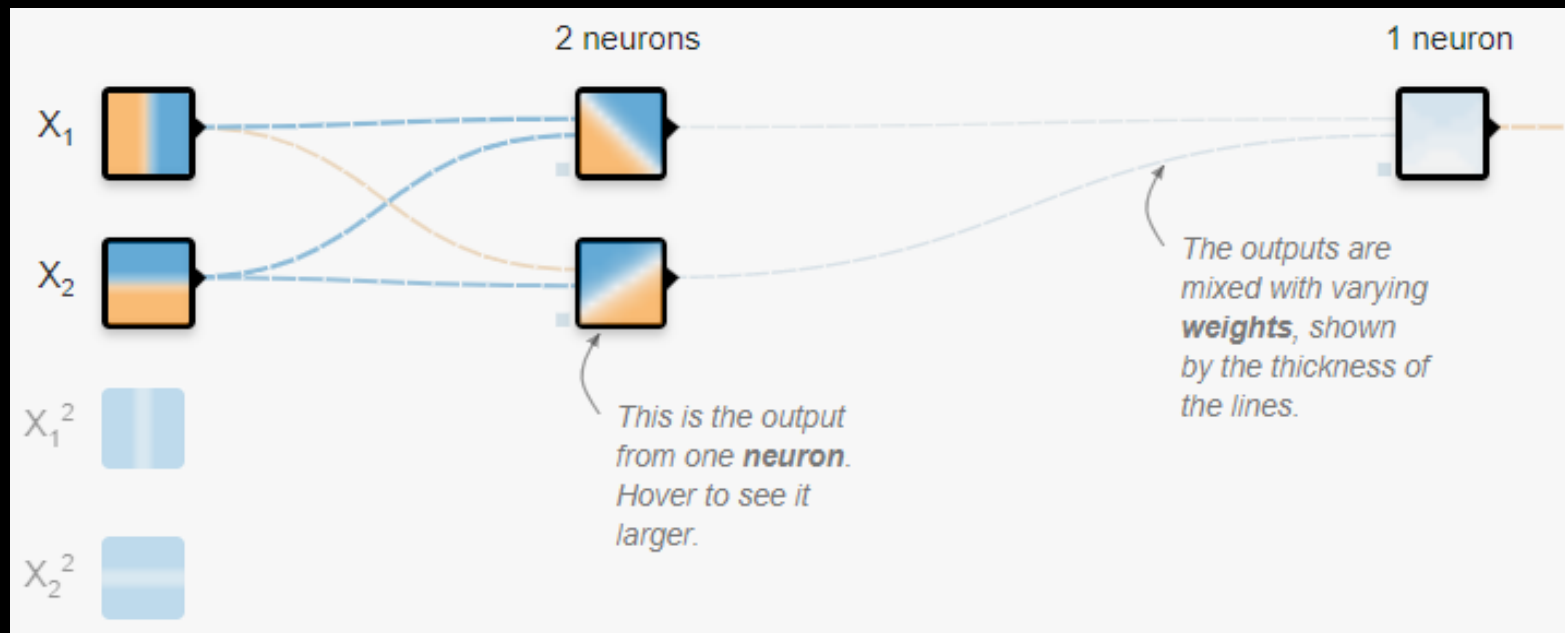
# As you wish (4 classes)



From the above

More neurons, more complex (detail)  
decision boundary

<http://playground.tensorflow.org>



# As you wish

## go wider & deeper

- to make more complex nonlinear decision boundaries.
- We can classify anything we imagine.



# The way of machine learning

- learning over and over again just like human being
- If it misrecognizes, just say 'Nope, you were wrong', which makes it update its weights to do better next time.
- Try it over and over again just like a child.

# Learning or Programming?

“This (machine learning) is the next transformation...the programming paradigm is changing. Instead of programming a computer, you teach a computer to learn something and it does what you want”

— Eric Schmidt, Google



# Change of Paradigm

Not programming,  
but data-driven learning  
(parameter tuning)