

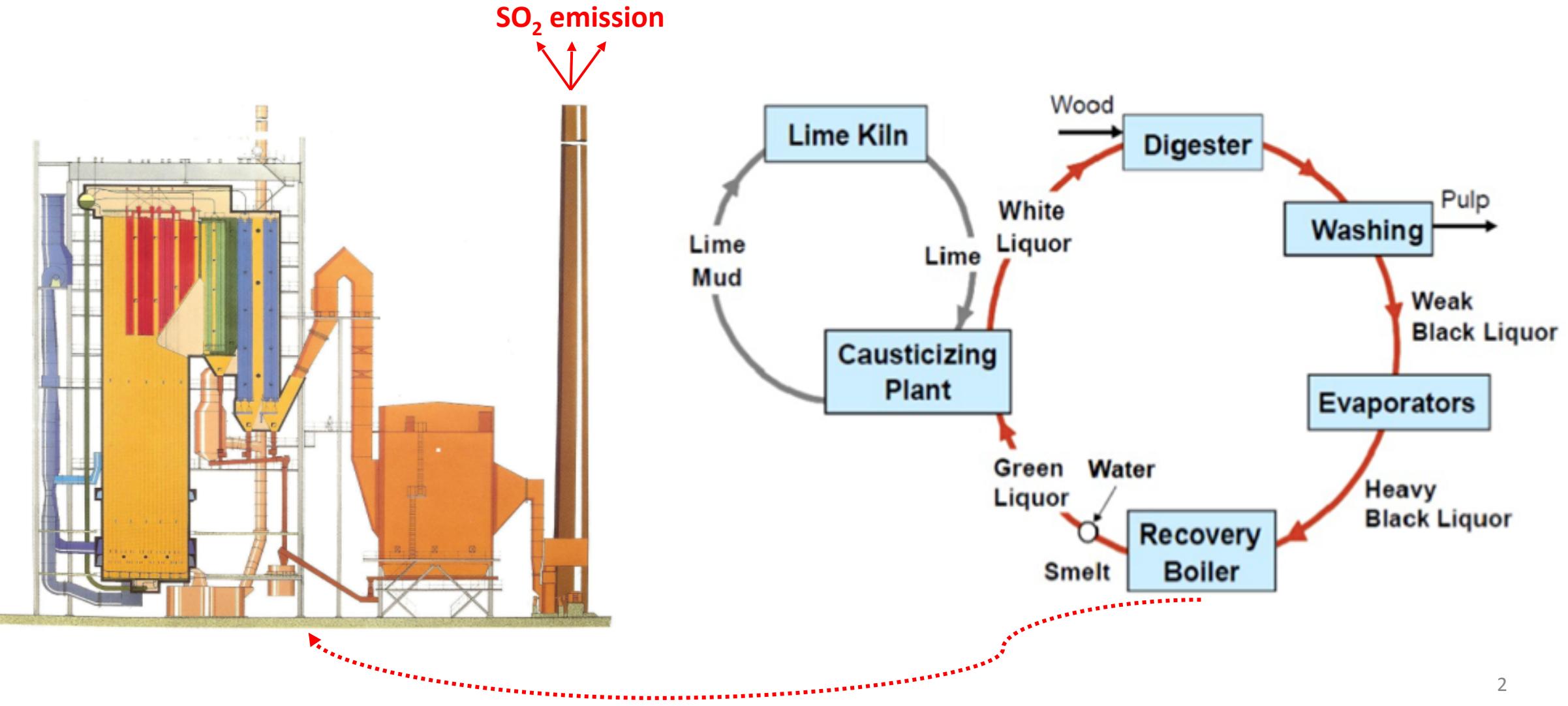


# Root Cause Analysis for SO<sub>2</sub> Emission in Kraft Recovery Boiler

Daniel Yung Chi Cho

Dec 6, 2018

# Recovery Cycle



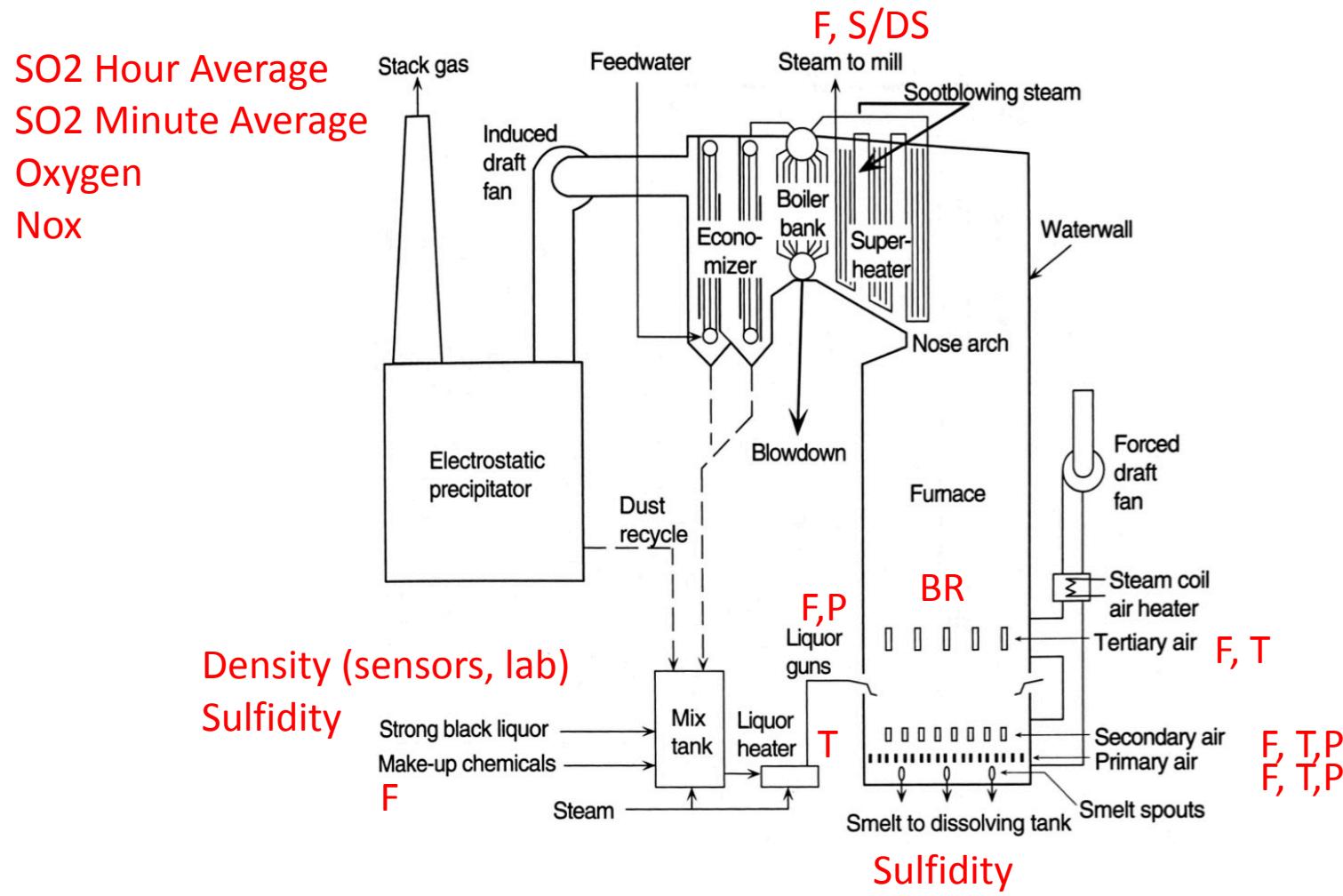
# Problem Statement

- High sulfur dioxide emission at recovery boiler at a pulp mill.
- Sulfur dioxide is a regulated pollutant.
- Company faces penalty for emission beyond the limit.

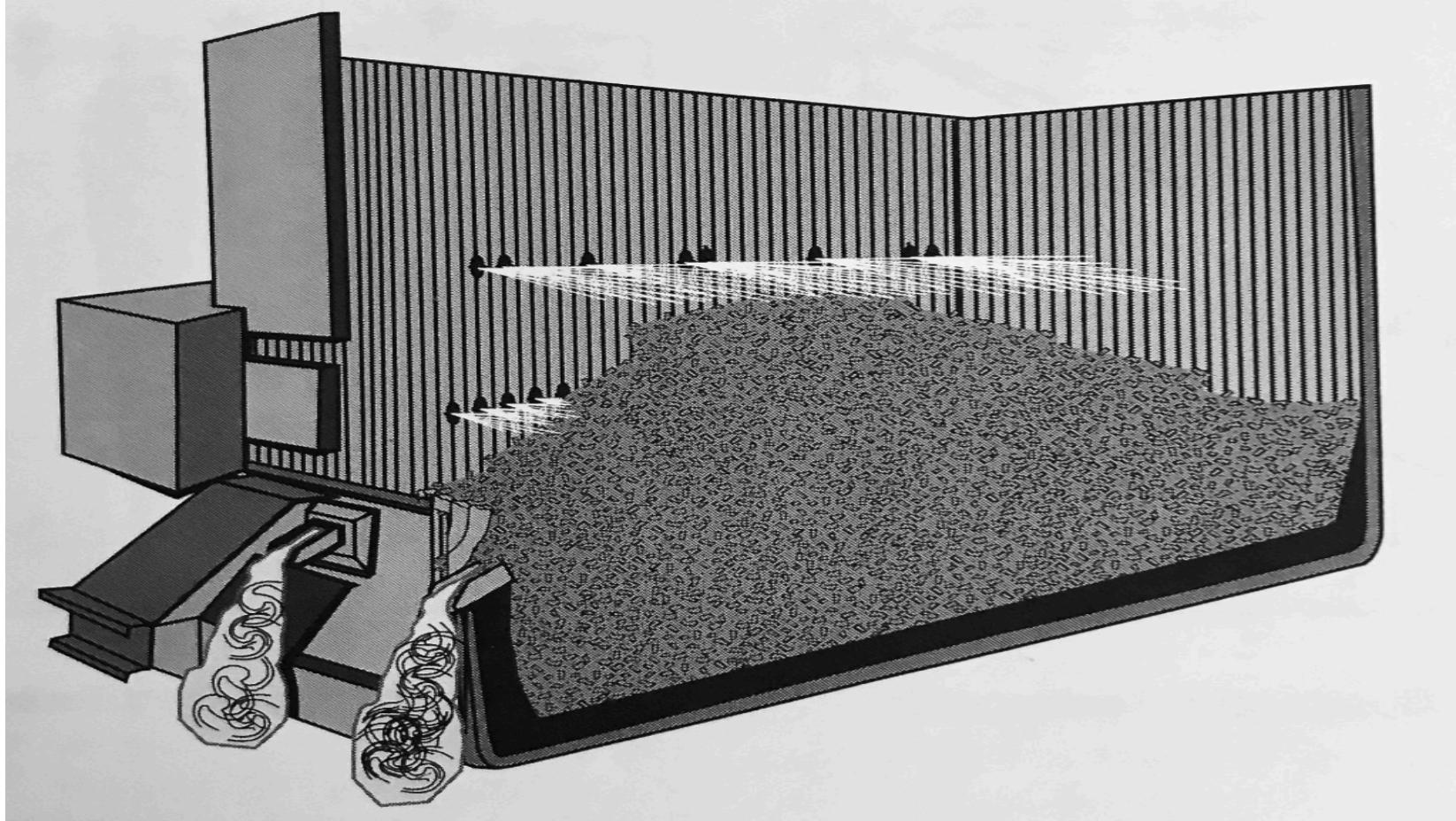
# Objective

- Finding the root cause for sulfur dioxide emission based on historical data.

# Recovery Boiler schematics



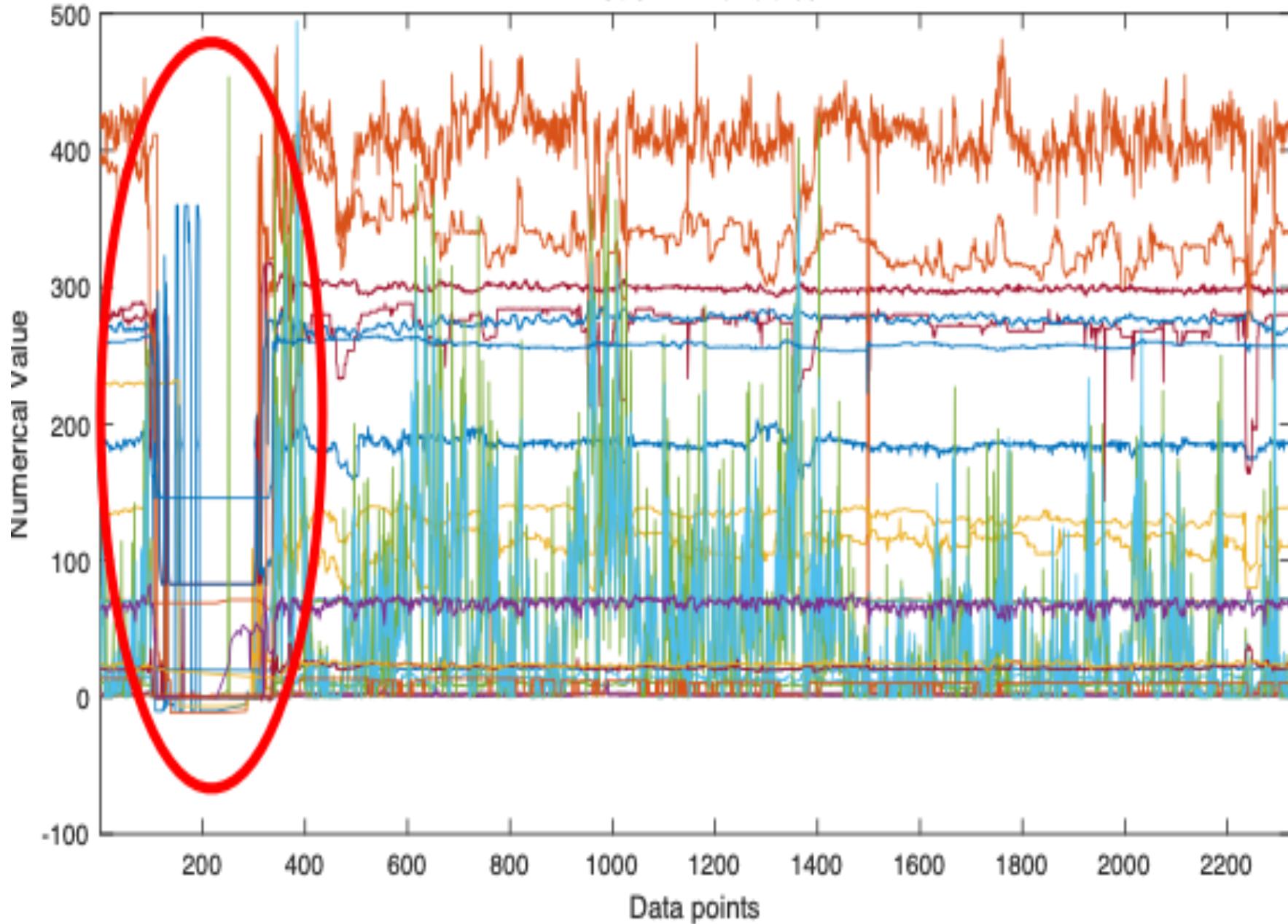
# Inside the Recovery boiler

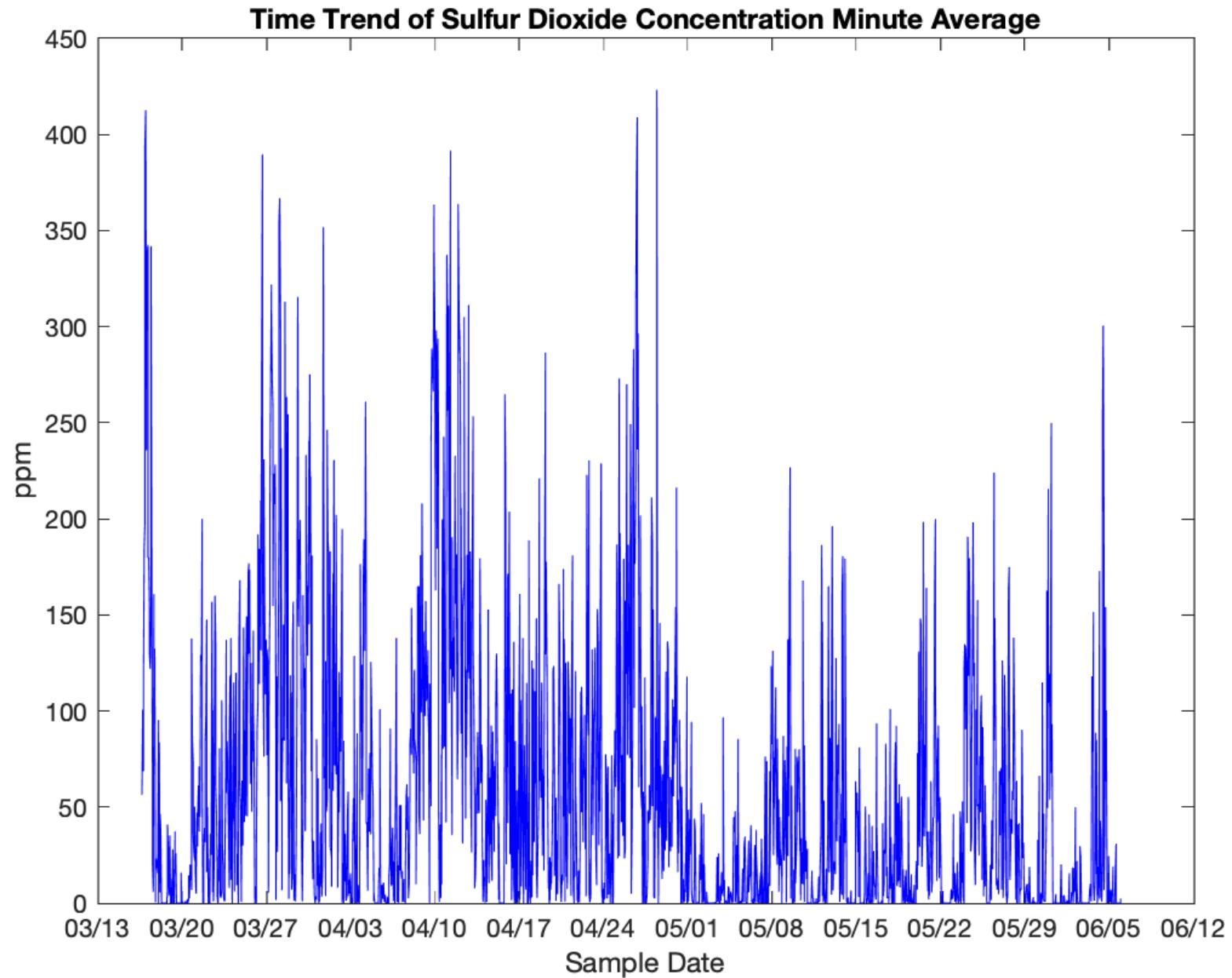


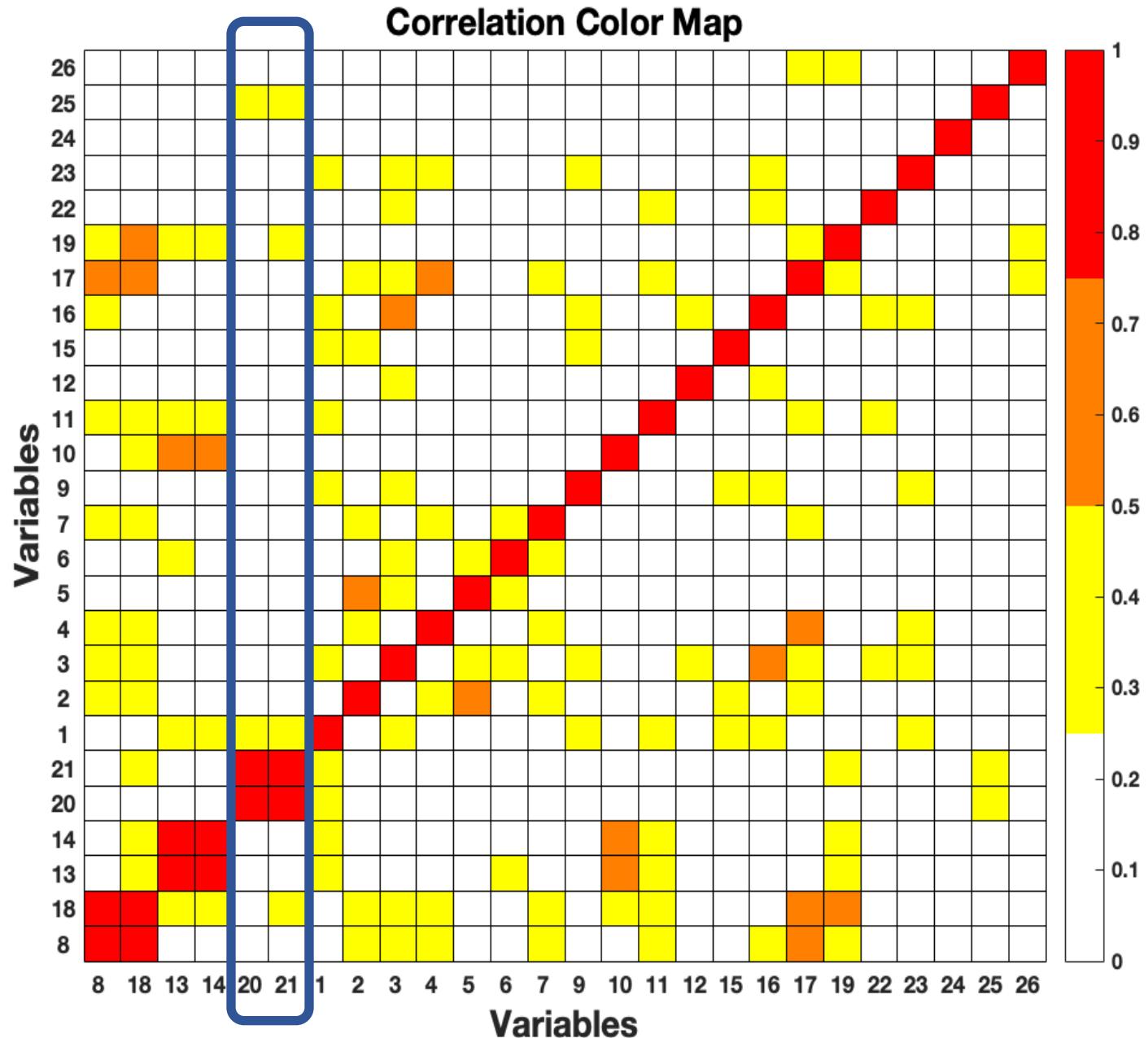
# Exploratory Analysis

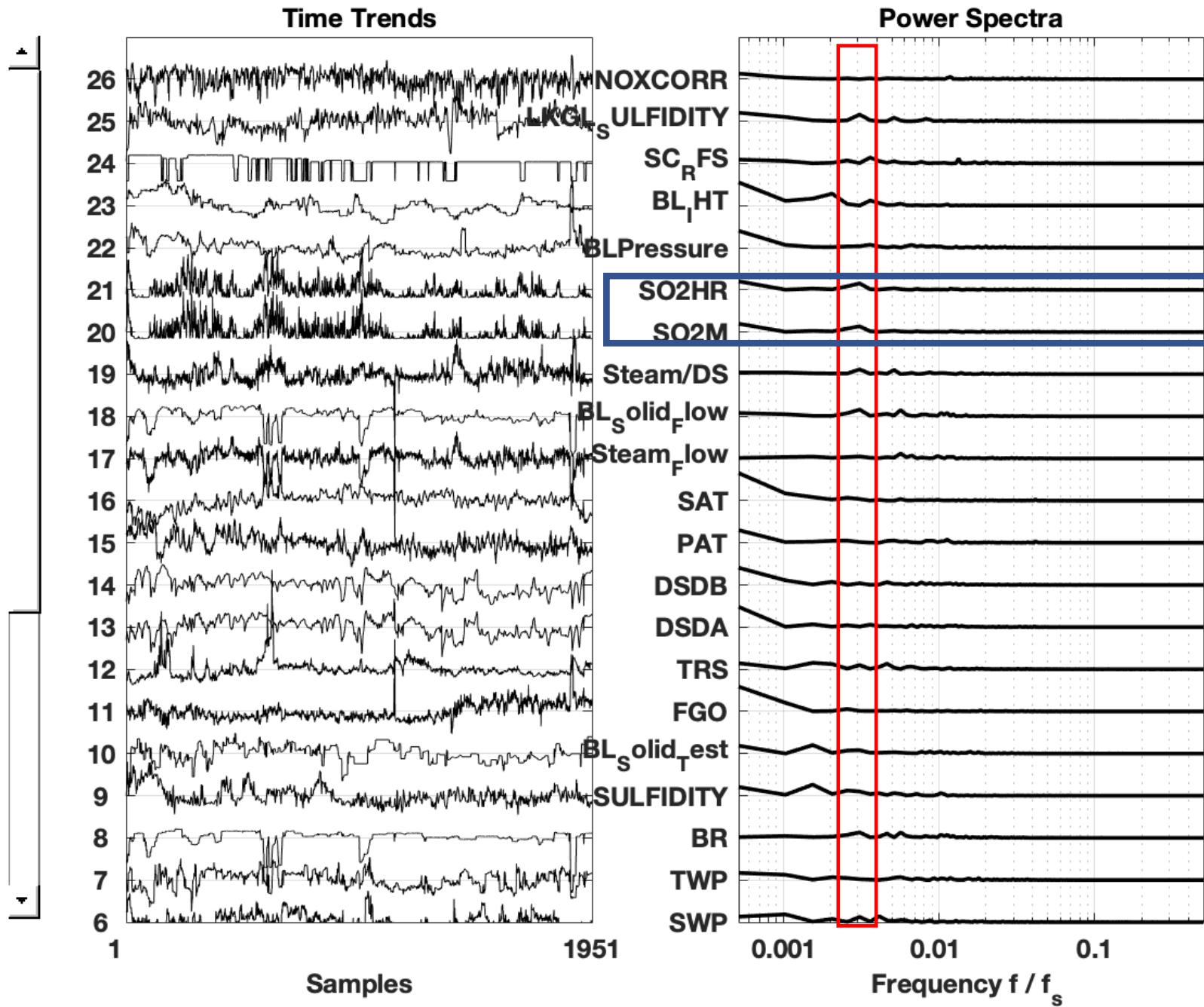
Correlation Map, High Density plot, Compression Test, Quantification Test

Plot of All Variables



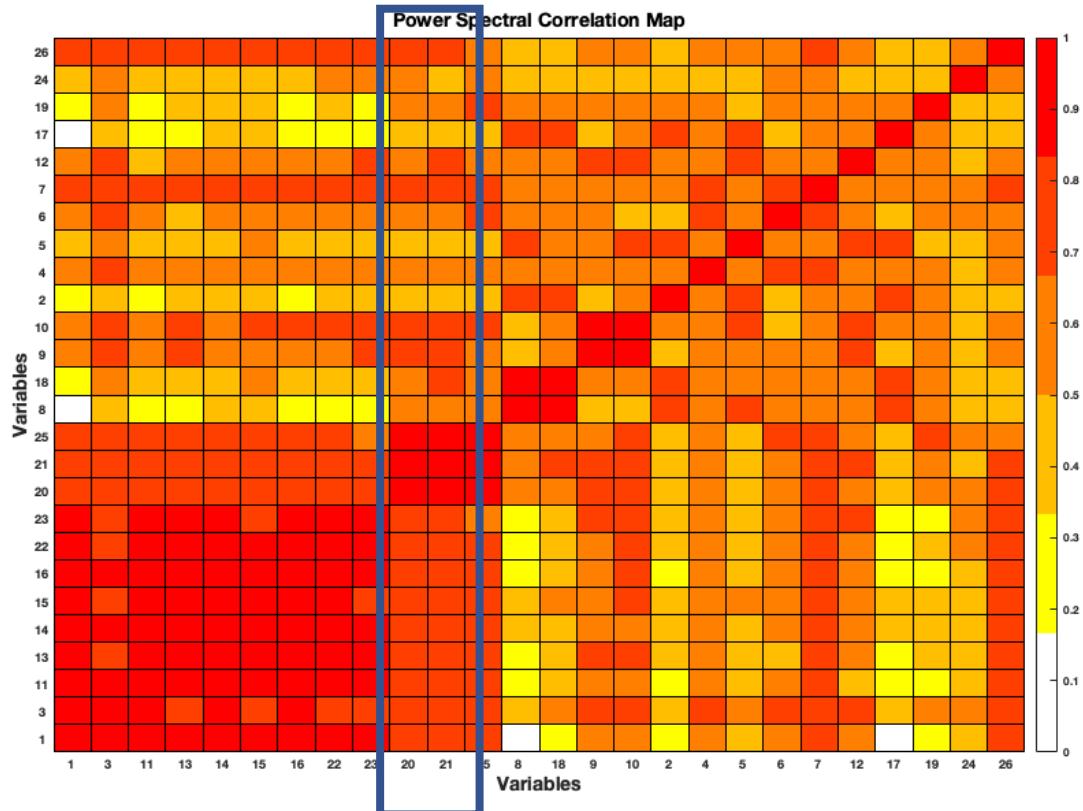






# Spectral Correlation

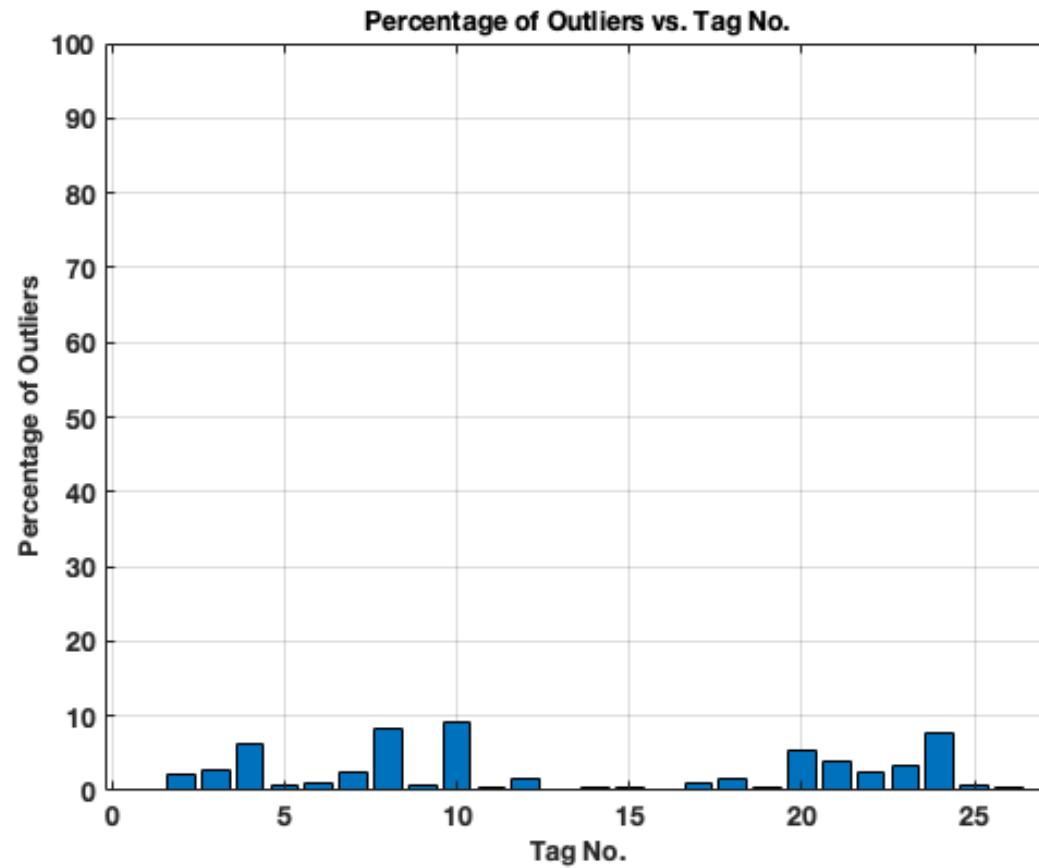
- Secondary Air Flow (Tag 3)
- Flue Gas Oxygen (Tag11)
- Dry Solid Density Transmitter A & B (Tag 13,14)
- Primary Air Temperature (Tag 15)
- Secondary Air Temperature (Tag 16)
- Black Liquor Pressure (Tag 22),  
Black Liquor Indirect Heater  
Temperature (Tag 23)
- Green Liquor Sulfidity (tag 25)
- and NOX Correlation (Tag 26)



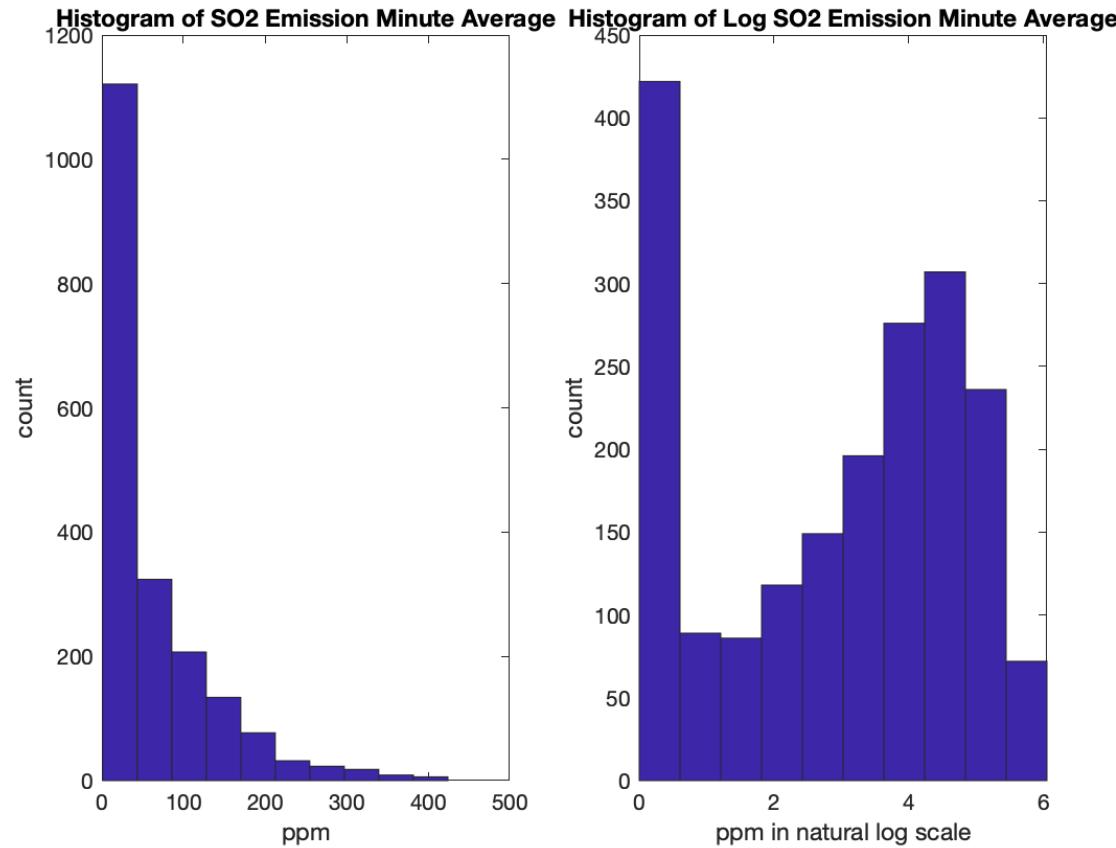
# Pre-Processing

Outliner, Transformation, lag adjustment, MA filter, Normalization

# Outlier Treatment Using DVA tool



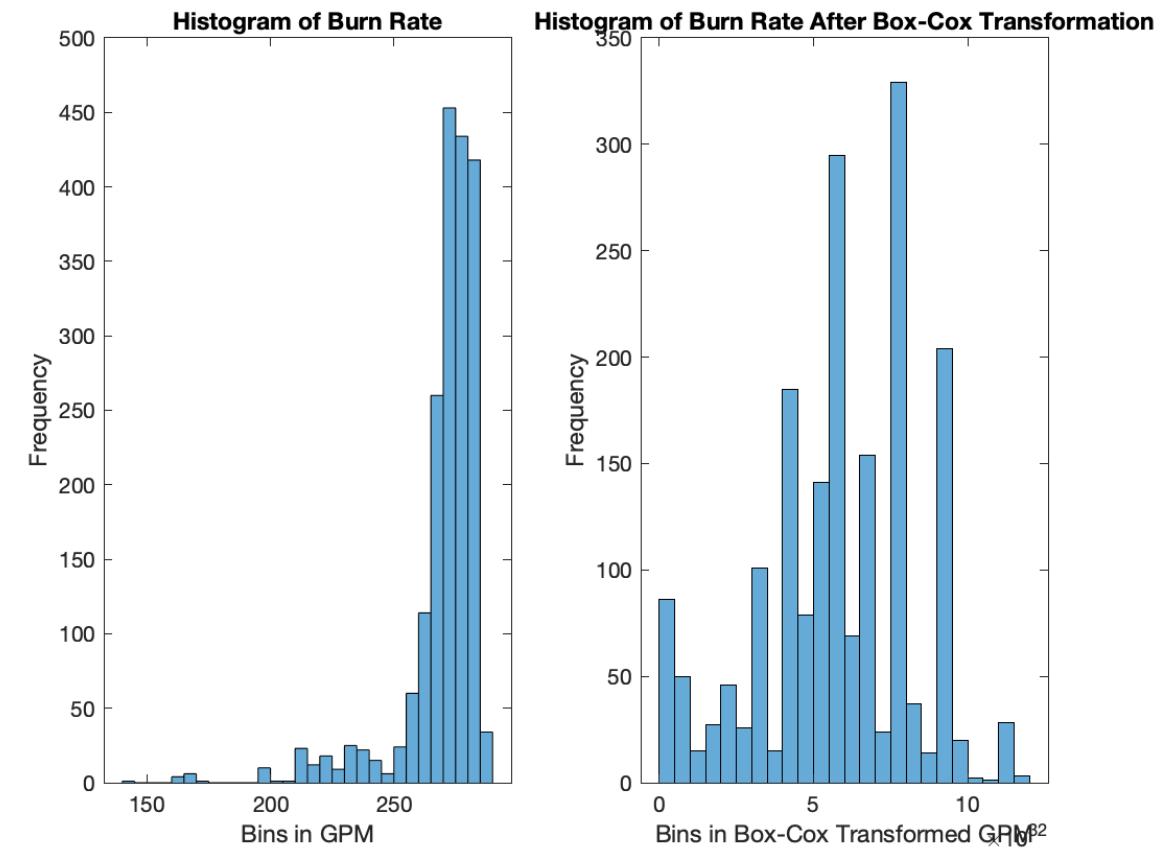
# Log Transformation of SO<sub>2</sub> Emission



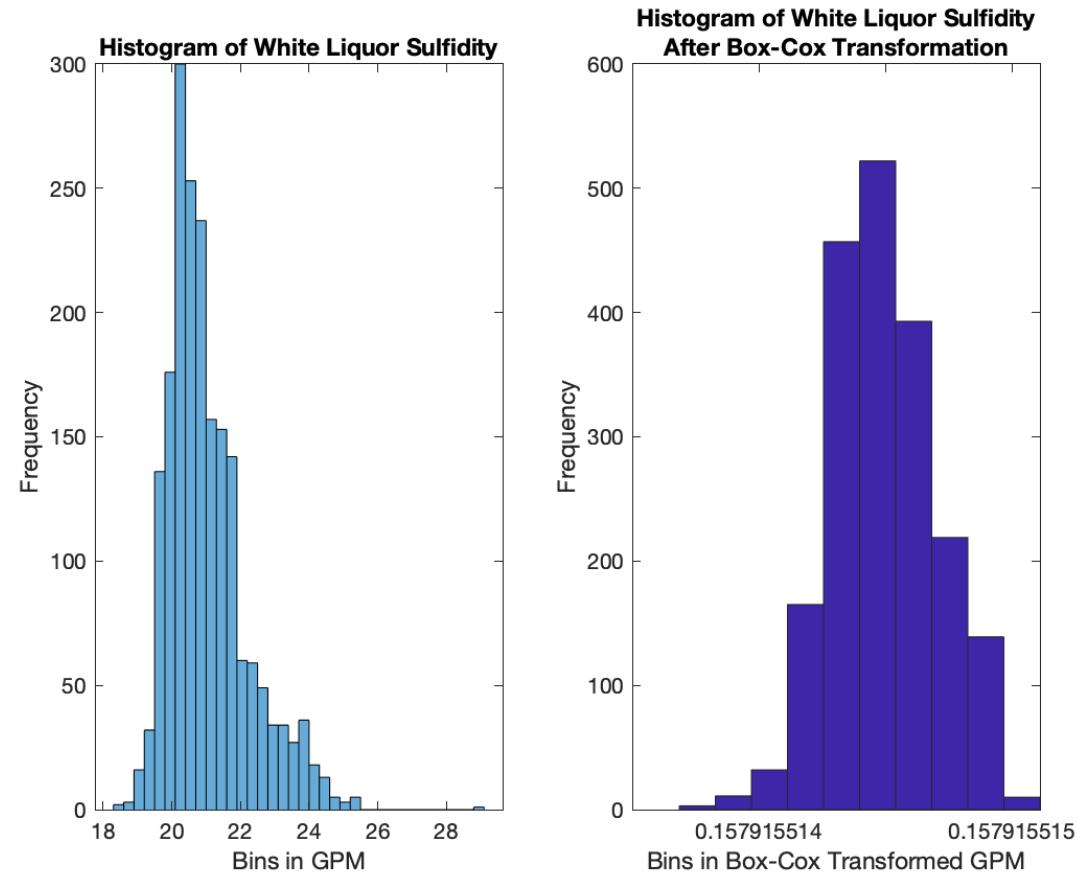
# Box-Cox Transformation of burn rate

Definition of Box-Cox

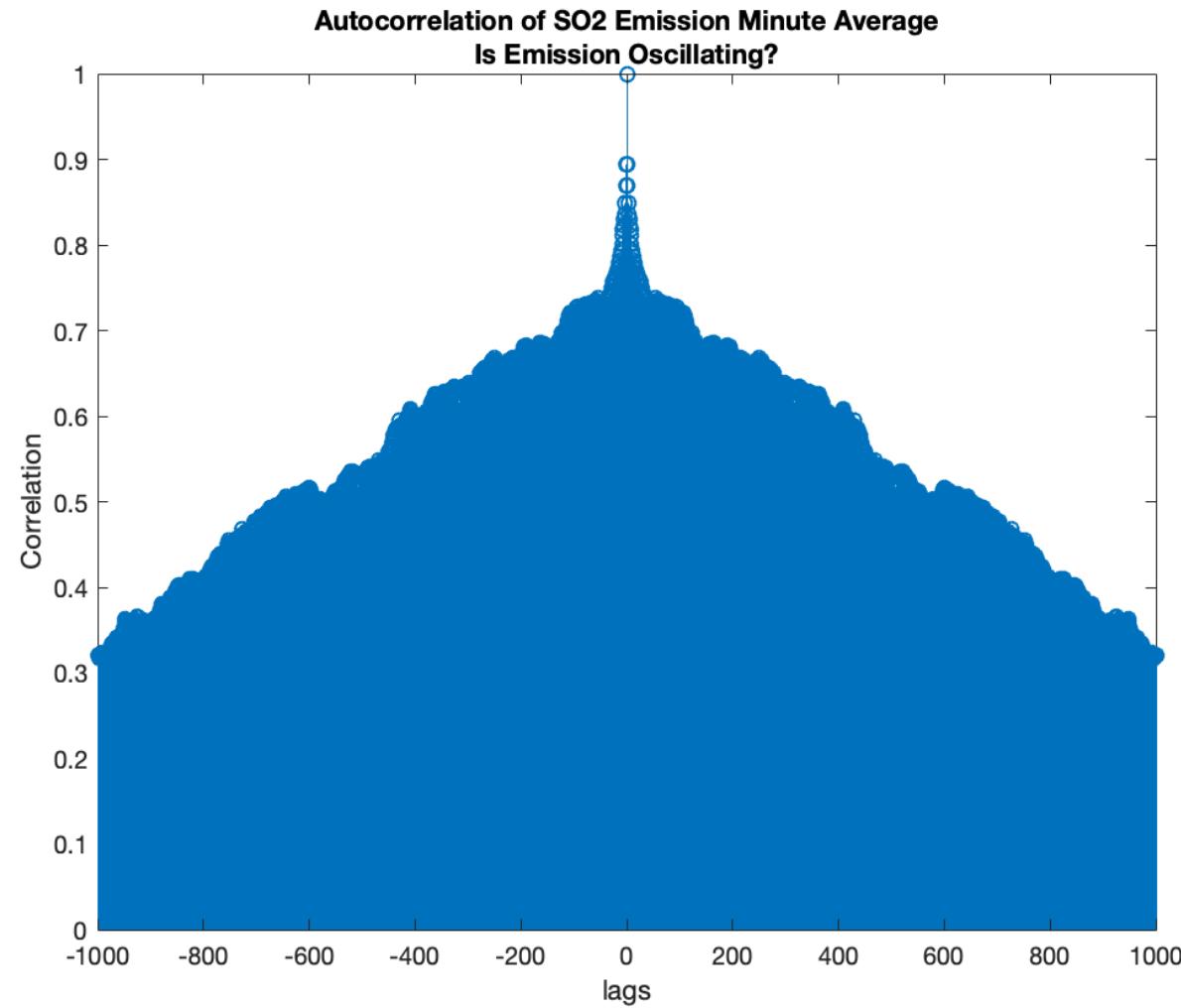
$$Data(\lambda) = \frac{Data^\lambda - 1}{\lambda}$$



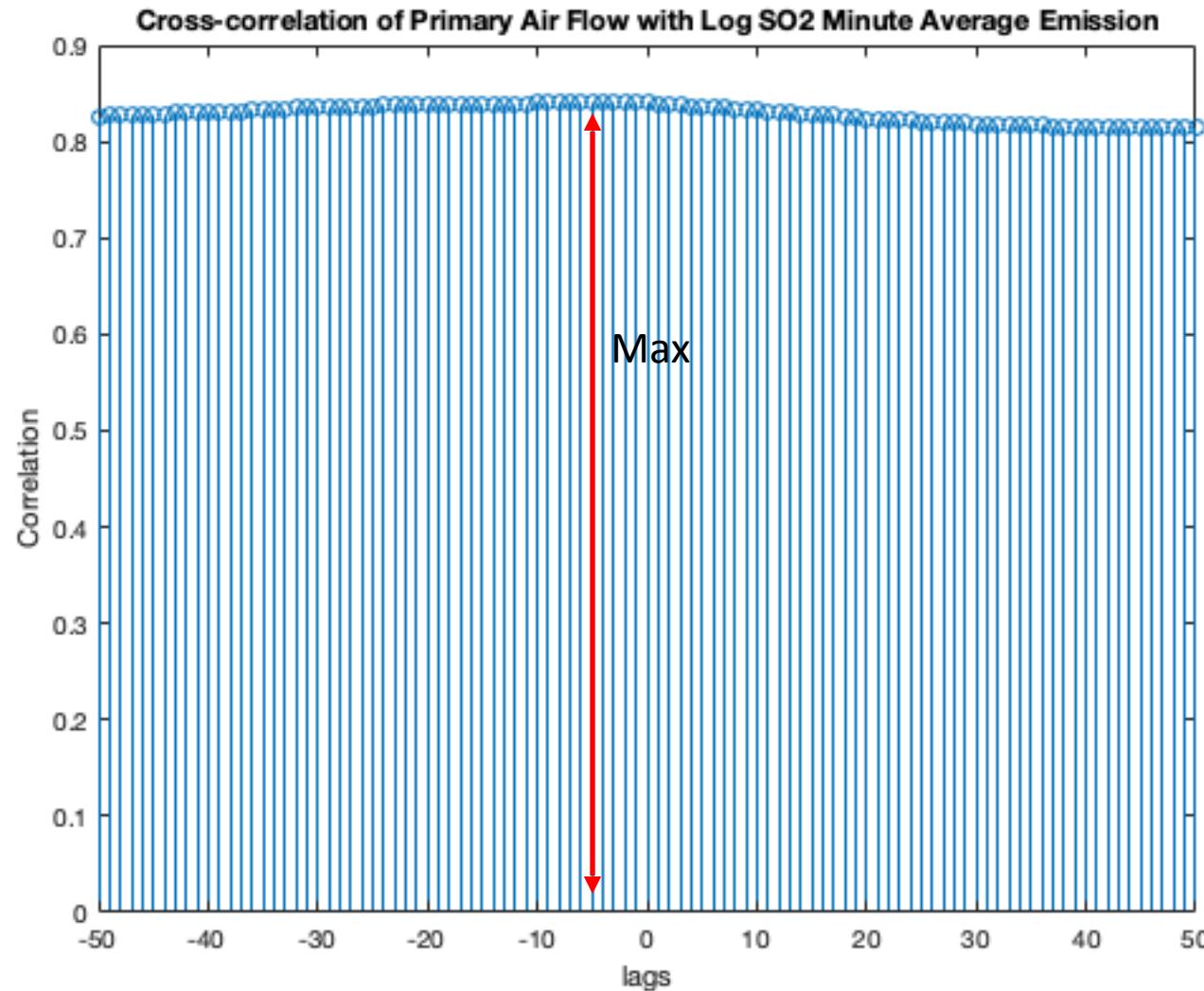
# Box-Cox Transformation of Sulfidity



# Is Emission Oscillating?



# Cross-correlation for all variables with SO<sub>2</sub>



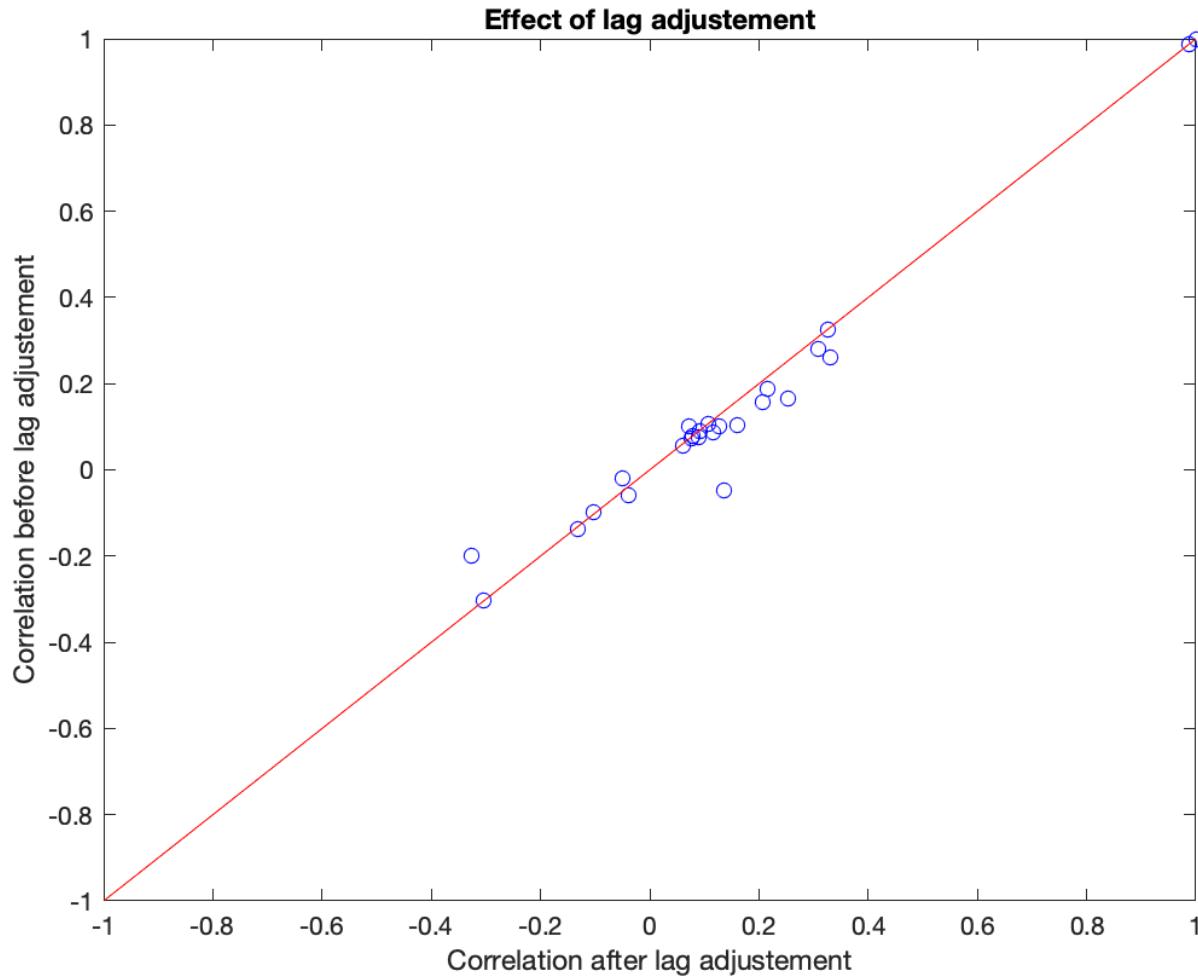
# Lag time found by maximizing Cross-Correlation

Variables	Lag time with Log
Time stamp	0
PAF	-5
SAF	-5
TAF	-9
PWP	-5
SWP	0
TWP	-26
BR	-10
Sulfidity	-1
BL_Solid_Test	-9
FGO	-21
TRS	-30
DSDA	-10

Variables	Lag time
DSDB	-10
PAT	0
SAT	0
Steam_Flow	-2
BL_Solid_Flow	-10
Steam/DS	-2
SO2M	0
SO2HR	-1
BLPressure	-10
BL_IHT	0
SC_RFS	-34
LKG1_SULFIDITY	-9
NOXCORR	-15

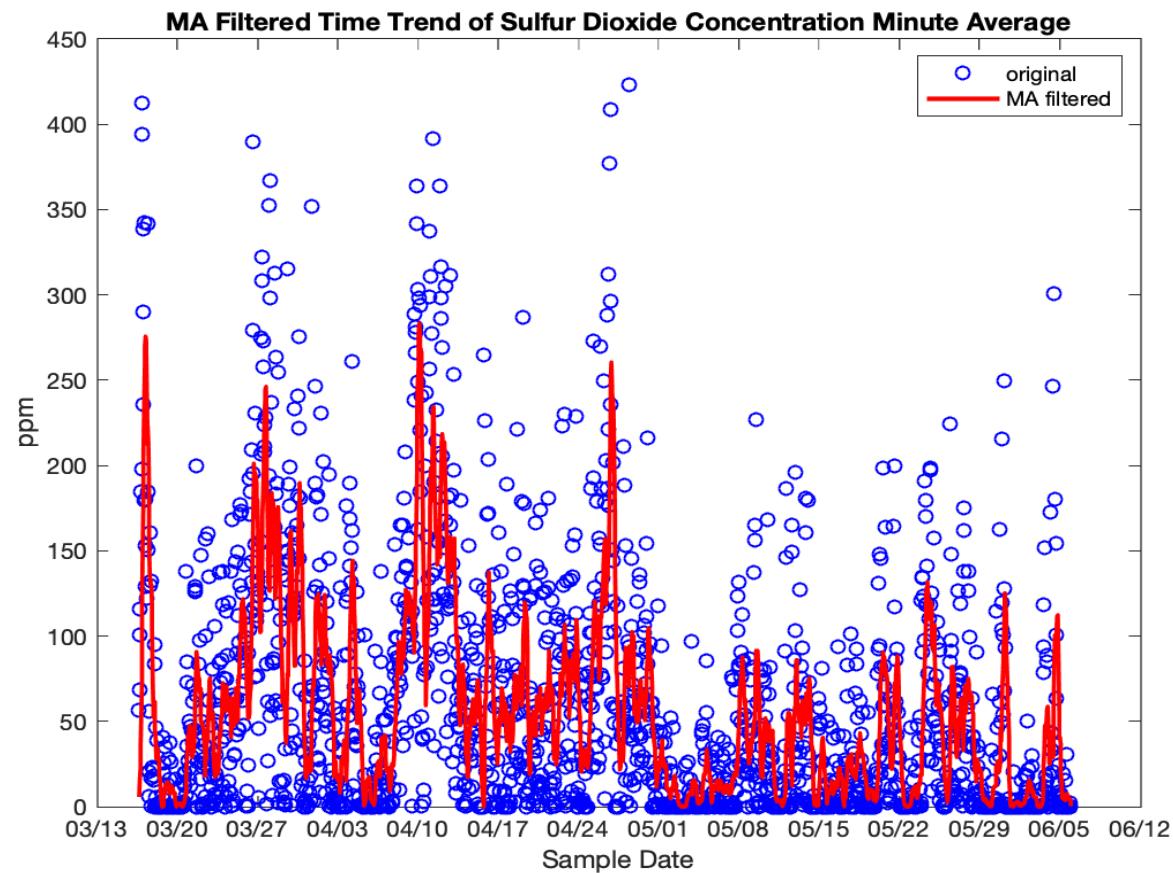
# Effect of Lag adjustment

## Changes in Correlation with SO<sub>2</sub> emission



# Moving Average filter

Window size = 20



# Normalization

- Data are normalized and centered to balance the scale of the variables and make variance comparable.

# Creation of training and test set

- Training set and test set were created using random sampling without replacement.
- 1366 records goes to training and 585 records goes to testing

# Training and Testing

OLS, PCR, PLS, Regression Trees

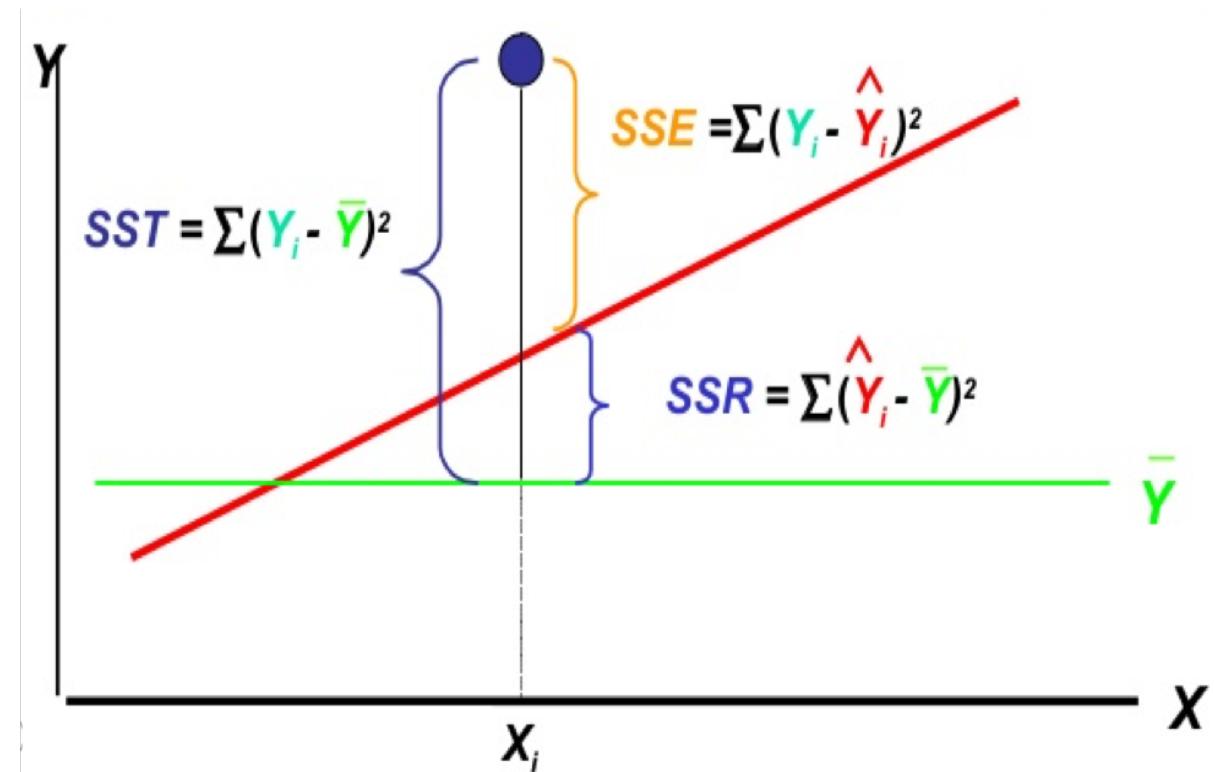
# Ordinary Least Square Regression

Model

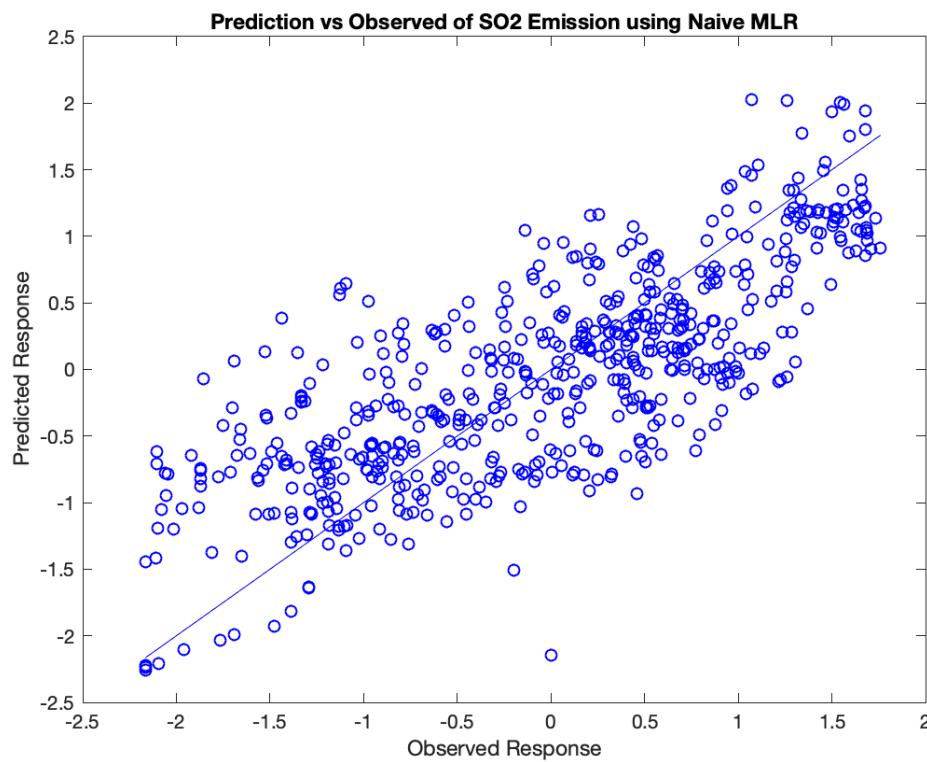
$$\hat{\beta} = (X_t^T X_t)^{-1} X_t^T Y_t$$

Testing

$$\hat{Y} = \hat{\beta} X_{test}$$



# Ordinary Least Square Testing

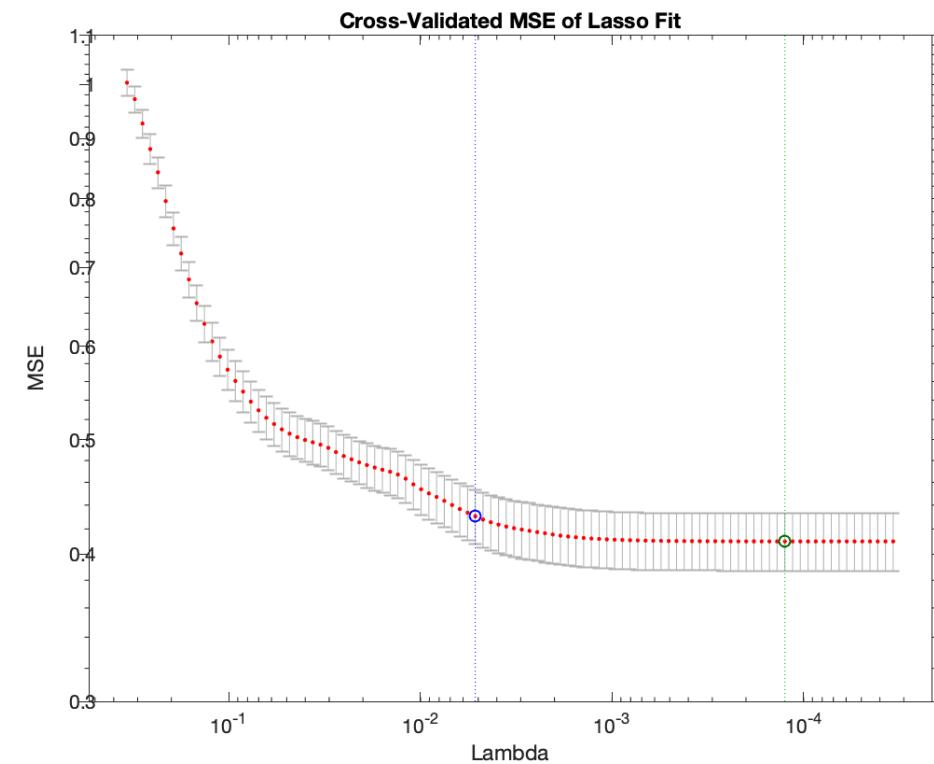
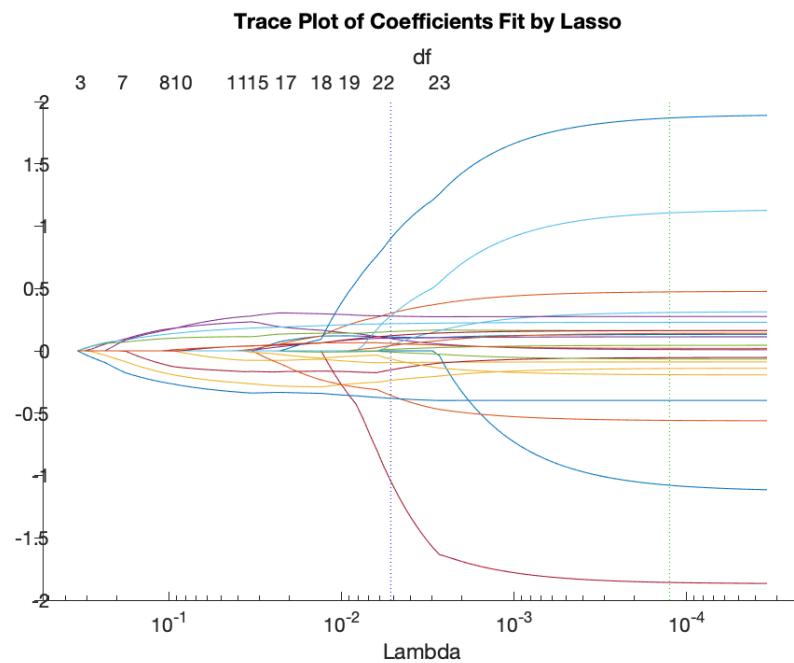


- Regress with all 23 variables
- SSE is 237.8710
- RMSE was 0.6512
- R<sup>2</sup> is 0.5866.

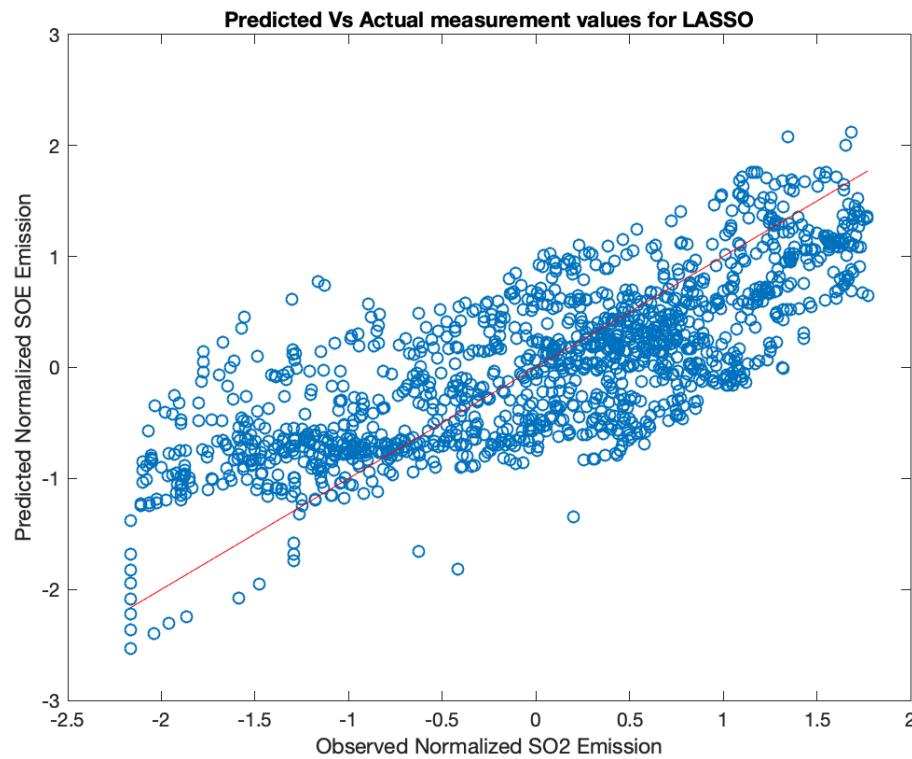
# LASSO

## Objective Function

$$\min_{\beta \in \mathbb{R}^p} \left\{ \frac{1}{N} \|y - X\beta\|_2^2 + \lambda \|\beta\|_1 \right\}$$

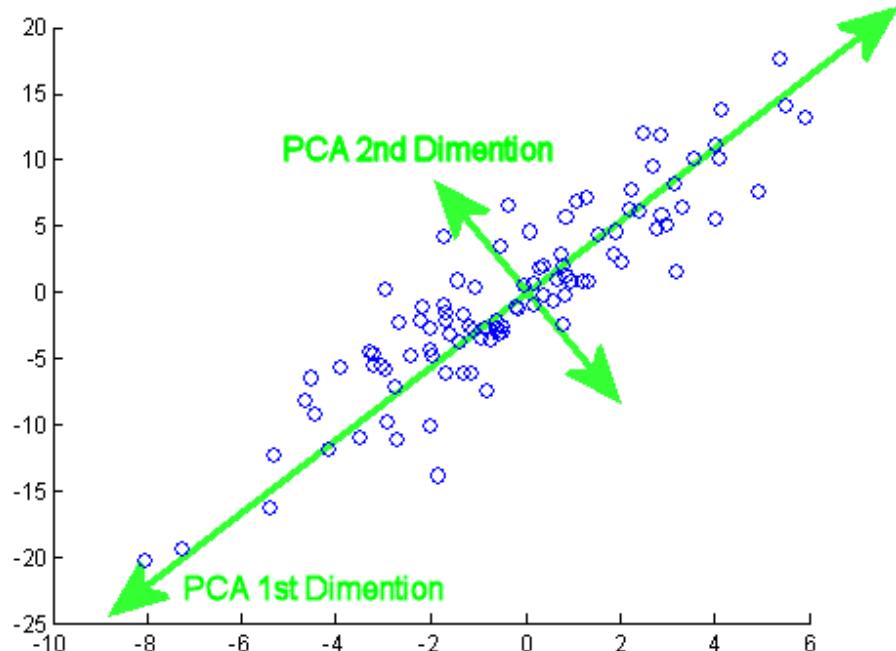


# Testing LASSO



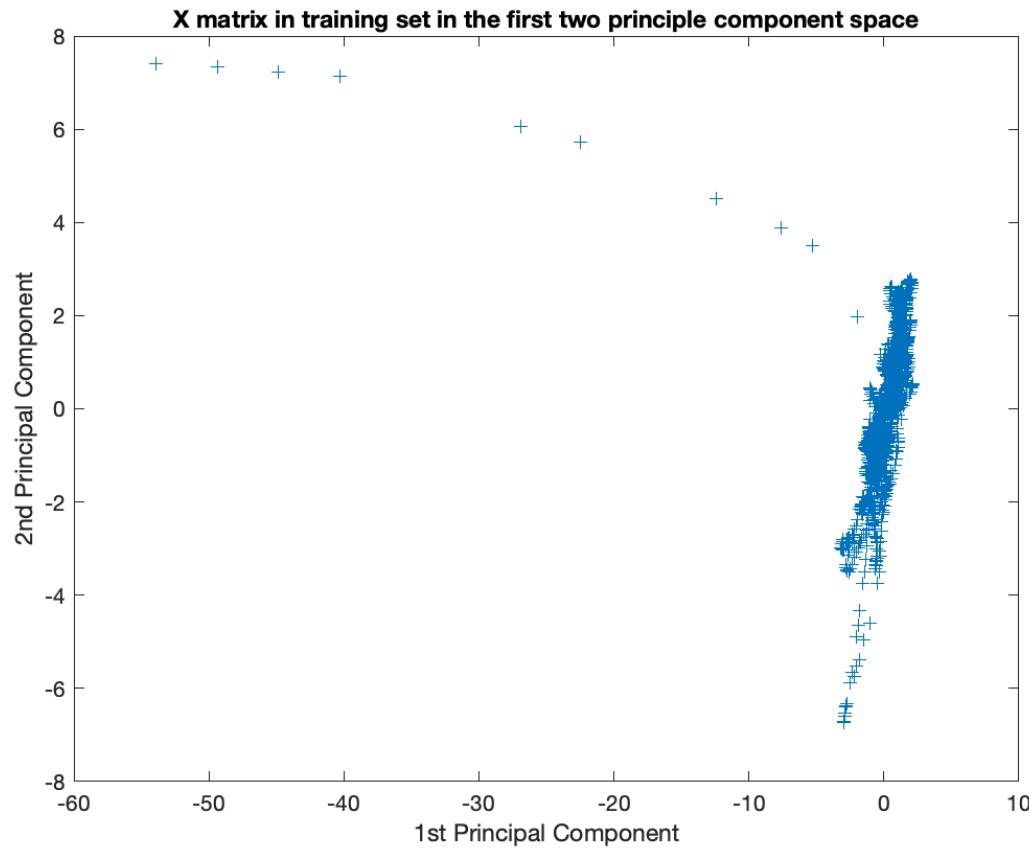
- Regress with all except Sulfidity
- RSS = 251.8956
- RSE = 0.6695
- Rsq = 0.5623

# Principle Component Analysis

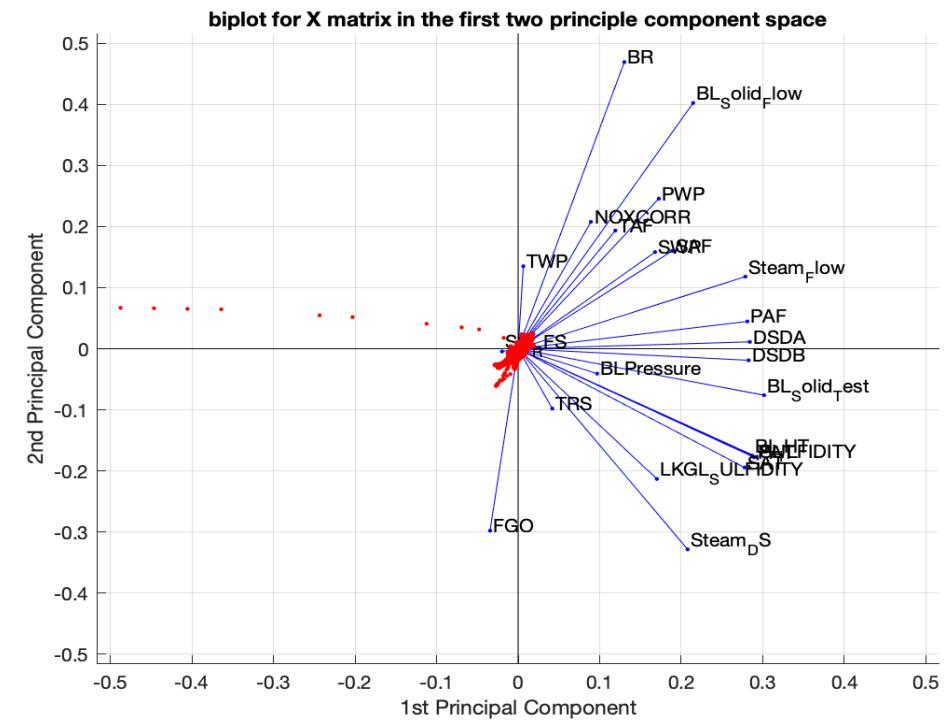
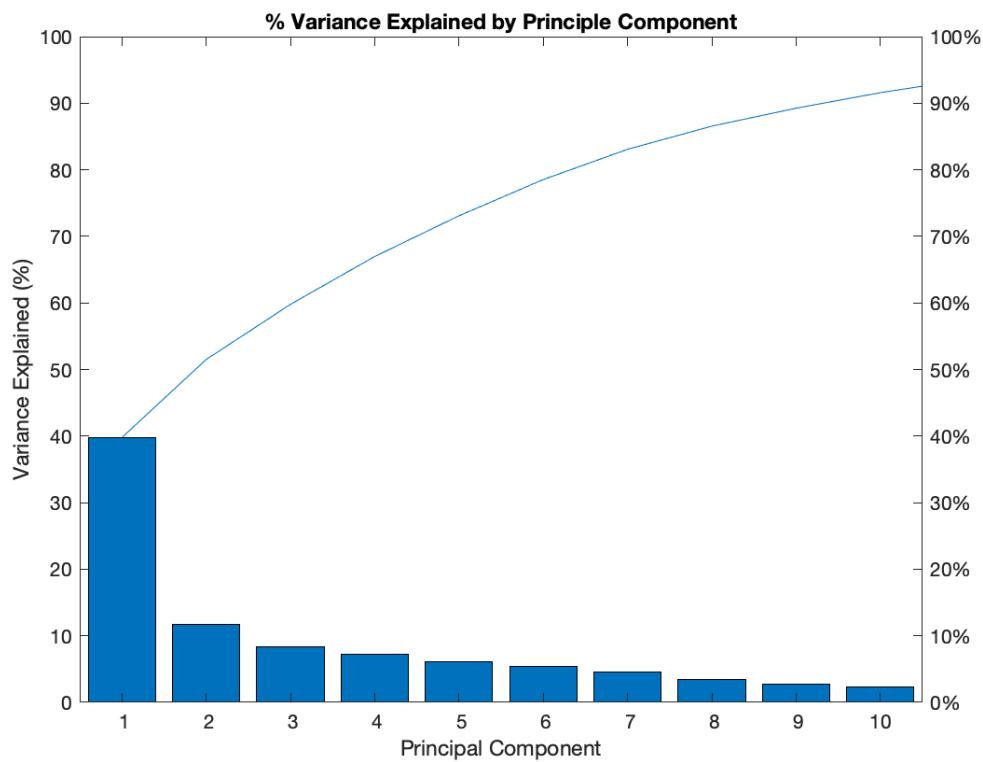


- Dimension reduction by creating latent variables that are linear combination of the original variables.
- PCA finds efficient ways to describe data with less variable and with minimum data loss

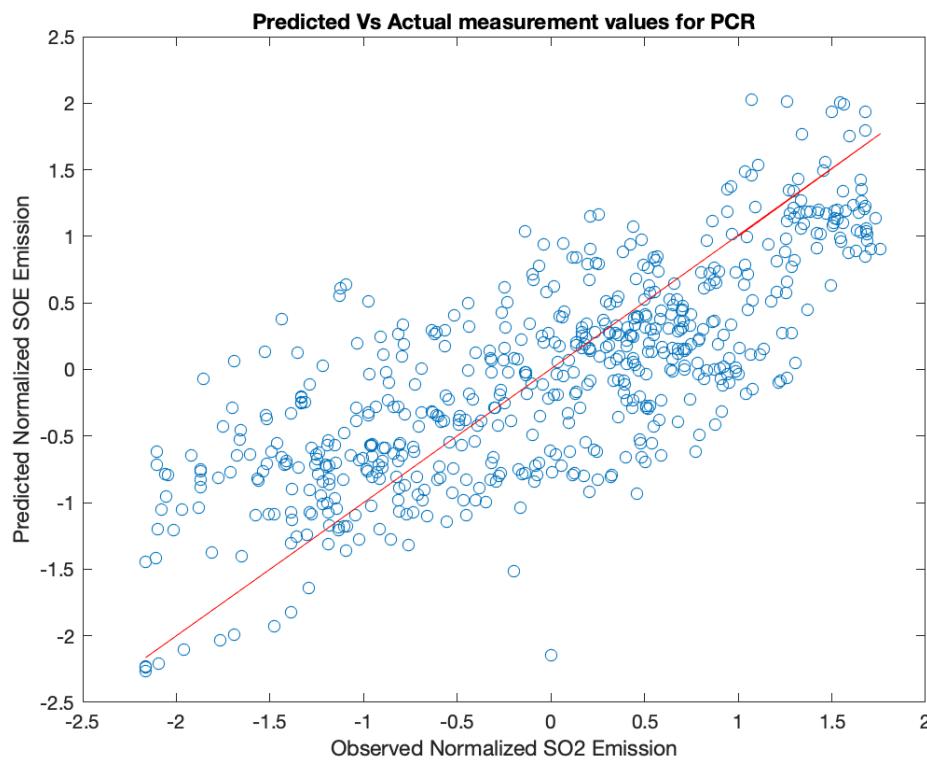
# X training data in the first two principle component space



# Variance explained by principle components

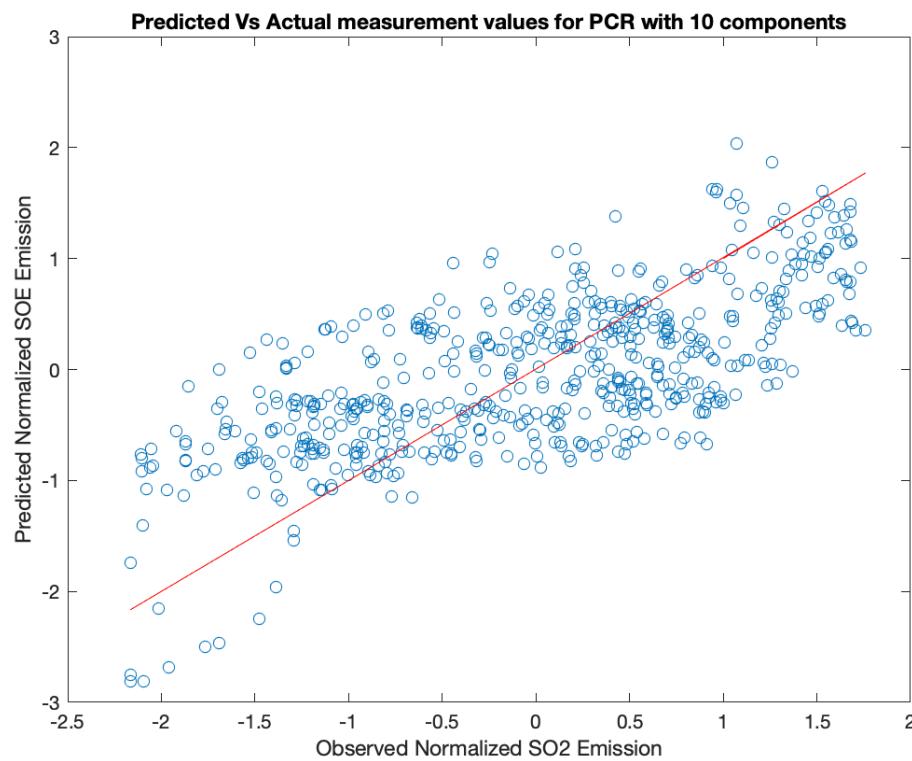


# Principle Component Regression



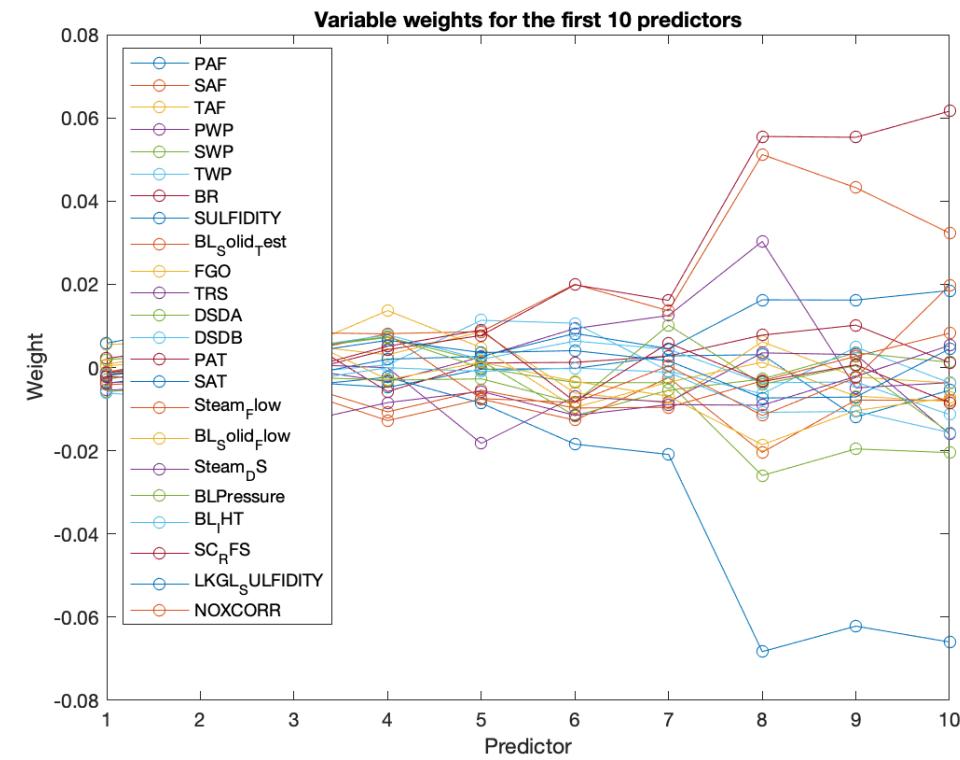
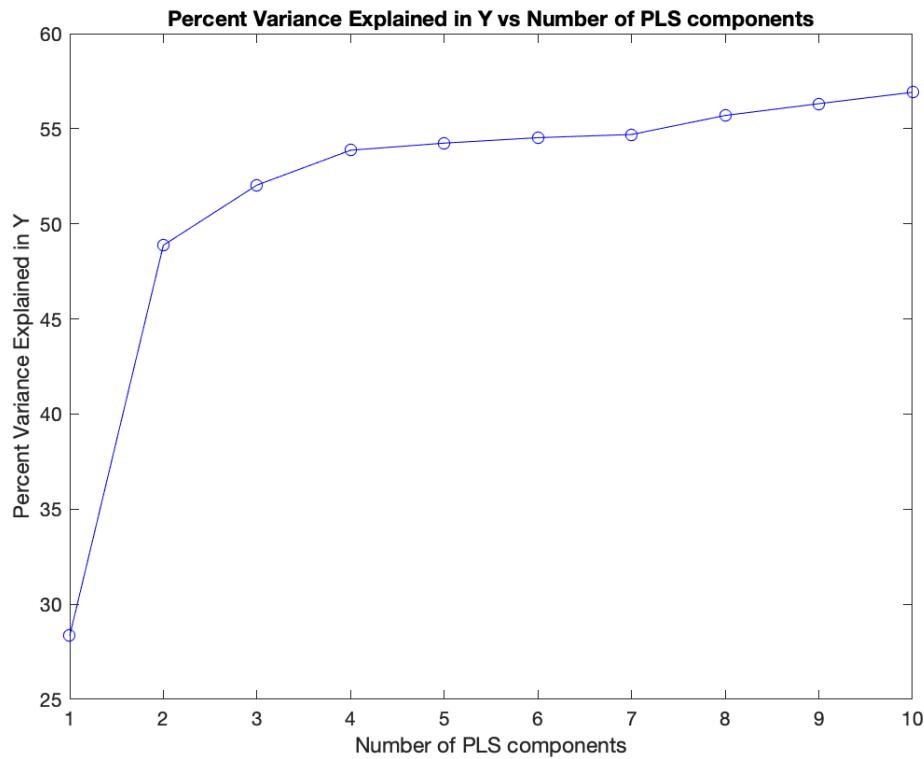
- Regression with all variables
- SSE is 237.87
- RMSE is 0.6512
- Rsq = 0.5866
- Identical to OLS when regressing all variables

# Principle Component Regression

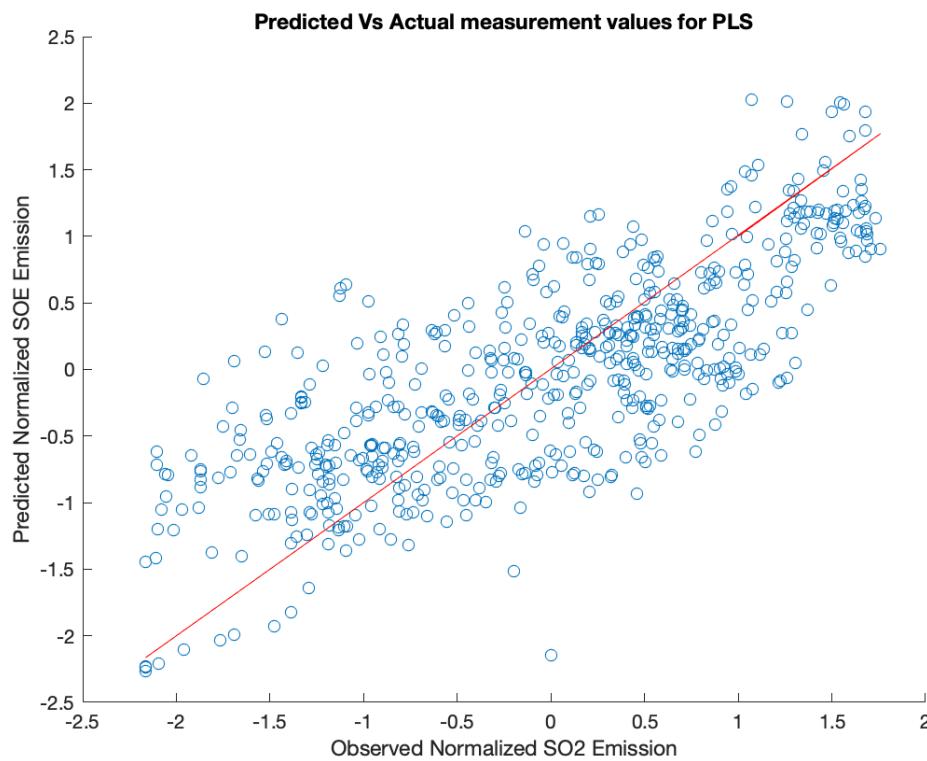


- Regress with top 10 components
- SSE = 304.6549
- RMSE = 0.7369
- R-sq = 0.4706
- Over estimated in the low end and underestimating in the high end

# Partial Least Square

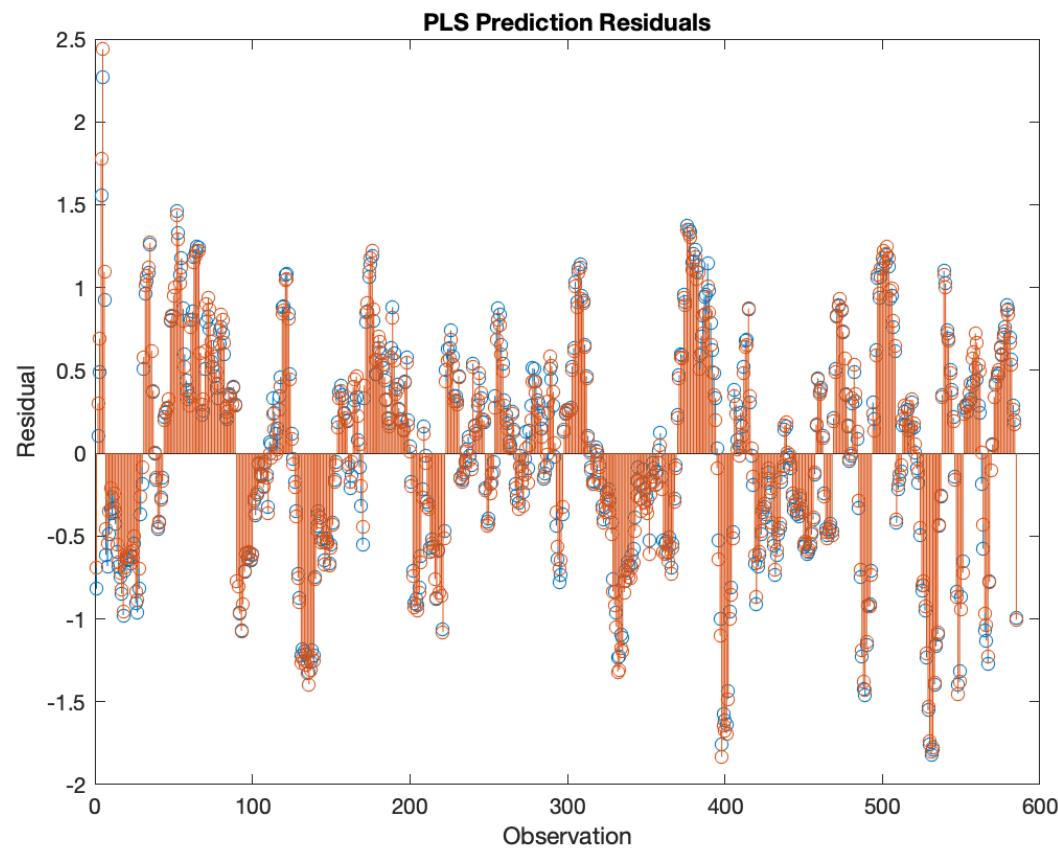


# Partial Least Square Testing

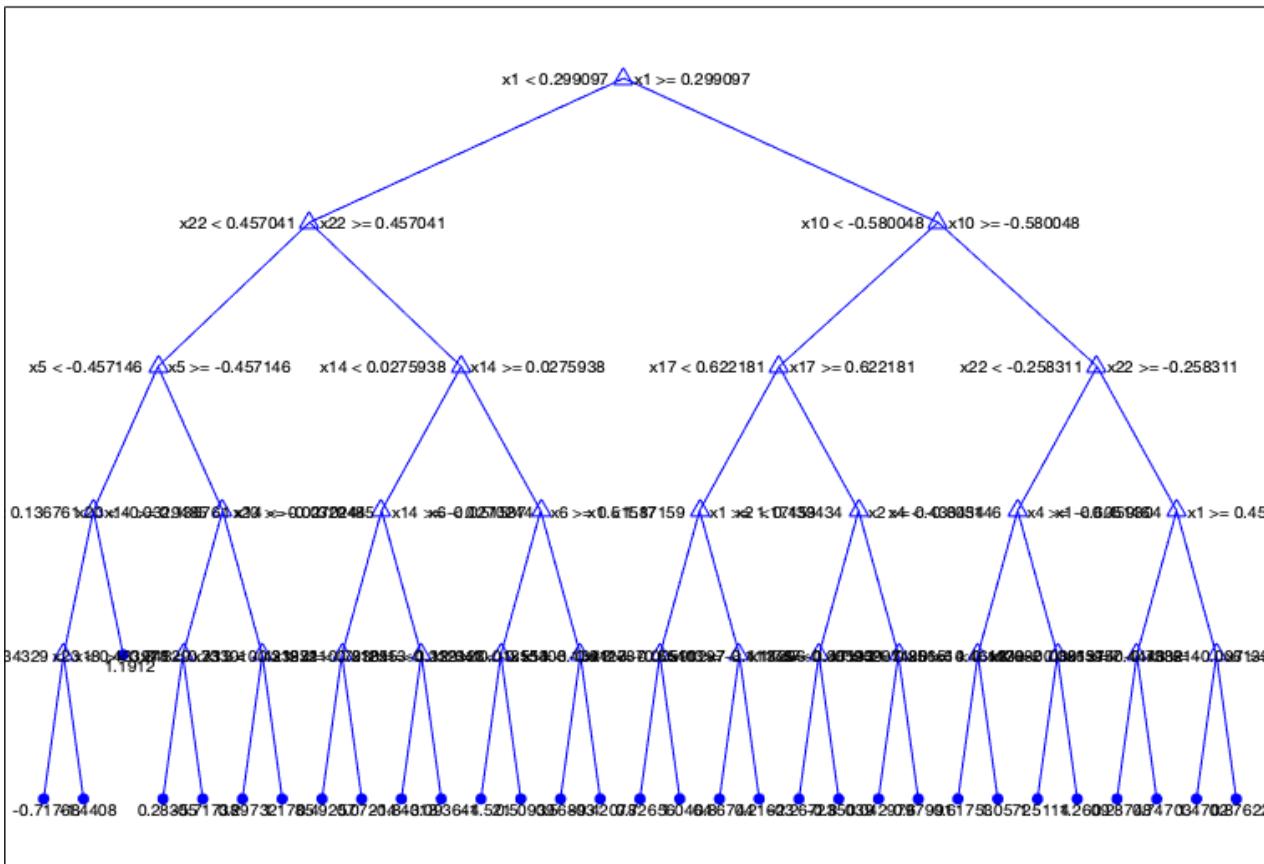


- Regress with to 10 components & 10 fold crossvalidation
- SSE = 257.56
- RMSE = 0.66
- R square = 0.55
- Same accuracy as OLS with fewer components

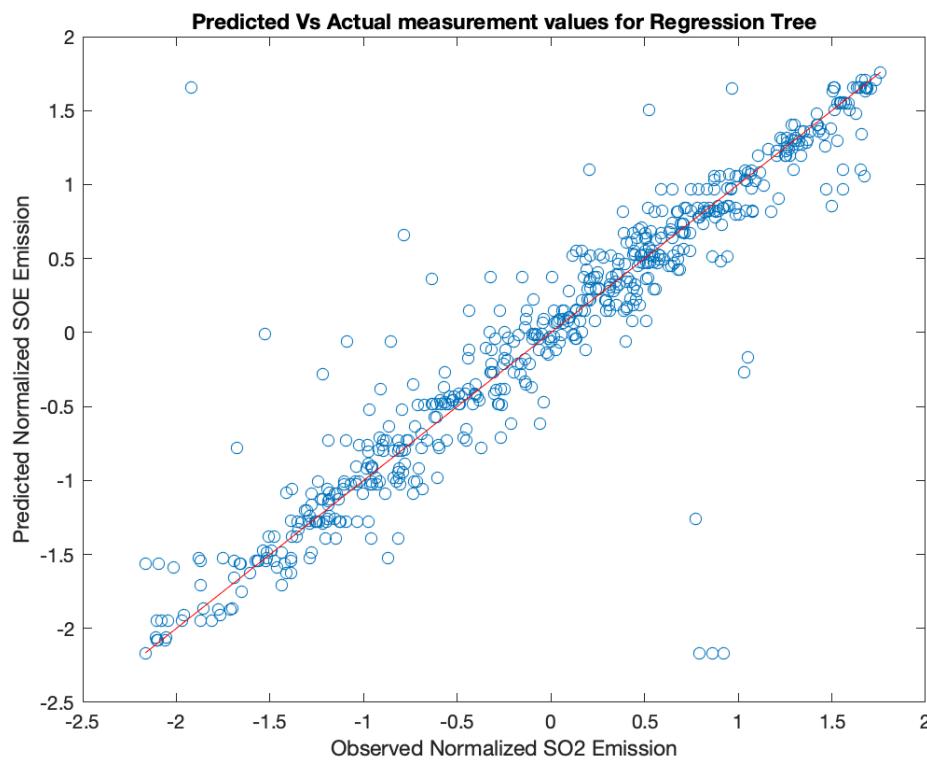
# PLS Residuals



# Regression Trees

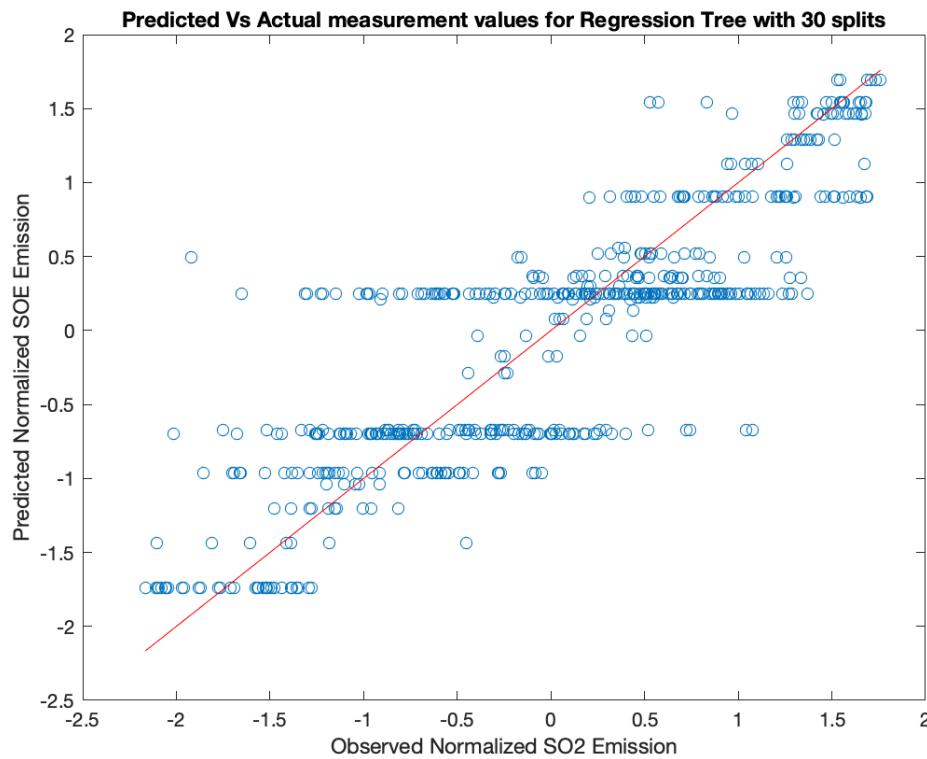


# Regression Tree Testing



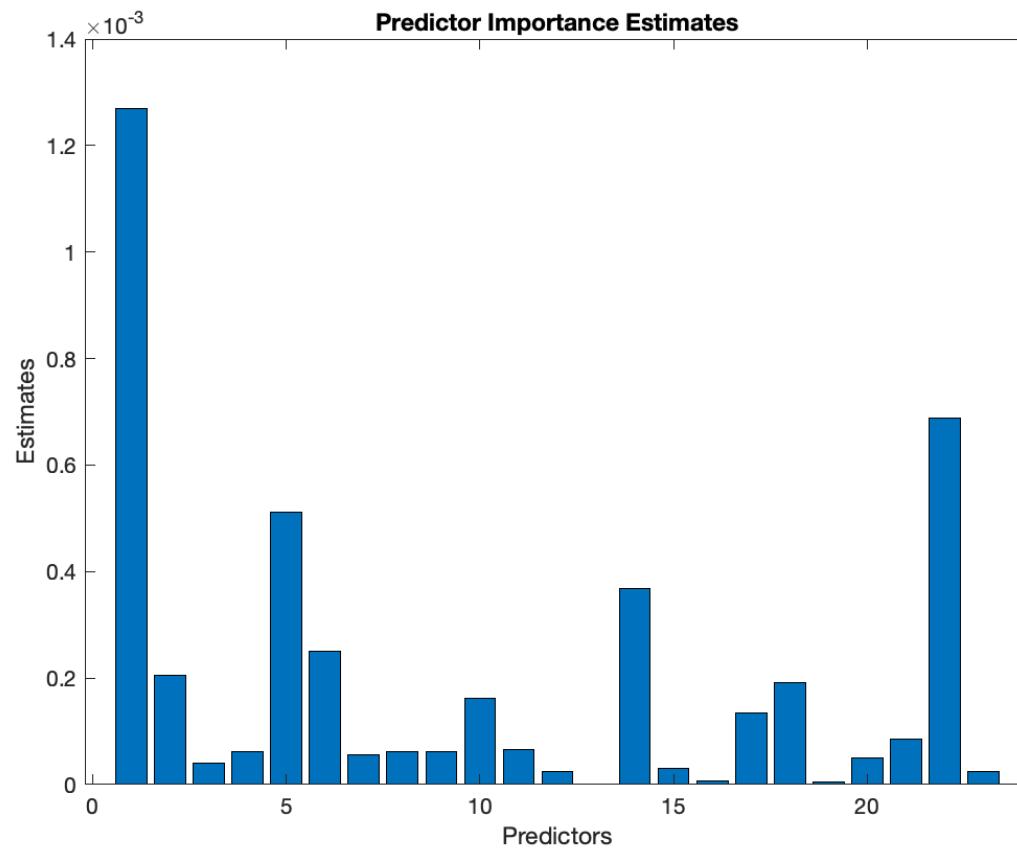
- Regression with all variables with unlimited branches and 10 fold cross validation.
- SSE = 81.5320
- RMSE = 0.3812
- R sq = 0.8583

# Regression Tree Testing



- With 30 splits only, 10 fold cross validation, and all variables
- SSE = 150.8188
- RMSE = 0.5126
- R sq = 0.7379

# Regression Tree Importance of parameters



# Summary of Method Prediction Performance

Method	RMSE	R square	number of variables/components/ split for trees
OLS	0.6512	0.5866	23
LASSO	0.6695	0.5623	22
PCR	0.6512	0.5866	23
PCR	0.7369	0.4706	10
PLS	0.6699	0.5524	10
Regression Trees	0.3669	0.8583	max
Regression Trees	0.5056	0.7451	30

# Root Cause Analysis

## Top 6 Variables in beta magnitude

	OLS Beta	PCR Beta	PLS Beta with 10 component	Decision Tree
Intercept			-0.0033	-0.002
Primary Air Flow	0.13	0.1338	0.1736	1.25E-03
Secondary Air Flow	0.48	0.4791	0.3014	8.33E-05
Tertiary Air Flow	-0.09	-0.0891	-0.106	1.24E-05
Primary Windbox Pressure	0.01	0.0063	0.0692	4.35E-05
Secondary Windbox Pressure	0.16	0.1629	0.1517	4.62E-04
Tertiary Windbox Pressure	0.23	0.2291	0.2278	2.92E-04
Burn Rate	-0.05	-0.0517	-0.2344	1.10E-05
White Liquor Sulfidity	-1.15	-1.1528	-0.2019	3.55E-05
Black Liquor Solid 50./50 Test	-0.56	-0.5635	-0.5889	1.15E-04
Flue Gas Oxygen	-0.14	-0.1381	-0.2517	6.98E-05
Total Reduced Sulfur	0.11	0.1131	0.1305	5.07E-05
Dry Solid Density				
Transmitter A	0.04	0.0446	0.2063	1.25E-05
Dry Solid Density Transmitter B	0.32	0.3174	-0.0241	1.12E-05
Primary Air Temperature	-1.88	-1.8789	-0.6623	4.04E-04
Secondary Air Temperature	1.91	1.9104	0.7832	6.65E-05
Steam Flow Rate	0.14	0.1429	0.103	1.87E-05
Black Liquor Solid Flow Rate	-0.19	-0.1942	-0.0042	8.37E-05
Steam to Dry Solid Ratio	0.28	0.2757	0.3191	1.62E-04
Black Liquor Pressure	-0.07	-0.0679	0.0106	4.80E-05
Black Liquor Indirect Heater Temperature	1.15	1.1518	0.1438	1.75E-04
Salt Cake Rotary Feeder Speed	0.16	0.163	0.1107	7.59E-07
Lime Kiln Green Liquor Sulfidity	-0.4	-0.3978	-0.3204	7.19E-04
Nitrogen Oxides correlation	0.02	0.0184	0.0697	1.39E-04

# Root Cause Analysis

	SPECTRAL ANALYSIS	REGRESSION	REACHABILITY
PRIMARY AIR FLOW		Yes	
SECONDARY AIR FLOW	Yes	Yes	Yes
TERTIARY AIR FLOW			
PRIMARY WINDBOX PRESSURE			
SECONDARY WINDBOX PRESSURE			
TERTIARARY WINDBOX PRESSURE			
BURN RATE			
WHITE LIQUOR SULFIDITY	Yes	Yes	Yes
BLACK LIQUOR SOLID 50./50 TEST		Yes	
FLUE GAS OXYGEN	Yes		
TOTAL REDUCED SULFUR			
DRY SOLID DENSITY TRANSMITTER A	Yes		
DRY SOLID DENSITY TRANSMITTER B	Yes		
PRIMARY AIR TEMPERATURE	Yes	Yes	Yes
SECONDARY AIR TEMPERATURE	Yes	Yes	Yes
STEAM FLOW RATE			
BLACK LIQUOR SOLID FLOW RATE			
STEAM TO DRY SOLID RATIO			
BLACK LIQUOR PRESSURE	Yes		
BLACK LIQUOR INDIRECT HEATER	Yes	Yes	Yes
TEMPERATURE			
SALT CAKE ROTARY FEEDER SPEED			
LIME KILN GREEN LIQUOR SULFIDITY	Yes	Yes	
NITROGEN OXIDES CORRELATION			

# Conclusion

- Primary air temperature is the root cause of SO<sub>2</sub> emission
- Regression tree has the highest accuracy in predicting SO<sub>2</sub> emission from data
- Emission can be reduced if the mill increase primary air temperature and lower black liquor indirect heat temperature
- There is no oscillation in SO<sub>2</sub> emission in the data provided.

# Next Step

- Sensitivity analysis on moving average filter window size
- Random forest maybe able to give better insights into importance of parameters
- Convert normalized prediction back to its units