

Denote

c_i :volumn of client i

v_j :vehicle capacity of vehicle j

f_j :operation fee of vehicle j

$$y_j : y_j = \begin{cases} 1 & \text{if vehicle } j \text{ is put into use} \\ 0 & \text{otherwise} \end{cases}$$

$$Y_{jk} : Y_{jk} = \begin{cases} 1 & \text{if vehicle } j \text{ covers location } k \\ 0 & \text{otherwise} \end{cases}$$

$$\chi_{ij}^V : \chi_{ij}^V = \begin{cases} 1 & \text{if client } i \text{ is assigned to vehicle } j \\ 0 & \text{otherwise} \end{cases}$$

$$\alpha_{ik}^L : \alpha_{ik}^L = \begin{cases} 1 & \text{if client } i \text{ has location } k \text{ as destination} \\ 0 & \text{otherwise} \end{cases}$$

$$\chi_{C(TSP)} : \chi_{C(TSP)} = \begin{cases} 1 & \text{if combination } C \text{ of location is picked} \\ 0 & \text{otherwise} \end{cases}$$

Given c client volumn, v vehicle capacity, f operation fee of each vechicle , α requirement of clients, $C(TSP)$ the outcome of TSP. the goal is to minimize the total cost

$$\text{COST} = \sum_j f_j \cdot y_j$$

while satisfies

$$\chi_{ij}^V + \chi_{i'j}^V = 1 \quad \text{if } i \text{ and } i' \text{ are incompatible}$$

$$\sum_i \chi_{ij}^V = 1$$

$$\sum_j c_i \cdot \chi_{ij}^V \leq v_j \quad v_j \in V$$

$$\sum_{k \in \chi_{C(TSP)}} \chi_{C(TSP)} \leq \alpha_{ik}^L$$

The constraints are based on the following consideration:

0. incompatible clients are 互斥

1. (Each client is required to be picked up by a vehicle
2. (Each client's destination (location) request should be met by any route
3. (Each vehicle's capacity should not be exceeded.

Concerns:

The number of the third constraints could be exponential due to the exponential combination of different locations into different route for a vehicle. (There are ways to handle this).