



# Exercise Sheet 3

Topic: Feature Detectors, Descriptors,  
Epipolar Geometry, RANSAC

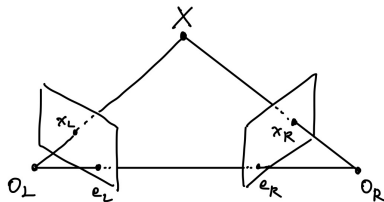
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## Par1: ORB Descriptors

See implementation on GitLab.

## Part 2: Epipolar constraint



We know that the unprojected vector  $x_L, x_R$  are normalized vectors

Let's say the real distance  $\overline{O_L X}, \overline{O_R X}$  are  $\lambda_L$  and  $\lambda_R$

We first assume  $X$  is represented in  $O_R$  camera fr

$$\lambda_R x_R = X \quad \textcircled{1}$$

$$\lambda_L x_L = R_{LR} X + T_{LR} \quad \textcircled{2}$$

Take  $\textcircled{1}$  into  $\textcircled{2}$

$$\Rightarrow \lambda_L x_L = R_{LR} (\lambda_R x_R) + T_{LR}$$

We try to multiply  $\hat{T}_{LR}$  from both side to eliminate  $T_{LR}$

$$\Rightarrow \lambda_L \hat{T}_{LR} x_L = \lambda_R \hat{T}_{LR} R_{LR} x_R$$

From the epipolar constraint,  $O_L x_L, T_{LR}, O_R x_R$  should lie on the same plane, since  $\hat{T}_{LR} x_L = T_{LR} \times x_L \perp x_L$

If we try to compute the inner product of  $x_L$  and  $T_{LR} \times x_L$ , we would get zero since they are perpendicular.

So, by multiplying both side with  $x_L^T$ , we have:

$$\Rightarrow \lambda_L \underbrace{x_L^T (\hat{T}_{LR} x_L)}_{0, \text{ since } x_L \perp (T_{LR} \times x_L)} = \lambda_R \hat{x}_L^T \hat{T}_{LR} R_{LR} x_R$$

$$\Rightarrow x_L^T \hat{T}_{LR} R_{LR} x_R = 0$$

And we define our essential matrix  $E = \hat{T}_{LR} R_{LR}$

$$\Rightarrow x_L^T E x_R = 0 \quad \#$$

## Part 3: Five-point algorithm and RANSAC

See implementation on GitLab.

## Part 4: Bag-of-Words for Place Recognition

The main difference between **match\_all()** and **match\_bow()** is how they determine the vector **ids\_to\_match**. The method **match\_all()** basically adds all the image pairs when two images are not in the same frame. However, the method **match\_bow()** iterates through all the pairs of (FrameCamId, KeypointsData), and for each frame (image), it transforms all the corner descriptors into bag-of-words vector **v**, and then uses **query()** to find a number of candidate frames (images) from the database. In the end, it only adds pair of current frame (image) ID and its candidate frames (images) IDs into vector **ids\_to\_match**, which could reduce lots of unnecessary image pairs. The number of candidate frames (images) is controlled by the parameter **num\_bow\_candidates**.

After successfully implementing the BoW matching method, we now compare the number of candidate pairs and inliers using two different method **match\_all()** and **match\_bow()**.

**match\_all()** has 13284 candidate pairs and about 44336 inliers features, while **match\_bow** has 3649 candidate pairs and about 23938 inliers features (when parameter **num\_bow\_candidates** is set to 25). If now we have 2 x 1000 images, then **match\_all()** would have 1998000 candidate pairs and **match\_bow** would have candidates at some number below 50000 (when parameter **num\_bow\_candidates** is set to 25). It's obvious to see that we can reduce a lot of computational cost when use **match\_bow()** method when dealing with a large number of images.

## References

As suggested in the exercise sheet.