

HW3 Code Part

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Set Up

In [4]:

```
# import library
library(lattice)
library(ggplot2)
library(scales)
```

Warning message:

"package 'ggplot2' was built under R version 3.6.3"

In [5]:

```
# read data
cmv <- read.table('hcmv.txt', header=TRUE)
# check # of rows in data
nrow(cmv)
```

296

In [6]:

```
# initialize the sizes, sites is n, bases is N
sites <- 296
bases <- 229354
```

In [9]:

```
cmv
```

location

177
1321
1433
1477
3248
3255
3286
7263
9023
9084
9333
10884
11754
12863
14263
14719
16013
16425
16752
16812
18009
19176
19325
19415
20030
20832
22027
22739
22910
23241
...
204548
205503
206000
207527
207788
207898
208572

location

209876
210469
215802
216190
216292
216539
217076
220549
221527
221949
222159
222573
222819
223001
223544
224994
225812
226936
227238
227249
227316
228424
228953

Locations (Random Scatter)

Here the goal is to graphically compare your sample palindrome locations to random uniform scatter. To do this, you can visualize the distribution of your sample, the distributions of random uniform scatter instances, and the theoretical uniform distribution. You can visualize the distributions using either histograms or empirical cdfs. Be sure to simulate the random uniform scatter several times (at least 5 times).

In [11]:

```

# Multiple plot function
#
# ggplot objects can be passed in ..., or to plotlist (as a list of ggplot objects)
# - cols: Number of columns in layout
# - layout: A matrix specifying the layout. If present, 'cols' is ignored.
#
# If the layout is something like matrix(c(1,2,3,3), nrow=2, byrow=TRUE),
# then plot 1 will go in the upper left, 2 will go in the upper right, and
# 3 will go all the way across the bottom.
#
# function import from http://www.cookbook-r.com/Graphs/Multiple_graphs_on_one_page_(ggplot2)/
multiplot <- function(..., plotlist=NULL, file, cols=1, layout=NULL) {
  library(grid)

  # Make a list from the ... arguments and plotlist
  plots <- c(list(...), plotlist)

  numPlots = length(plots)

  # If layout is NULL, then use 'cols' to determine layout
  if (is.null(layout)) {
    # Make the panel
    # ncol: Number of columns of plots
    # nrow: Number of rows needed, calculated from # of cols
    layout <- matrix(seq(1, cols * ceiling(numPlots/cols)),
                      ncol = cols, nrow = ceiling(numPlots/cols))
  }

  if (numPlots==1) {
    print(plots[[1]])
  } else {
    # Set up the page
    grid.newpage()
    pushViewport(viewport(layout = grid.layout(nrow(layout), ncol(layout))))

    # Make each plot, in the correct location
    for (i in 1:numPlots) {
      # Get the i,j matrix positions of the regions that contain this subplot
      matchidx <- as.data.frame(which(layout == i, arr.ind = TRUE))

      print(plots[[i]], vp = viewport(layout.pos.row = matchidx$row,
                                       layout.pos.col = matchidx$col))
    }
  }
}

```

In [12]:

```

# convert the data into a vector
loc.vec <- c(cmv$location)

```

In [13]:

`loc.vec`

```
177 1321 1433 1477 3248 3255 3286 7263 9023 9084 9333 10884
11754 12863 14263 14719 16013 16425 16752 16812 18009 19176 19325
19415 20030 20832 22027 22739 22910 23241 25949 28665 30378 30990
31503 32923 34103 34398 34403 34723 36596 36707 38626 40554 41100
41222 42376 43475 43696 45188 47905 48279 48370 48699 51170 51461
52243 52629 53439 53678 54012 54037 54142 55075 56695 57123 60068
60374 60552 61441 62946 63003 63023 63549 63769 64502 65555 65789
65802 66015 67605 68221 69733 70800 71257 72220 72553 74053 74059
74541 75622 75775 75812 75878 76043 76124 77642 79724 83033 85130
85513 85529 85640 86131 86137 87717 88803 89586 90251 90763 91490
91637 91953 92526 92570 92643 92701 92709 92747 92783 92859 93110
93250 93511 93601 94174 95975 97488 98493 98908 99709 100864
102139 102268 102711 104363 104502 105534 107414 108123 109185
110224 113378 114141 115627 115794 115818 117097 118555 119665
119757 119977 120411 120432 121370 124714 125546 126815 127024
127046 127587 128801 129057 129537 131200 131734 133040 134221
135361 136051 136405 136578 136870 137380 137593 137695 138111
139080 140579 141201 141994 142416 142991 143252 143549 143555
143738 146667 147612 147767 147878 148533 148821 150056 151314
151806 152045 152222 152331 154471 155073 155918 157617 161041
161316 162682 162703 162715 163745 163995 164072 165071 165883
165891 165931 166372 168261 168710 168815 170345 170988 170989
171607 173863 174049 174132 174185 174260 177727 177956 178574
180125 180374 180435 182195 186172 186203 186210 187981 188025
188137 189281 189810 190918 190985 190996 191298 192527 193447
193902 194111 195032 195112 195117 195151 195221 195262 195835
196992 197022 197191 198195 198709 201023 201056 202198 204548
205503 206000 207527 207788 207898 208572 209876 210469 215802
216190 216292 216539 217076 220549 221527 221949 222159 222573
222819 223001 223544 224994 225812 226936 227238 227249 227316
228424 228953
```

In [15]:

```
# construct the plot of 2 distributions and theoretical line for 6 times
for(i in 1:6){

  # simulate the random uniform scatter
  sample <- as.integer(runif(sites, min = 1, max=bases))

  # combine the random scatter and original data into one dataframe
  data <- data.frame(
    type = c(rep('original', sites), rep('sample', sites)),
    location = c(loc.vec, sample))

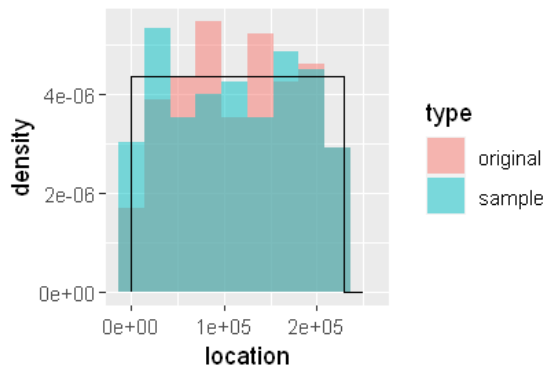
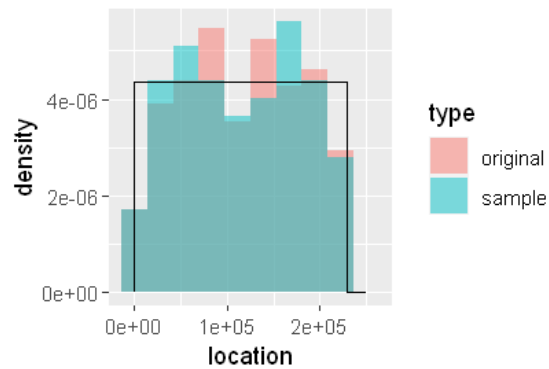
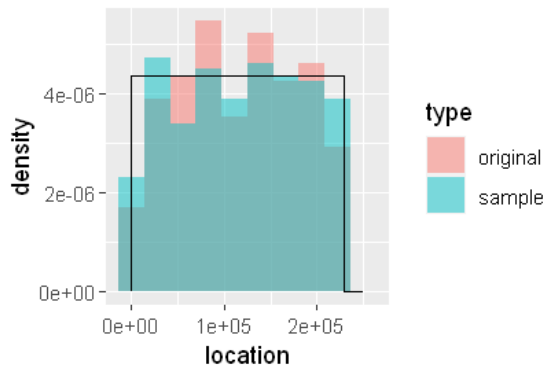
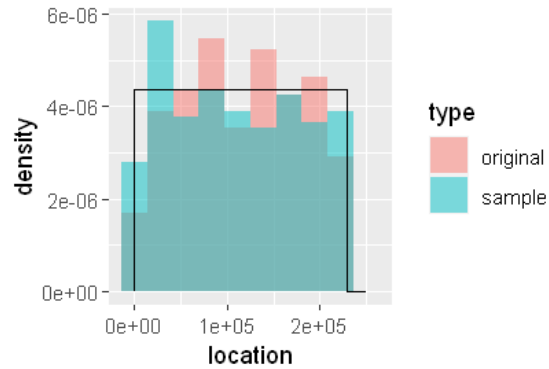
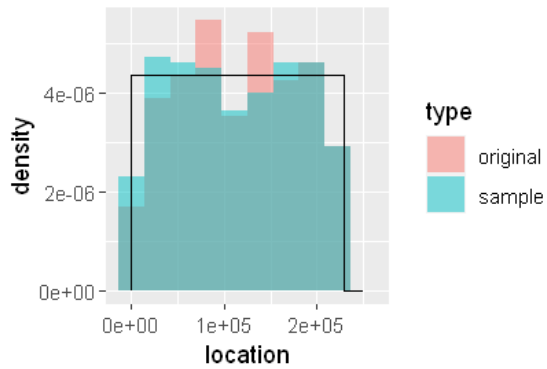
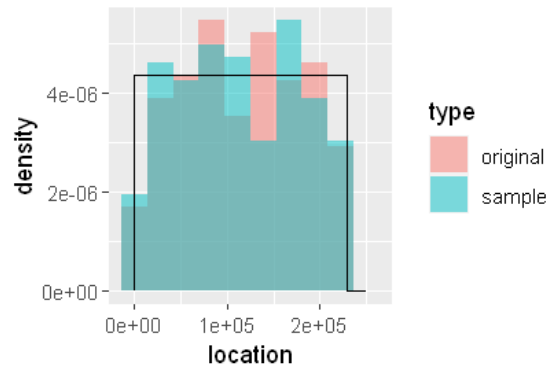
  # calculate the density of theoretical normal distribution
  x <- seq(from=0, to=250000, length.out=250000/2)
  y <- dunif(x, min=1, max=bases)
  unif <- data.frame(x=x, y=y)

  # plot two histograms for distributions + one theoretical distribution density
  plot <- ggplot() +
    geom_histogram(data, mapping=aes(x=location, y=..density.., fill=type), bin
s=10,
    position='identity', alpha=0.5)+
    geom_line(data=unif,mapping=aes(x=x, y=y))

  # save plot
  name <- paste('plot', i, sep='_')
  assign(name, plot)
}
```

In [16]:

```
# combine 6 plots on one canvas  
multiplot(plot_1, plot_2, plot_3, plot_4, plot_5, plot_6, cols=2)
```

In []:

In []:

In []:

In []:

Spacings

Here the goal is to graphically examine the distribution of your sample spacings. There are 3 types of spacings to examine: spacings between consecutive palindromes, spacings between palindromes with one in between (i.e. sums of pairs of consecutive spacings), and spacings between palindromes with two in between (i.e. sums of triplets of consecutive spacings). Next, you can graphically compare these 3 types of spacings to those that come from random uniform scatter (using empirical cdf or histograms). Again, you should simulate at least 5 random uniform scatters. Lastly, using theoretical results discussed in lecture, identify the theoretical distributions of the spacings from random uniform scatter (you won't be expected to know the distribution for the sums of consecutive triplets but it shouldn't be too hard to intuit). Overlay these theoretical distributions as a cdf or density on your plots.

In []:

In []:

Counts

Here the goal is to use graphical and formal statistical methods to examine the counts of palindromes in regions of the DNA. Be sure to do this for a few different (but reasonable) interval lengths. The graphical displays should compare the distribution of counts to random uniform scatter (this will be analogous to the locations and spacings sections). Using results from lecture, you can organize a formal statistical test to further examine your distributions of counts.

In [37]:

```
# create intervals
regionsplit <- function(n.region, gene, site){
  count.int <- table(cut(site, breaks = seq(1, length(gene), length.out=n.region+1), include.lowest=TRUE))
  count.vector <- as.vector(count.int)
  count.tab <- table(factor(count.vector, levels=0:max(count.vector)))
  return (count.tab)
}
```

In [38]:

```
ranges <- c(30, 57, 100)
vectors <- vector(mode = "list", length = 3)
for (i in 1:3){
  vectors[[i]]=regionsplit(ranges[i], gene, data$location)
}
```

Error: \$ operator is invalid for atomic vectors

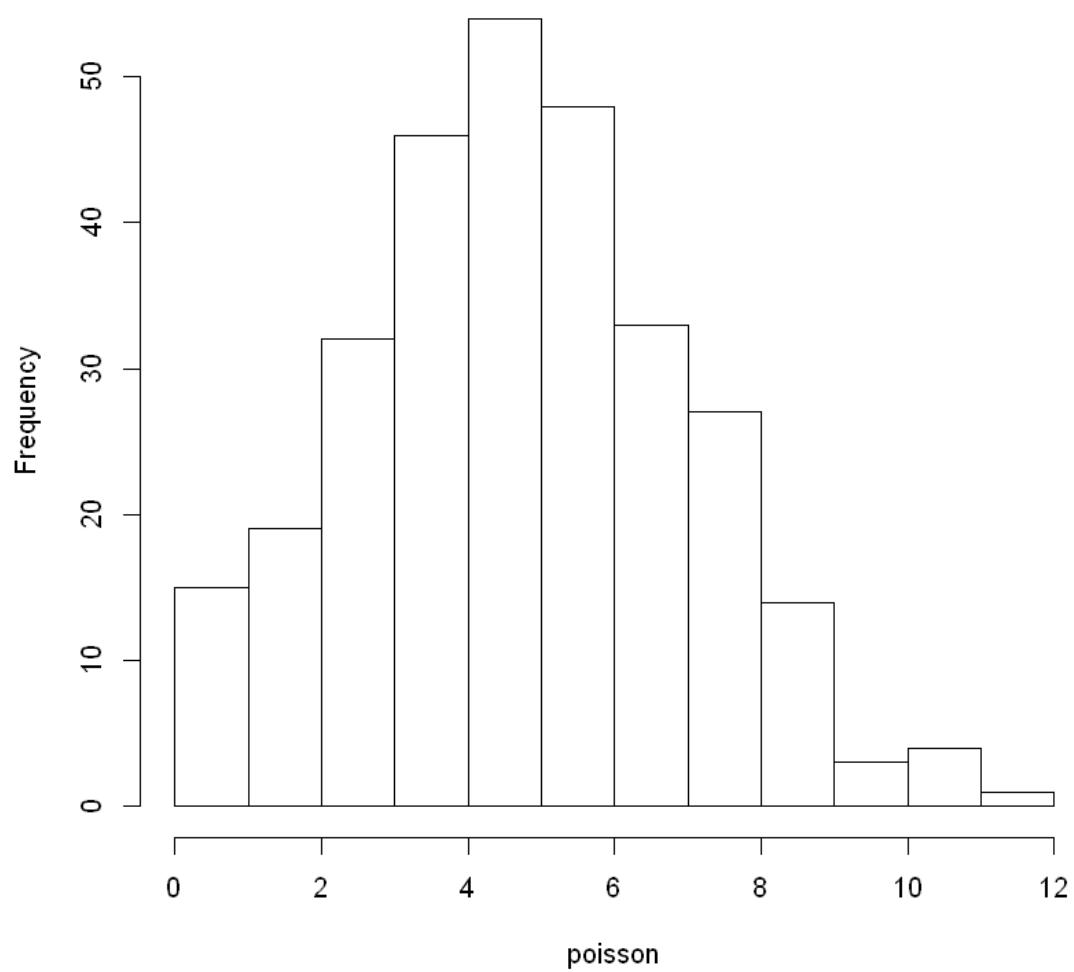
Traceback:

1. regionsplit(ranges[i], gene, data\$location)
2. table(cut(site, breaks = seq(1, length(gene), length.out = n.region + 1), include.lowest = TRUE)) # at line 3 of file <text>
3. cut(site, breaks = seq(1, length(gene), length.out = n.region + 1), include.lowest = TRUE)

In [39]:

```
poisson <- rpois(296, lambda=5)  
hist(poisson)
```

Histogram of poisson



In [40]:

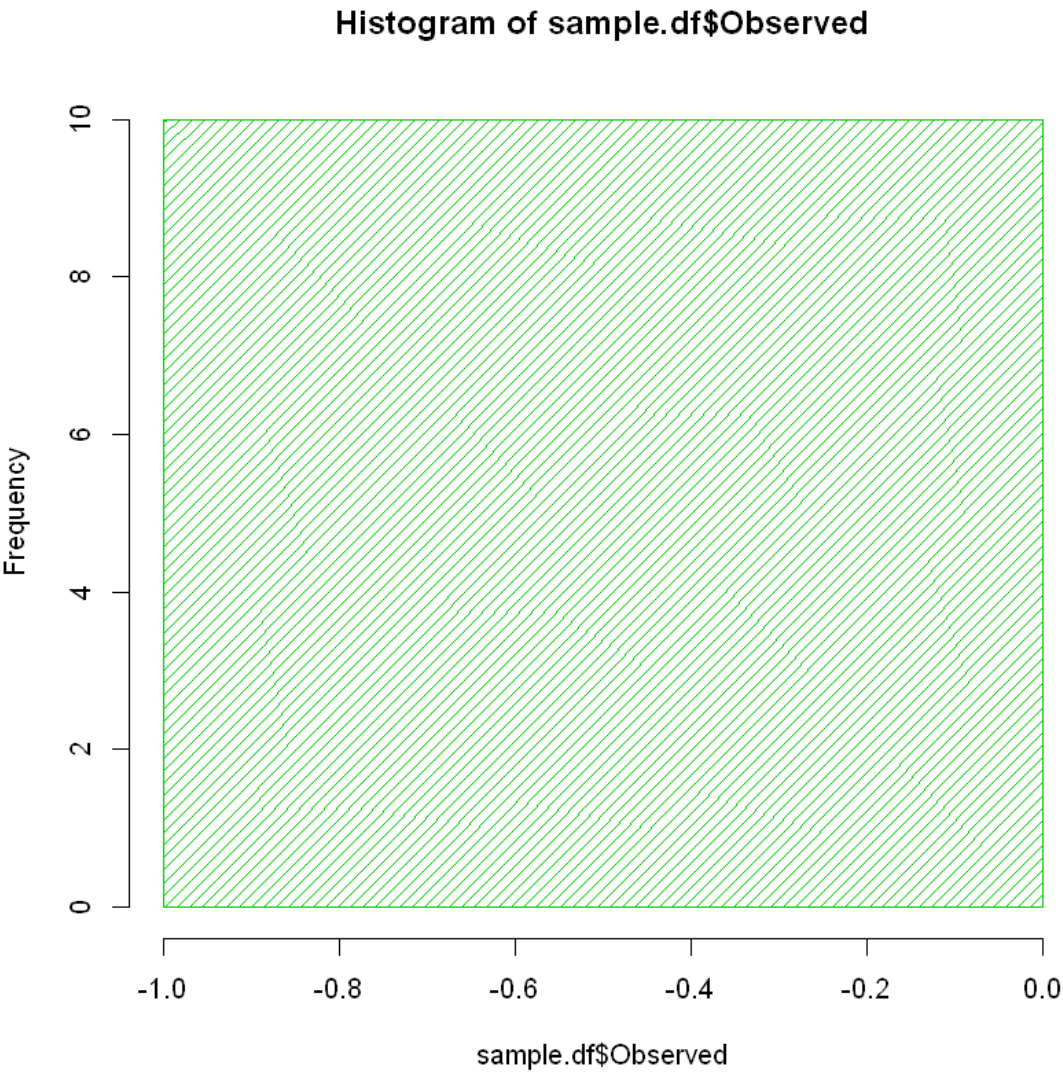
```
#30
trunc=9
lvls=factor(c(0:(trunc-1),paste(">=",trunc,sep="")),levels=c(0:(trunc-1),paste(">=",trunc,sep="")))

sample.vec=as.vector(vectors[[1]])
sample.trunc=c(sample.vec[1:trunc],sum(sample.vec[-(1:trunc)]))
lambda=n/ranges[1]
p=c(dpois(0:(trunc-1),lambda),1-sum(dpois(0:(trunc-1),lambda)))
E=p*ranges[1]
sample.df=data.frame(levels=lvls,Observed=sample.trunc,Expected=E)
hist(sample.df$Observed, breaks=20, probability = FALSE, density = 20, col = 3, border = 3)
print(sample.df)
print(chisq.test(sample.trunc,p=p,simulate.p.value=TRUE))
```

	levels	Observed	Expected
1	0	0	0.001556261
2	1	0	0.015355106
3	2	0	0.075751857
4	3	0	0.249139441
5	4	0	0.614543954
6	5	0	1.212700069
7	6	0	1.994217891
8	7	0	2.810897599
9	8	0	3.466773705
10	>=9	0	19.559064117

Error in chisq.test(sample.trunc, p = p, simulate.p.value = TRUE): at least one entry of 'x' must be positive
Traceback:

1. print(chisq.test(sample.trunc, p = p, simulate.p.value = TRUE))
2. chisq.test(sample.trunc, p = p, simulate.p.value = TRUE)
3. stop("at least one entry of 'x' must be positive")



In []:

```
# 57
trunc=9
lvls=factor(c(0:(trunc-1),paste(">=",trunc,sep="")),levels=c(0:(trunc-1),paste(">=",trunc,sep="")))

sample.vec=as.vector(vectors[[2]])
sample.trunc=c(sample.vec[1:trunc],sum(sample.vec[-(1:trunc)]))
lambda=n/ranges[2]
p=c(dpois(0:(trunc-1),lambda),1-sum(dpois(0:(trunc-1),lambda)))
E=p*ranges[2]
sample.df=data.frame(levels=lvls,Observed=sample.trunc,Expected=E)
hist(sample.df$Observed, breaks=20, probability = FALSE, density = 20, col = 3, border = 3)
print(sample.df)
print(chisq.test(sample.trunc,p=p,simulate.p.value=TRUE))
```

In []:

```
# 100 intervals
``{r}
trunc=9
lvls=factor(c(0:(trunc-1),paste(">=",trunc,sep="")),levels=c(0:(trunc-1),paste(">=",trunc,sep="")))

sample.vec=as.vector(vectors[[3]])
sample.trunc=c(sample.vec[1:trunc],sum(sample.vec[-(1:trunc)]))
lambda=n/ranges[3]
p=c(dpois(0:(trunc-1),lambda),1-sum(dpois(0:(trunc-1),lambda)))
E=p*ranges[3]
sample.df=data.frame(levels=lvls,Observed=sample.trunc,Expected=E)
hist(sample.df$Observed, breaks=20, probability = FALSE, density = 20, col = 3, border = 3)
# df graph
print(sample.df)
# test stat
print(chisq.test(sample.trunc,p=p,simulate.p.value=TRUE))
```

Biggest Cluster

Here the goal is to use randomization or theory to examine the largest cluster of palindromes in a sub-interval. Again, you're expected to try a few different interval sizes. With respect to the randomization, focus on the probability of obtaining, in any subinterval, a count as large or larger than the count you observe in your sample. There is also a theoretical approach to obtaining such a probability. You are free to implement either method.

In [3]:

```
data <- cmv$location  
N <- 229354 #size of DNA chain  
n <- 296 #number of palindromes  
k <- 58 #interval size
```

Error in eval(expr, envir, enclos): 找不到对象'cmv'
Traceback:

In []:

```
choice <- c(200, 2000, 4000, 5000, 10000, 50000)  
intervals <- ceiling(N / choice)  
lambda <- c()  
maxcount <- c()  
p_value <- c()
```

In []:

```

library(hash)
for(k in intervals) {
  dict <- hash()
  count <- as.vector(table(cut(data, breaks = seq(0, N, length.out = k+1), include.lowest = TRUE)))
  lambda <- c(lambda, mean(count))
  maxcount <- c(maxcount, max(count))

  for (i in 0:max(count)) {
    key <- toString(i)
    dict[[key]] <- 0
  }
  key <- toString(max(count)+1)
  dict[[key]] <- 0

  for (i in count) {
    dict[[toString(i)]] <- dict[[toString(i)]] + 1
  }

  observed <- c()
  for (i in 0:max(count)) {
    key <- toString(i)
    observed <- c(observed, dict[[key]])
  }
  observed <- c(observed, dict[[toString(max(count)+1)]])

  expected <- c()
  for (i in 0:max(count)) {
    expected <- c(expected, dpois(i, lambda))
  }
  expected <- c(expected, 1 - sum(expected))

  counts_expected <- expected * k

  chi <- sum((observed - counts_expected)^2 / expected)

  p_value <- c(p_value, pchisq(chi, df = max(count) - 2))
}
result <- data.frame(choice, intervals, lambda, maxcount, p_value)
result

```

In [106]:

```
data <- cmv$location
```

Advanced Analysis

Anything can further help us to answer the question: "How would you advise biologist who is about to start experimental searching for the origin of replication?"

In []:

In []: