# Application of efficient frequency-domain full waveform inversion using time-domain encoded simultaneous sources

Jun, H., Jin, H., Shin, C.

Korea Institute of Ocean Science and Technology, 787, Haean-ro, Snagnok-gu, Ansan, Gyeonggi-do, South Korea

## **Abstract**

Full waveform inversion (FWI) is used to determine accurate subsurface velocities through recursive calculation. FWI needs extensive computation; therefore, reducing the computational cost while inverting for an acceptable result is important for the practical application of FWI. Frequency-domain FWI has the advantages of selection of certain frequency components and reduced computational time because of the use of a matrix solver, which solves many sources simultaneously through one matrix factorization. However, the size of the matrix increases exponentially with the size of the computational domain and the number of parameters. The efficiency of frequency-domain FWI decreases in 3D FWI because of limited computational memory. To enhance the efficiency of frequency-domain FWI, time-domain modeling with a simultaneous source was exploited in this study. Although the time-domain modeling scheme is one of the most efficient methods for performing 3D frequency-domain FWI, it still requires time-marching for every source. However, the efficiency can be greatly improved by using the simultaneous source method. Moreover, this method is not limited by the amount of memory required because the time-domain modeling scheme is a matrixfree method. To suppress the crosstalk noise in the simultaneous source method, we use random phase (RP) encoding. random time delay (RTD), and the partial-source assembling method. The nonlinear conjugate gradient method (NLCG) is also used to accelerate the convergence speed. To validate the efficiency of the proposed algorithm, a numerical test is conducted using the 2D SEG/EAGE overthrust model and shows that determining the appropriate balance between the computational cost and the quality of the result can improve the efficiency of the encoded simultaneous source FWI (ESSFWI). The 3D numerical test also verified that the proposed algorithm enhances the computational efficiency and guarantees the quality of the inverted result. © 2017 Geophysical Press Ltd.

| Author keywords             |  |         |
|-----------------------------|--|---------|
| Encoded simultaneous source | Frequency domain Full waveform inversion Time domain |         |
| Funding details             |  |         |
| Funding number              | Funding sponsor                                      | Acronym |
| PE99534                     | Korea Institute of Ocean Science and Technology      | KIOST   |

### Funding text

This work was supported by the Energy Efficiency & Resources CoreTechnology Program (No. 20132510100060) of the Korea Institute of Energy Technology Evaluation and Planning (KETEP), and by the Korea Institute of Ocean Science and Technology (Grant No. PE99534), and granted financial resource from the Ministry of Trade, Industry & Energy, Republic of Korea.

ISSN: 09630651 Source Type: Journal Original language: English Document Type: Article Publisher: Geophysical Press LTD.

# References

Anagaw, A.Y., Sacchi, M.D.

Comparison of multifrequency selection strategies for simultaneous-source full-waveform inversion (2013) Geophysics, 79 (5), pp. R165-R181.

DOI: 10.1190/GEO2013-0263.1

Ben-Hadj-Ali, H., Operto, S., Virieux, J.

An efficient frequency-domain full waveform inversion method using simultaneous encoded sources (2011) Geophysics, 76 (4), pp. R109-R124.

DOI: 10.1190/1.3581357

Berkhout, A.J.L., Blacquière, G.L. 3)

> Blended acquisition with dispersed source arrays, the next step in seismic acquisition?(2011) SEG Technical Program Expanded Abstracts, 30 (1), pp. 16-19.

DOI: 10.1190/1.3627532

Boonyasiriwat, C., Schuster, G.T. 4)

> 3D multisource full-waveform inversion using dynamic random phase encoding (2010) 80th Ann. Internat. SEG Mtg.

Brossier, R., Operto, S., Virieux, J.

Seismic imaging of complex onshore structures by 2D elastic frequency-domain full-waveform inversion

(2009) Geophysics, 74 (6), pp. WCC105-WCC118.

DOI: 10.1190/1.3215771





Butzer, S., Kurzmann, A., Bohlen, T. 3D elastic full-waveform inversion of small-scale heterogeneities in transmission geometry (2013) Geophysical Prospecting, 61 (6), pp. 1238-1251.

DOI: 10.1111/1365-2478.12065

- Fletcher, R., Reeves, C.M. 7) Function minimization by conjugate gradients (1964) Comput. J., 7 (2), pp. 149-154.
- Jun, H., Kim, Y., Shin, J., Shin, C., Min, D.-J. Laplace-fourier-domain elastic full-waveform inversion using time-domain modeling (2013) Geophysics, 79 (5), pp. R195-R208.

DOI: 10.1190/GEO2013-0283.1

Jun, H., Park, E., Shin, C. 9) Weighted pseudo-Hessian for frequency-domain elastic full waveform inversion (2015) Journal of Applied Geophysics, 123, pp. 1-17.

DOI: 10.1016/j.jappgeo.2015.09.014

10) Jeong, W., Pyun, S., Son, W., Min, D.-J. A numerical study of simultaneous-source full waveform inversion with I1-norm (2013) Geophysical Journal International, 194 (3), pp. 1727-1737.

DOI: 10.1093/gji/ggt182





- Krebs, J.R., Anderson, J.E., Hinkley, D., Baumstein, A., Lee, S., Neelamani, R., Lacasse, M.-D.
   Fast full wave seismic inversion using source encoding
   (2009) SEG Technical Program Expanded Abstracts, 28 (1), pp. 2273-2277.
- 12) Kim, Y., Shin, C., Calandra, H., Min, D.-J.

  An algorithm for 3D acoustic time-Laplace-Fourier-domain hybrid full waveform inversion (2013) Geophysics, 78 (4), pp. R151-R166.

- Marquardt, D.W.

  An algorithm for least-squares estimation of nonlinear parameters (1963) J. Soc. Ind. Appl. Math., 11 (2), pp. 431-441.
- 14) Plessix, R.-E.

A review of the adjoint-state method for computing the gradient of a functional with geophysical applications

(2006) Geophysical Journal International, 167 (2), pp. 495-503.

DOI: 10.1111/j.1365-246X.2006.02978.x

15) Plessix, R.-É.

Three-dimensional frequency-domain full-waveform inversion with an iterative solver (2009) Geophysics, 74 (6), pp. WCC149-WCC157.

DOI: 10.1190/1.3211198

Pyun, S., Son, W., Shin, C.
 3D acoustic waveform inversion in the Laplace domain using an iterative solver (2011) Geophysical Prospecting, 59 (3), pp. 386-399.

167



Romero, L.A., Ghiglia, D.C., Ober, C.C., Morton, S.A. 17) Phase encoding of shot records in prestack migration (2000) Geophysics, 65 (2), pp. 426-436.

Schiemenz, A., Igel, H.

Accelerated 3-D full-waveform inversion using simultaneously encoded sources in the time domain: Application to Valhall ocean-bottom cable data (2013) Geophysical Journal International, 195 (3), pp. 1970-1988.

Schuster, G.T., Wang, X., Huang, Y., Dai, W., Boonyasiriwat, C. Theory of multisource crosstalk reduction by phase-encoded statics (2011) Geophysical Journal International, 184 (3), pp. 1289-1303.

Shin, C., Jang, S., Min, D.-J. 20) Improved amplitude preservation for prestack depth migration by inverse scattering theory (2001) Geophysical Prospecting, 49 (5), pp. 592-606.

Sirgue, L., Etgen, J.T., Albertin, U. 3D frequency domain waveform inversion using time domain finite difference methods (2008) 70th EAGE Conf., p. F022.

168

22) Vigh, D., Starr, E.W., Kapoor, J.

# Developing Earth models with full waveform inversion

(2009) Leading Edge (Tulsa, OK), 28 (4), pp. 432-435.

DOI: 10.1190/1.3112760

23) Xu, K., McMechan, G.A.

2D frequency-domain elastic full-waveform inversion using time-domain modeling and a multistep-length gradient approach

(2013) Geophysics, 79 (2), pp. R41-R53.

DOI: 10.1190/GEO2013-0134.1

24) Yang, J.Z., Liu, Y.Z., Dong, L.G.

Time-windowed frequency domain full waveform inversion using Phase-encoded Simultaneous Sources

(2013) 75th European Association of Geoscientists and Engineers Conference and Exhibition 2013

Incorporating SPE EUROPEC 2013: Changing Frontiers, pp. 3623-3627.



169