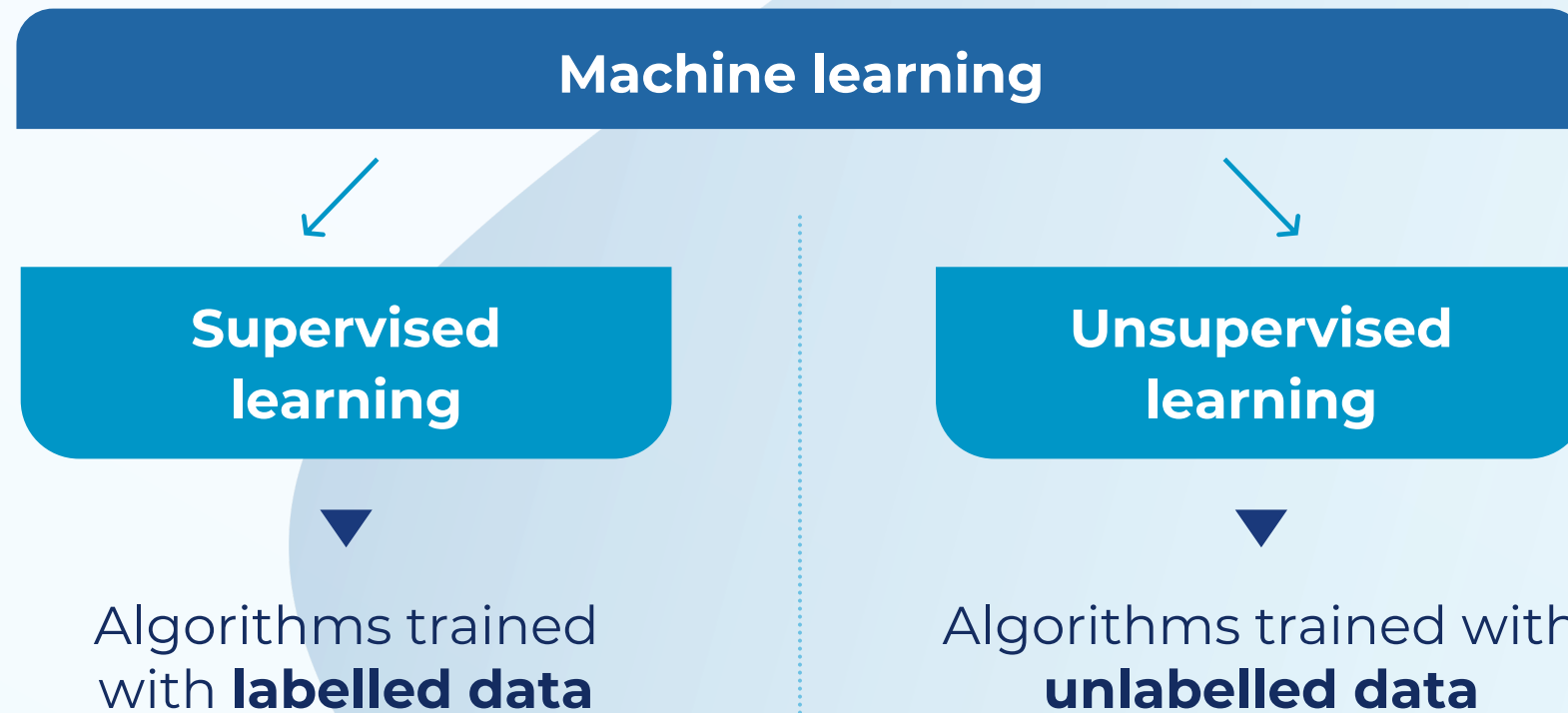
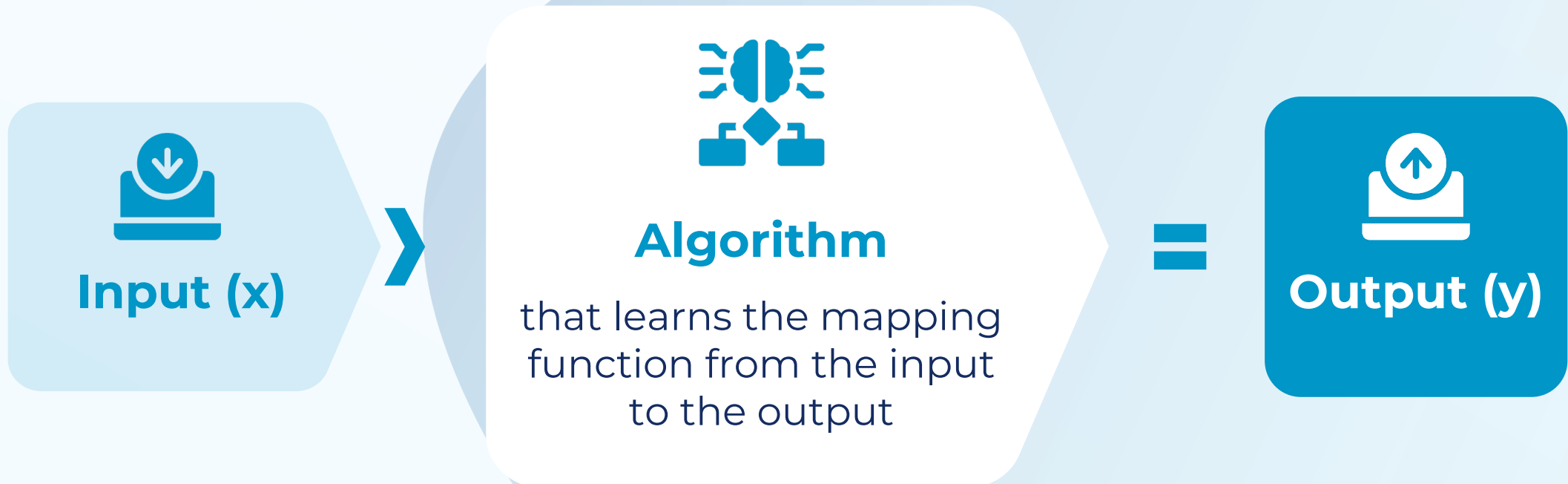


Machine learning is divided into two main categories



How does supervised learning work?



A supervised learning technique: regression



How does regression work?

- Regression models use an algorithm to understand the relationship between **a dependent variable** (input) and **an independent variable** (output).
- They are helpful for **predicting numerical values** based on different features' values. E.g., temperature forecast based on wind, humidity and pressure.

Regression aims

to build a relationship between each feature and the output for predictions

Linear relationships ► Linear regression

Linear regression uses a best fitting straight line – “**regression line**”

$$y = wX + b$$

dependent
variable

weight; the slope
of the gradient of
the line - indicates
the impact X has
on Y

independent
variable; used
to predict the
value of Y

Bias; is the
value of Y when
there is no X or
X is zero

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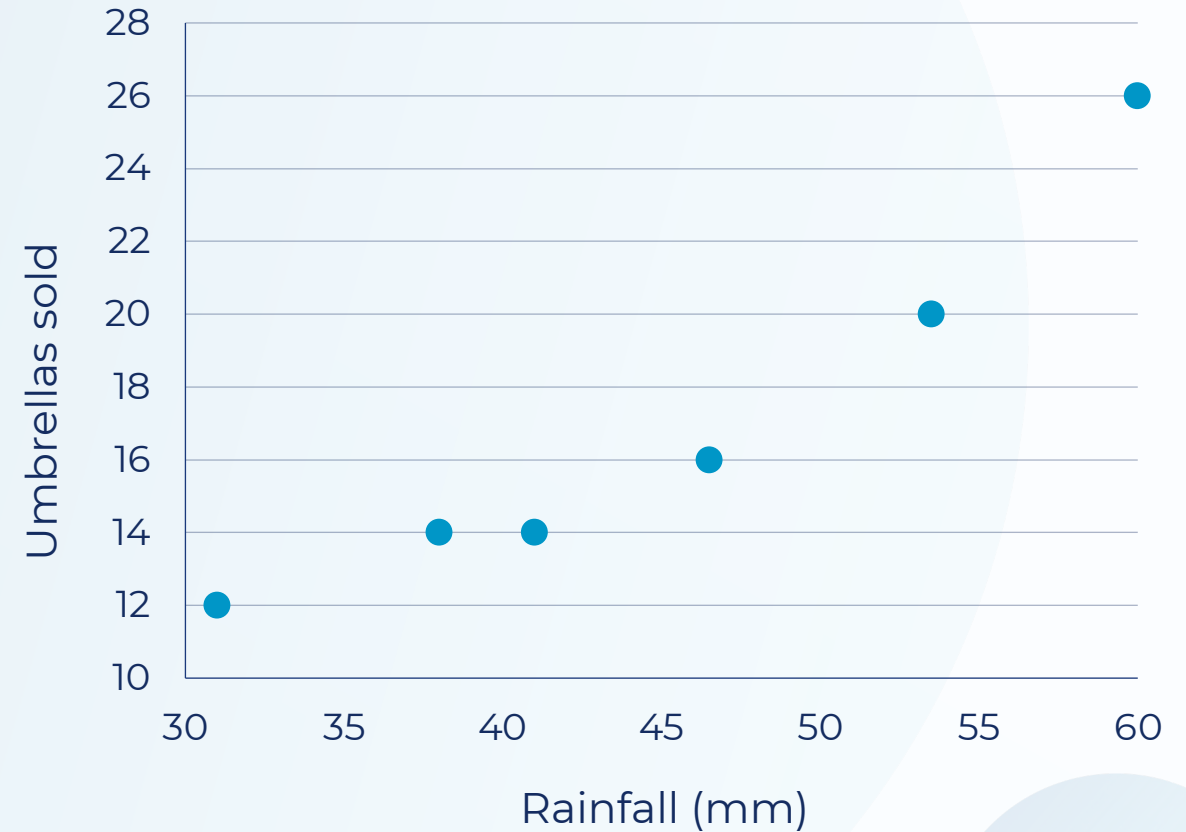
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A simple linear regression model

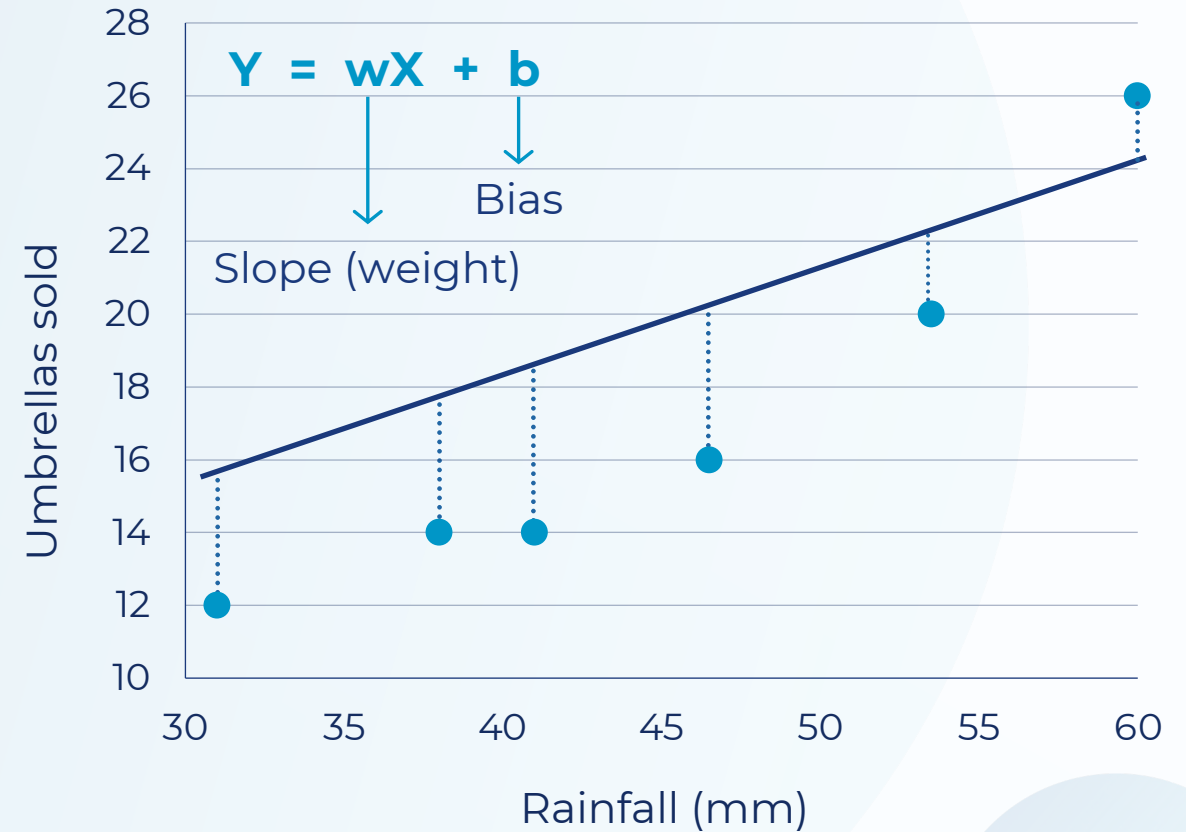
Simple linear regression only has one Y variable and one X variable:

- **The independent variable x:**
rainfall measured in millimeters
- **The dependent variable y:**
the number of umbrellas sold
- We can predict the number of umbrellas, or Y, for any quantity of rain.



How can we calculate the regression line?

- 1 We draw a line to represent the relationship
- 2 We measure the distances between the line and each datapoint (the residuals)
- 3 We sum up the residuals
- 4 We adjust the weight & the bias to minimize this sum



Multiple features call for multiple linear regression

Multiple features ► Multiple linear regression

The aim is to **predict output variable** using multiple features

$$y = w_1x_1 + w_2x_2 + \dots + b$$

-
- Multiple linear regression can have many independent variables to one dependent variable
 - Datasets with multiple features like the number of bedrooms, age of the building, covered area, etc.

How can we evaluate the performance of a regression model?



We use performance evaluation metrics

The most commonly used evaluation metrics is taking the difference between predicted and actual value of some test points:

- The mean of the squared difference is taken – **Mean Squared Error (MSE)**
- The size of the error is measured by taking the square root of MSE - **Root Mean Squared Error (RMSE)**

Evaluating the performance of a regression model using MSE & RMSE

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

$$\text{RMSE} = \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2}$$

MSE = Mean squared error
 n = Number of data points

y_i = Observed values
 \hat{y}_i = Predicted values