Extra Project

Yunxuan

2022-12-09

```
Cars <- read.table("cars.txt", head = T)</pre>
nrow(Cars)
## [1] 32
Cars
##
                                cyl
                                      disp hp drat
                                                            qsec vs
                                                                     am
                                                                             carb
##
                 Mazda RX4 21.0
                                   6 160.0 110 3.90 2.620 16.46
                                                                           4
                                                                                 4
                                                                                 4
## 2
                                   6 160.0 110 3.90 2.875 17.02
                                                                            4
            Mazda RX4 Wag 21.0
## 3
                Datsun 710 22.8
                                   4 108.0
                                            93 3.85 2.320 18.61
                                                                           4
                                                                                 1
                                    258.0 110 3.08 3.215
## 4
           Hornet 4 Drive 21.4
                                                           19.44
                                                                           3
                                                                                 1
## 5
        Hornet Sportabout 18.7
                                   8 360.0 175 3.15 3.440 17.02
                                                                   0
                                                                           3
                                                                                 2
##
                   Valiant 18.1
                                   6 225.0 105 2.76 3.460 20.22
                                                                           3
                                                                                 1
##
  7
               Duster 360 14.3
                                   8 360.0 245 3.21 3.570 15.84
                                                                           3
                                                                                 4
                                                                                 2
##
  8
                 Merc 240D 24.4
                                   4 146.7
                                            62 3.69 3.190 20.00
                                                                           4
## 9
                  Merc 230 22.8
                                   4 140.8
                                            95 3.92 3.150 22.90
                                                                           4
                                                                                 2
## 10
                  Merc 280 19.2
                                   6 167.6 123 3.92 3.440 18.30
                                                                                 4
## 11
                 Merc 280C 17.8
                                   6 167.6 123 3.92 3.440 18.90
                                                                           4
                                                                                 4
##
  12
                Merc 450SE 16.4
                                   8 275.8 180 3.07 4.070 17.40
                                                                           3
                                                                                 3
## 13
               Merc 450SL 17.3
                                   8 275.8 180 3.07 3.730 17.60
                                                                           3
                                                                                 3
               Merc 450SLC 15.2
                                   8 275.8 180 3.07 3.780 18.00
                                                                           3
                                                                                 3
##
  14
       Cadillac Fleetwood 10.4
                                   8 472.0 205 2.93 5.250 17.98
                                                                           3
                                                                                 4
##
   15
##
   16
      Lincoln Continental 10.4
                                   8 460.0 215 3.00 5.424 17.82
                                                                           3
                                                                                 4
                                                                           3
                                                                                 4
##
  17
        Chrysler Imperial 14.7
                                   8 440.0 230 3.23 5.345 17.42
## 18
                  Fiat 128 32.4
                                      78.7
                                             66 4.08 2.200 19.47
                                                                            4
                                                                                 1
                                      75.7
## 19
               Honda Civic 30.4
                                            52 4.93 1.615 18.52
                                                                           4
                                                                                 2
##
   20
           Toyota Corolla 33.9
                                      71.1
                                            65 4.22 1.835 19.90
                                                                           4
                                                                                 1
##
   21
            Toyota Corona 21.5
                                   4 120.1
                                            97 3.70 2.465 20.01
                                                                           3
                                                                                 1
##
   22
         Dodge Challenger 15.5
                                   8 318.0 150 2.76 3.520 16.87
                                                                           3
                                                                                 2
                                                                                 2
##
  23
               AMC Javelin 15.2
                                   8 304.0 150 3.15 3.435 17.30
                                                                   0
                                                                           3
##
  24
                Camaro Z28 13.3
                                   8 350.0 245 3.73 3.840 15.41
                                                                   0
                                                                           3
                                                                                 4
                                                                                 2
                                   8 400.0 175 3.08 3.845 17.05
                                                                           3
## 25
         Pontiac Firebird 19.2
## 26
                 Fiat X1-9 27.3
                                      79.0
                                            66 4.08 1.935 18.90
                                                                           4
                                                                                 1
##
  27
            Porsche 914-2 26.0
                                   4 120.3
                                            91 4.43 2.140 16.70
                                                                           5
                                                                                 2
                                      95.1 113 3.77 1.513 16.90
                                                                                 2
##
  28
             Lotus Europa 30.4
                                                                           5
   29
           Ford Pantera L 15.8
                                   8 351.0 264 4.22 3.170 14.50
                                                                                 4
                                   6 145.0 175 3.62 2.770 15.50
                                                                           5
                                                                                 6
##
  30
             Ferrari Dino 19.7
## 31
            Maserati Bora 15.0
                                   8 301.0 335 3.54 3.570 14.60
                                                                           5
                                                                                 8
                                   4 121.0 109 4.11 2.780 18.60
                                                                                 2
## 32
                Volvo 142E 21.4
                                                                            4
```

1. Partition the data set into two sets a training data and a test data. Remove every fifth observation from the data for use as a test sample.

There are 32 observations. So the set test will contain 6 observations and the set train will contain 32-6=26

observations.

```
c<- 1:nrow(Cars)
train <- Cars[!c%%5==0,]
test <- Cars[c%%5==0,]
nrow(train)
## [1] 26
nrow(test)</pre>
```

[1] 6

2. Perform an exploratory analysis. Comment on your findings.

```
library(ggplot2)
library(cowplot)
library(ISLR)

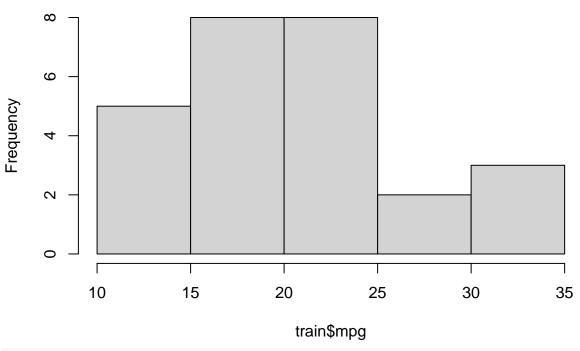
cars <- train[, -c(1,3,9,10)]
summary(cars)</pre>
```

```
##
        mpg
                        disp
                                         hp
                                                        drat
##
                                        : 52.0
                                                          :2.760
   Min.
         :10.40
                   Min.
                        : 75.7
                                   Min.
                                                   Min.
##
   1st Qu.:15.28
                   1st Qu.:120.5
                                   1st Qu.: 95.5
                                                   1st Qu.:3.098
## Median :19.55
                                                   Median :3.715
                   Median :196.3
                                   Median :111.5
##
  Mean
         :20.07
                   Mean :221.8
                                   Mean
                                         :145.2
                                                   Mean :3.622
##
   3rd Qu.:22.80
                   3rd Qu.:303.2
                                   3rd Qu.:180.0
                                                   3rd Qu.:3.920
##
  Max.
          :32.40
                   Max.
                          :460.0
                                   Max.
                                          :335.0
                                                   Max.
                                                          :4.930
                                        gear
##
         wt
                        qsec
                                                        carb
## Min.
          :1.513
                   Min.
                          :14.50
                                          :3.000
                                                          :1.000
                                   Min.
                                                   Min.
  1st Qu.:2.504
                   1st Qu.:16.88
                                   1st Qu.:3.000
                                                   1st Qu.:2.000
## Median :3.203
                                   Median :4.000
                                                   Median :2.000
                   Median :17.71
## Mean
         :3.168
                   Mean
                          :17.90
                                   Mean
                                          :3.692
                                                   Mean
                                                          :2.731
## 3rd Qu.:3.570
                   3rd Qu.:18.90
                                   3rd Qu.:4.000
                                                   3rd Qu.:4.000
          :5.424
                          :22.90
                                          :5.000
                                                          :8.000
## Max.
                   Max.
                                   Max.
                                                   Max.
pairs(cars[,c("mpg","disp","hp","drat","wt","qsec","gear","carb")],col="darkgreen",pch=20)
```

```
100
                  400
                                 3.0
                                      4.5
                                                      16 20
    mpg
               disp
                                                      qsec
                                                                                   5.0
                                                                gear
                                                                          carb
  10 20 30
                      50 200
                                            2
                                               4
                                                              3.0 4.0 5.0
cor(cars[,c("mpg","disp","hp","drat","wt","qsec","gear","carb")])
##
                          disp
                                         hp
                                                    drat
               mpg
## mpg
         1.00000000 \ -0.8879788 \ -0.77751430 \ \ 0.66124336 \ -0.8592776 \ \ 0.40733515
## disp -0.8879788 1.0000000 0.82413517 -0.65054746 0.8889453 -0.48080537
## hp
        -0.7775143 \quad 0.8241352 \quad 1.00000000 \quad -0.38749899 \quad 0.6489729 \quad -0.70529394
## drat 0.6612434 -0.6505475 -0.38749899 1.00000000 -0.6853894 0.02358719
        -0.8592776 \quad 0.8889453 \quad 0.64897286 \quad -0.68538941 \quad 1.0000000 \quad -0.16302267
## qsec 0.4073352 -0.4808054 -0.70529394 0.02358719 -0.1630227 1.00000000
## gear 0.5113112 -0.4801054 -0.09115853 0.70791536 -0.5747590 -0.21560113
## carb -0.5623724 0.5332080 0.80794216 -0.07828427 0.4678306 -0.66441318
##
                            carb
                gear
## mpg
         0.51131118 -0.56237236
## disp -0.48010537 0.53320804
        -0.09115853 0.80794216
## hp
## drat 0.70791536 -0.07828427
        -0.57475897
                     0.46783065
## qsec -0.21560113 -0.66441318
## gear 1.00000000
                      0.19999446
## carb 0.19999446 1.00000000
```

We see that predictors such as mpg, disp and hp has a relationship between each other, as the graph shows. hist(train\$mpg)

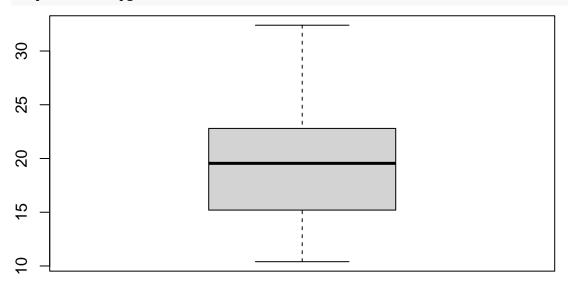
Histogram of train\$mpg



summary(train\$mpg)

Min. 1st Qu. Median Mean 3rd Qu. Max. ## 10.40 15.28 19.55 20.07 22.80 32.40

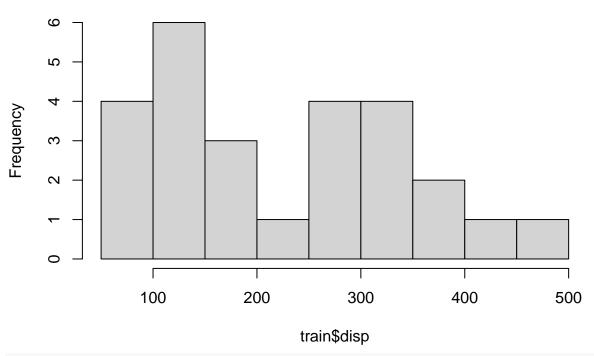
boxplot(train\$mpg)



For mpg, most values are in the interval [15,28,22,80]. There is no outlier. The values are comparatively concentrated.

hist(train\$disp)

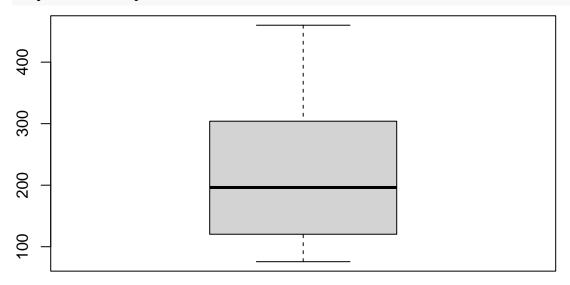
Histogram of train\$disp



summary(train\$disp)

Min. 1st Qu. Median Mean 3rd Qu. Max. ## 75.7 120.5 196.3 221.8 303.2 460.0

boxplot(train\$disp)



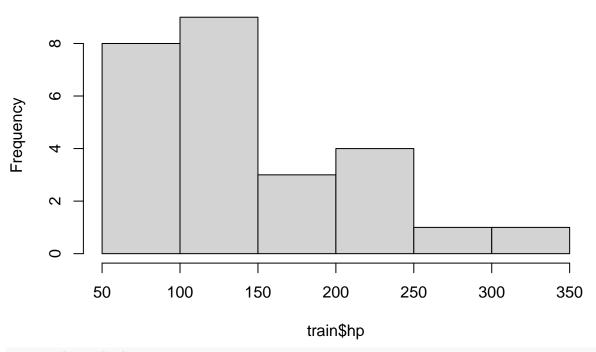
For disp, most values are in the interval [120.5,303.2]. There is no outlier. The values are comparatively scattered.

summary(train\$cyl)

Min. 1st Qu. Median Mean 3rd Qu. Max. ## 4.000 4.000 6.000 6.077 8.000 8.000 For cyl, the number of getting 6 cyl is the least while the number of getting 8 cyl is the most.

hist(train\$hp)

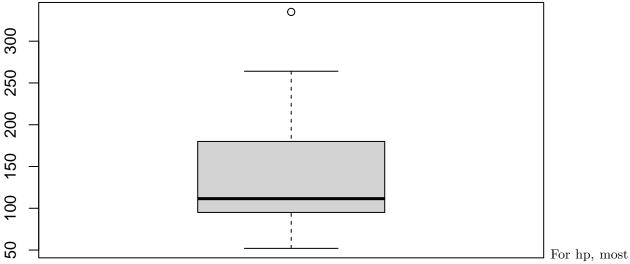
Histogram of train\$hp



summary(train\$hp)

Min. 1st Qu. Median Mean 3rd Qu. Max. ## 52.0 95.5 111.5 145.2 180.0 335.0

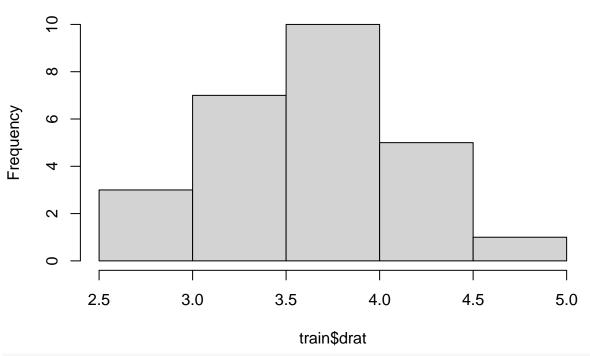
boxplot(train\$hp)



values are in the interval [95.5,180]. There is an outlier, but we should keep it. The values are comparatively scattered.

hist(train\$drat)

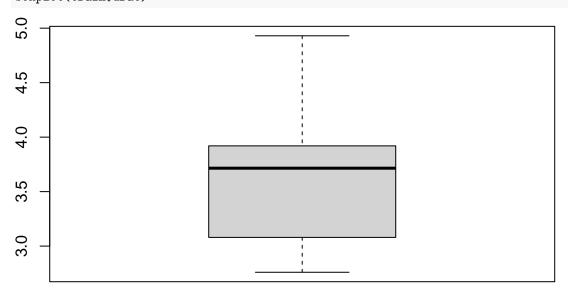
Histogram of train\$drat



summary(train\$drat)

Min. 1st Qu. Median Mean 3rd Qu. Max. ## 2.760 3.098 3.715 3.622 3.920 4.930

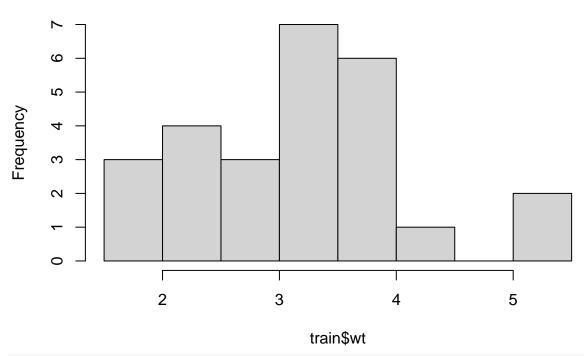
boxplot(train\$drat)



For drat, most values are in the interval [3.098, 3.920]. There is no outlier. The values are comparatively concentrated.

hist(train\$wt)

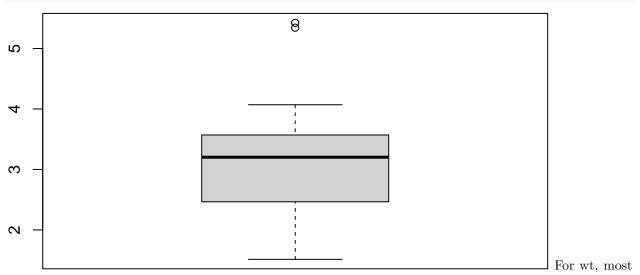
Histogram of train\$wt



summary(train\$wt)

Min. 1st Qu. Median Mean 3rd Qu. Max. ## 1.513 2.504 3.203 3.168 3.570 5.424

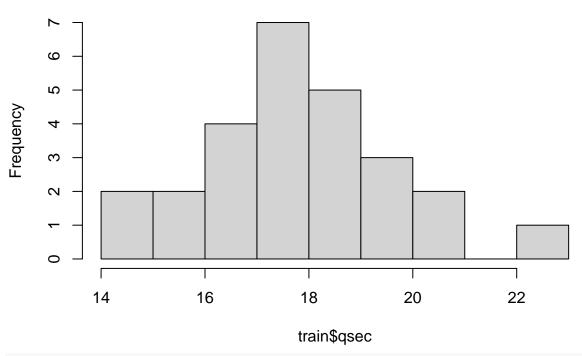
boxplot(train\$wt)



values are in the interval [2.5,3.6]. There are two outliers, but we should keep them.

hist(train\$qsec)

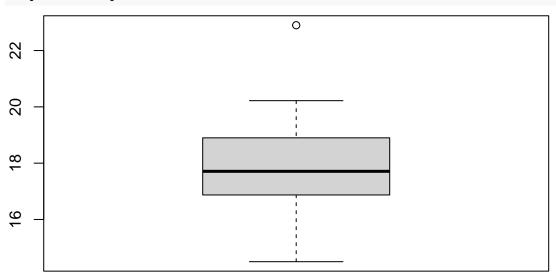
Histogram of train\$qsec



summary(train\$qsec)

Min. 1st Qu. Median Mean 3rd Qu. Max. ## 14.50 16.88 17.71 17.90 18.90 22.90

boxplot(train\$qsec)



For qsec, most values are in the interval [17,19]. There is an outlier, but we should keep it. The values are comparatively concentrated.

summary(train\$vs)

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 0.0000 0.0000 0.0000 0.4615 1.0000 1.0000
```

The number of being 0 is a little bit more than number being 1 for vs.

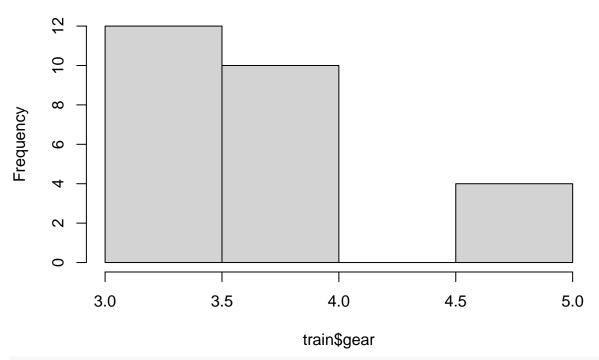
summary(train\$am)

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 0.0000 0.0000 0.0000 0.4231 1.0000 1.0000
```

The number of being 0 is a little bit more than number being 1 for am.

hist(train\$gear)

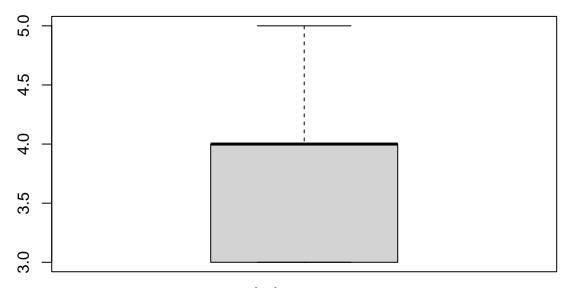
Histogram of train\$gear



summary(train\$gear)

Min. 1st Qu. Median Mean 3rd Qu. Max. ## 3.000 3.000 4.000 3.692 4.000 5.000

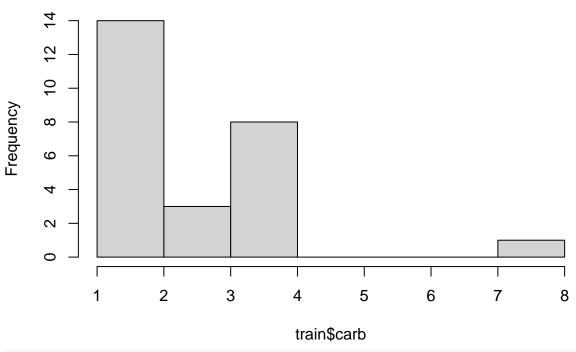
boxplot(train\$gear)



For gear, most values are in the interval [3,4]. There is no outlier.

hist(train\$carb)

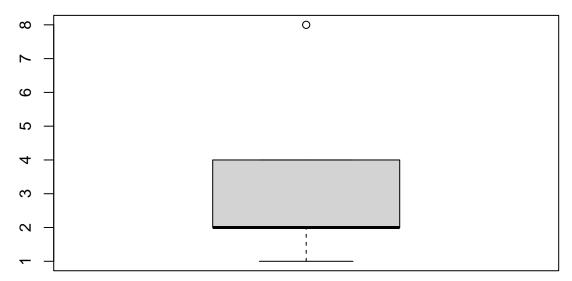
Histogram of train\$carb



summary(train\$carb)

Min. 1st Qu. Median Mean 3rd Qu. Max. ## 1.000 2.000 2.000 2.731 4.000 8.000

boxplot(train\$carb)



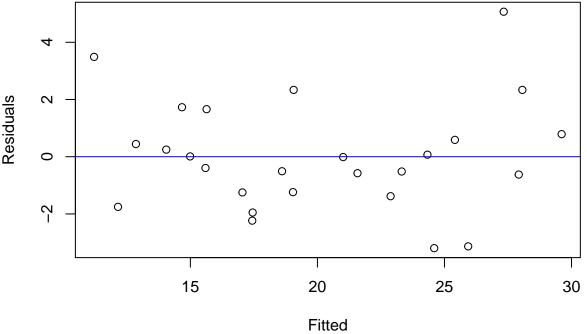
For carb, most values are in the interval [2,4]. There is an outlier, but we should keep it. The distribution is comparatively concentrated.

- 3. Perform a regression analysis and come up with the best multiple linear regression model that explains the response mpg in terms of the rest (except name). Comment on your findings and explain the methods and strategies that you employed in order to select the model you picked. Things you have to include in this part:
- Model diagnostics
- Justification on whether it is necessary or not to do any transformation on the response or the predictors
- Variable selection

```
lmod1 <- lm(mpg ~ factor(cyl)+disp+hp+drat+wt+qsec+factor(vs)+factor(am)+gear+carb, data=train)
summary(lmod1)</pre>
```

```
##
## Call:
   lm(formula = mpg ~ factor(cyl) + disp + hp + drat + wt + qsec +
##
       factor(vs) + factor(am) + gear + carb, data = train)
##
##
   Residuals:
##
##
       Min
                 1Q Median
                                  3Q
                                          Max
   -3.1964 -1.2457 -0.2034
##
                             0.7388
                                      5.0684
##
##
  Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
   (Intercept)
                25.33640
                             17.38473
                                        1.457
                                                  0.167
## factor(cyl)6 -2.85871
                              2.48654
                                       -1.150
                                                  0.270
## factor(cyl)8 -0.66735
                              4.66762
                                       -0.143
                                                  0.888
                              0.02283
                                        0.489
                                                  0.632
## disp
                  0.01117
## hp
                 -0.04869
                              0.03021
                                       -1.611
                                                  0.129
                                       -0.260
                                                  0.799
## drat
                 -0.48406
                              1.86041
## wt
                 -2.71321
                              2.16587
                                       -1.253
                                                  0.231
                                        0.276
                                                  0.787
                  0.22852
                              0.82846
##
   qsec
  factor(vs)1
##
                  1.94056
                              2.50451
                                        0.775
                                                  0.451
## factor(am)1
                  2.25309
                              2.30330
                                        0.978
                                                  0.345
## gear
                  0.73942
                              1.51024
                                        0.490
                                                  0.632
                                        0.650
                                                  0.526
##
  carb
                  0.67277
                              1.03493
##
```

```
## Residual standard error: 2.592 on 14 degrees of freedom
## Multiple R-squared: 0.8877, Adjusted R-squared: 0.7995
## F-statistic: 10.06 on 11 and 14 DF, p-value: 7.337e-05
Diagnostic Test: 1. Check Error Assumptions 1i. Check Constant Variance.
require(lmtest)
## Loading required package: lmtest
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
       as.Date, as.Date.numeric
require(MASS)
## Loading required package: MASS
require(ggplot2)
plot(fitted(lmod1),residuals(lmod1),xlab='Fitted',ylab='Residuals')
abline(h=0, col="blue")
                                                                         0
```



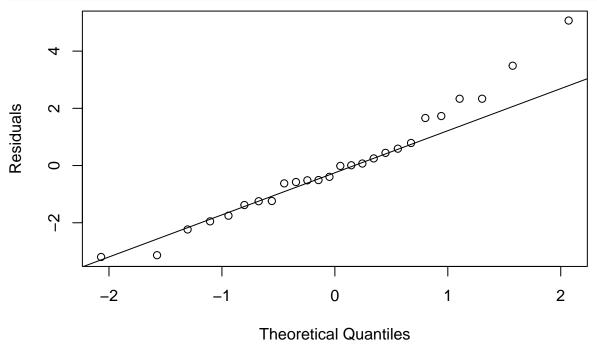
car::ncvTest(lmod1) # Null hypothesis = constant error variance

```
## Non-constant Variance Score Test
## Variance formula: ~ fitted.values
## Chisquare = 1.206952, Df = 1, p = 0.27194
```

By using the graph we find that there is no clear pattern of variance change along observations, so we then use a heteroscedasticity test. Thus, it is homoscedasticity (constant symmetrical variation).

1ii. Check Normality.

```
qqnorm(residuals(lmod1), ylab = 'Residuals', main = '')
qqline(residuals(lmod1))
```



shapiro.test(residuals(lmod1))

```
##
## Shapiro-Wilk normality test
##
## data: residuals(lmod1)
## W = 0.96313, p-value = 0.457
```

Since p-value is 0.457 which is greater than 0.05 and 0.1, we say it fails to reject the null hypothesis that the random errors are normally distributed. Thus, we conclude that the random errors follow a normal distribution.

1iii. Uncorrelated Errors

```
dwtest(mpg ~ factor(cyl)+disp+hp+drat+wt+qsec+factor(vs)+factor(am)+gear+carb, data=train)
```

```
##
## Durbin-Watson test
##
## data: mpg ~ factor(cyl) + disp + hp + drat + wt + qsec + factor(vs) + factor(am) + gear + carb
## DW = 1.6514, p-value = 0.05224
## alternative hypothesis: true autocorrelation is greater than 0
```

Since the p-value is 0.05224 which is greater than 0.05, we fail to reject the hypothesis of uncorrelated errors.

2. Check Unusual Observations 2i. High Leverage Points

```
lev=hatvalues(lmod1)
n<-length(lev)
p<-dim(model.matrix(lmod1))[2]
dat=data.frame(index=seq(n),leverage=lev)
high.lev<-dat[which(dat$lev>2*(p)/n),"index"];high.lev
```

```
## integer(0)
```

2ii. Outliers

```
r=rstandard(lmod1)
r.a<- abs(r)
outliersm<-which(abs(r)>=3); outliersm
```

named integer(0)

2iii. Influential Observations.

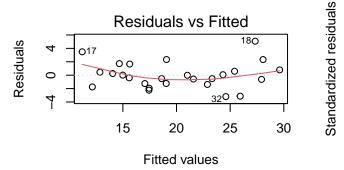
```
d=cooks.distance(lmod1)
dat3=data.frame(index=seq(length(r)),distance=d)
influ<-dat3[which(dat3$distance>4/n),"index"];influ
```

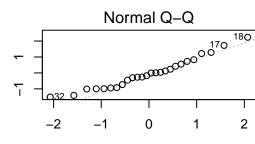
[1] 9 14 24

Therefore, there are three influential observations. There is no outlier or high leverage point.

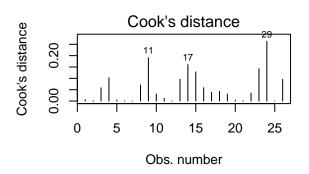
Diagnostic Summary (Unusual observations in a single plot)

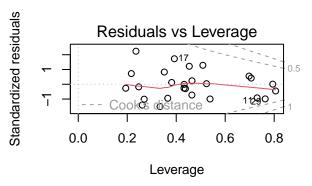
```
par(mfrow = c(2,2))
plot(lmod1,c(1,2,4,5))
```





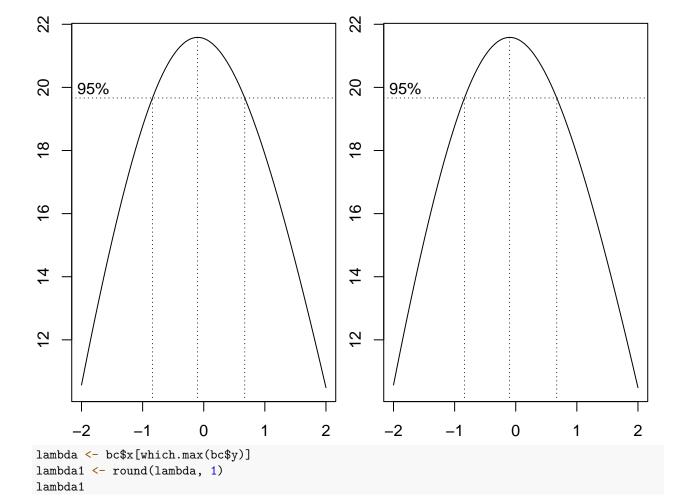
Theoretical Quantiles





Now, we check whether the response needs a Box-Cox transformation.

```
par(mfrow=c(1,2),mar=c(2,2,0.8,0.5))
boxcox(lmod1,plotit=TRUE)
bc = boxcox(lmod1,plotit=TRUE)
```



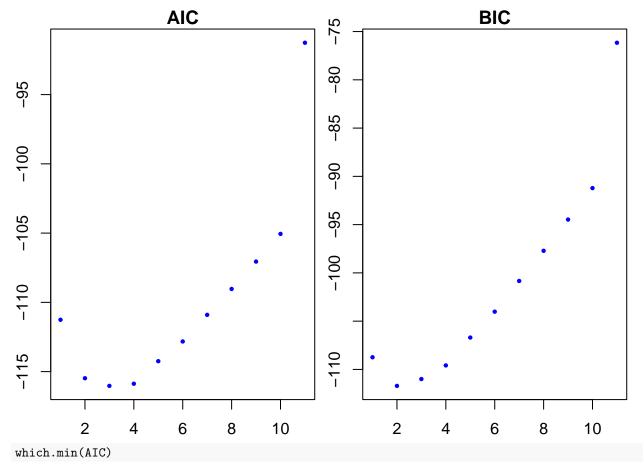
[1] -0.1

Since 1 is not in the confidence interval, we need to do a Box-Cox transformation. Take log transformation on the response

```
fit <- lm(log(mpg) ~ factor(cyl)+disp+hp+drat+wt+qsec+factor(vs)+factor(am)+gear+carb, data=train)
summary(fit)</pre>
```

```
##
## Call:
## lm(formula = log(mpg) ~ factor(cyl) + disp + hp + drat + wt +
       qsec + factor(vs) + factor(am) + gear + carb, data = train)
##
##
## Residuals:
##
        Min
                  1Q
                       Median
                                    3Q
                                            Max
   -0.15498 -0.05515 -0.01540 0.04231
##
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 3.1572565 0.7824988
                                        4.035 0.00123 **
## factor(cyl)6 -0.0681248 0.1119206
                                       -0.609
                                               0.55248
## factor(cyl)8 -0.0323755 0.2100929
                                       -0.154
                                               0.87973
## disp
                -0.0002144
                           0.0010278
                                       -0.209
                                               0.83776
                -0.0014273 0.0013600
## hp
                                       -1.050 0.31171
```

```
## drat
               -0.0169624 0.0837382 -0.203 0.84239
## wt.
               -0.1075789 0.0974874
                                      -1.104 0.28841
## qsec
                0.0130669 0.0372894
                                       0.350 0.73124
                                       0.349 0.73250
## factor(vs)1
                0.0393093 0.1127298
## factor(am)1
                0.0631129 0.1036733
                                       0.609 0.55243
                0.0520620 0.0679768
                                       0.766 0.45647
## gear
                0.0056894 0.0465830
                                       0.122 0.90453
## carb
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1167 on 14 degrees of freedom
## Multiple R-squared: 0.9069, Adjusted R-squared: 0.8338
## F-statistic: 12.4 on 11 and 14 DF, p-value: 2.141e-05
AIC and BIC:
require(leaps)
## Loading required package: leaps
models<- regsubsets(log(mpg) ~ cyl+disp+hp+drat+wt+qsec+vs+am+gear+carb, data=train, nvmax= NULL)
rs<- summary(models)
rs$which
##
      (Intercept)
                   cyl disp
                                hp drat
                                            wt qsec
                                                                gear carb
                                                       ٧S
                                                              am
            TRUE FALSE TRUE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## 1
## 2
            TRUE TRUE FALSE FALSE TRUE FALSE FALSE FALSE FALSE FALSE
## 3
            TRUE TRUE FALSE TRUE FALSE TRUE FALSE FALSE FALSE FALSE
## 4
            TRUE
                  TRUE FALSE TRUE FALSE
                                         TRUE FALSE FALSE FALSE
                                                                 TRUE FALSE
## 5
            TRUE
                  TRUE FALSE TRUE FALSE
                                          TRUE
                                               TRUE FALSE FALSE
                                                                 TRUE FALSE
## 6
            TRUE TRUE FALSE TRUE FALSE
                                         TRUE
                                               TRUE FALSE
                                                           TRUE
                                                                 TRUE FALSE
## 7
                                                           TRUE
                                                                 TRUE FALSE
            TRUE TRUE TRUE FALSE
                                         TRUE
                                               TRUE FALSE
## 8
            TRUE TRUE TRUE FALSE
                                          TRUE
                                               TRUE FALSE
                                                           TRUE
                                                                 TRUE TRUE
## 9
            TRUE
                  TRUE TRUE
                              TRUE FALSE
                                          TRUE
                                                TRUE
                                                      TRUE
                                                           TRUE
                                                                 TRUE
                                                                       TRUE
## 10
            TRUE TRUE TRUE TRUE TRUE
                                         TRUE
                                               TRUE
                                                     TRUE
                                                           TRIF
                                                                 TRIIE
                                                                       TRUE
n <- dim(train)[1]</pre>
AIC <- n*log(rs$rss/n)+2*seq(2,12,1)
## Warning in n * log(rs$rss/n) + 2 * seq(2, 12, 1): longer object length is not a
## multiple of shorter object length
BIC \leftarrow n*log(rs$rss/n)+log(n)*seq(2,12,1)
## Warning in n * log(rs$rss/n) + log(n) * seq(2, 12, 1): longer object length is
## not a multiple of shorter object length
par(mar = c(2,2,1.2,0.5), mfrow=c(1,2))
plot(AIC~I(1:11), main="AIC", xlab = "# predictors", pch = 20, col = "blue", cex=0.7)
plot(BIC~I(1:11),main="BIC",xlab = "# predictors", pch = 20, col = "blue",cex=0.7)
```



[1] 3
which.min(BIC)

[1] 2

Thus, we attain minimum AIC at 3 and BIC at 2 predictors.

```
### best model according to AIC
AICnames<-names(which(rs$which[which.min(AIC),])=="TRUE" )[-1]
train.formulaAIC <- as.formula(paste("log(mpg) ~", paste(AICnames, collapse = " + ")))
AIC.model<-lm(train.formulaAIC, data =train)
summary(AIC.model)</pre>
```

```
##
## Call:
## lm(formula = train.formulaAIC, data = train)
##
## Residuals:
##
                  1Q
                       Median
                                    3Q
                                            Max
## -0.146383 -0.062130 -0.005557 0.056563 0.207179
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3.8633348 0.0782008 49.403 < 2e-16 ***
             -0.0579078  0.0236393  -2.450  0.022725 *
## cyl
             ## hp
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1001 on 22 degrees of freedom
## Multiple R-squared: 0.8924, Adjusted R-squared: 0.8777
## F-statistic: 60.8 on 3 and 22 DF, p-value: 8.243e-11
### best model according to BIC
BICnames <- names (which (rs \$ which [which . min (BIC),]) == "TRUE") [-1]
train.formulaBIC <- as.formula(paste("log(mpg) ~", paste(BICnames, collapse = " + ")))</pre>
BIC.model<-lm(train.formulaBIC, data =train)</pre>
summary(BIC.model)
##
## Call:
## lm(formula = train.formulaBIC, data = train)
## Residuals:
        Min
                   1Q
                         Median
                                       3Q
                                                Max
## -0.161424 -0.047284 -0.008892 0.061733 0.211381
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 3.90510 0.07511 51.992 < 2e-16 ***
                          0.01778 -4.622 0.000119 ***
## cyl
              -0.08216
## wt
              -0.14076
                          0.03403 -4.136 0.000401 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1028 on 23 degrees of freedom
## Multiple R-squared: 0.8813, Adjusted R-squared: 0.871
## F-statistic: 85.36 on 2 and 23 DF, p-value: 2.276e-11
Ridge Regression
require(glmnet)
## Loading required package: glmnet
## Loading required package: Matrix
## Loaded glmnet 4.1-6
library(glmnet)
library(dplyr)
##
## Attaching package: 'dplyr'
## The following object is masked from 'package:MASS':
##
##
## The following objects are masked from 'package:stats':
##
##
      filter, lag
## The following objects are masked from 'package:base':
```

```
##
       intersect, setdiff, setequal, union
library(tidyr)
##
## Attaching package: 'tidyr'
## The following objects are masked from 'package:Matrix':
##
##
       expand, pack, unpack
Train = na.omit(train)
x = scale(model.matrix(log(mpg) \sim cyl+disp+hp+drat+wt+qsec+vs+am+gear+carb, train)[,-1])
y = log(Train$mpg)
grid = 10^seq(10, -2, length = 100)
ridge_mod = glmnet(x, y, alpha = 0, lambda = grid)
set.seed(1) #we set a random seed first so our results will be reproducible.
cv.out.ridge=cv.glmnet(x, y, alpha = 0)
## Warning: Option grouped=FALSE enforced in cv.glmnet, since < 3 observations per
## fold
plot(cv.out.ridge)
abline(v = log(cv.out.ridge$lambda.min), col="red", lwd=3, lty=2)
            0.08
Mean-Squared Error
      90.0
      0.04
      0.02
                        -2
                                       0
                                                     2
                                                                   4
                                           Log(\lambda)
bestlam = cv.out.ridge$lambda.min
bestlam
## [1] 0.151475
out = glmnet(x,y,alpha=0)
predict(out,type="coefficients",s=bestlam)[1:11,]
```

```
## (Intercept)
                                   disp
                        cyl
                                                  hp
                                                             drat
##
   2.95985680 -0.03693273 -0.04750091 -0.04108515 0.02034380 -0.05099436
##
                         vs
                                     am
                                                gear
## 0.01331621 0.02179306 0.02860022
                                         0.02619382 -0.02742018
best_model <- glmnet(x,y, alpha = 0, lambda = bestlam)</pre>
Now we have log full model, AIC model, BIC model, and ridge model.
  4. point estimation:
test1_point <- predict(fit, newdata = test, interval = "confidence")</pre>
test1 point
##
           fit
                     lwr
## 5 2.764375 2.607370 2.921380
## 10 2.950512 2.715737 3.185287
## 15 2.530480 2.304874 2.756086
## 20 3.356639 3.208632 3.504645
## 25 2.713809 2.544550 2.883068
## 30 3.008960 2.788467 3.229453
test2_point <- predict(AIC.model, newdata = test, interval = "confidence")</pre>
test2_point
##
           fit
                     lwr
## 5 2.788304 2.711303 2.865305
## 10 2.942767 2.892647 2.992886
## 15 2.512552 2.404855 2.620248
## 20 3.326438 3.254696 3.398180
## 25 2.731591 2.662361 2.800822
## 30 2.997940 2.939512 3.056368
test3_point <- predict(BIC.model, newdata = test, interval = "confidence")</pre>
test3_point
##
           fit
                     lwr
                              upr
## 5 2.763587 2.692815 2.834359
## 10 2.927913 2.881030 2.974795
## 15 2.508816 2.398593 2.619038
## 20 3.318154 3.245581 3.390727
## 25 2.706580 2.645045 2.768116
## 30 3.022220 2.973123 3.071317
test4_point <- predict(best_model, s = bestlam, newx = scale(as.matrix(test[,2:11])))</pre>
test4_point
##
## 5 2.925668
## 10 2.973764
## 15 3.006795
## 20 2.987386
## 25 2.925207
## 30 2.940320
Since models are log value, we need to turn them back to y.
t1pt <- exp(test1_point)</pre>
t1pt
```

```
fit
                    lwr
                             upr
## 5 15.86912 13.56334 18.56690
## 10 19.11574 15.11575 24.17424
## 15 12.55953 10.02292 15.73812
## 20 28.69258 24.74521 33.26965
## 25 15.08664 12.73750 17.86901
## 30 20.26631 16.25607 25.26584
t2pt <- exp(test2_point)
t2pt
##
           fit
                    lwr
                             upr
## 5 16.25343 15.04887 17.55440
## 10 18.96825 18.04100 19.94316
## 15 12.33637 11.07682 13.73914
## 20 27.83901 25.91174 29.90962
## 25 15.35731 14.33008 16.45817
## 30 20.04420 18.90663 21.25023
t3pt <- exp(test3_point)
t3pt
##
           fit
                    lwr
## 5 15.85662 14.77321 17.01949
## 10 18.68858 17.83263 19.58562
## 15 12.29037 11.00768 13.72252
## 20 27.60934 25.67662 29.68754
## 25 14.97797 14.08407 15.92859
## 30 20.53684 19.55290 21.57029
t4pt <- exp(test4_point)
t4pt
##
            s1
## 5 18.64668
## 10 19.56543
## 15 20.22248
## 20 19.83377
## 25 18.63809
## 30 18.92190
SSR_t1 = sum((t1pt[,1]-test$mpg)^2)
SSR_t2 = sum((t2pt[,1]-test$mpg)^2)
SSR_t3 = sum((t3pt[,1]-test$mpg)^2)
SSR_t4 = sum((t4pt[,1]-test$mpg)^2)
MSE_t1 = SSR_t1/(dim(test)[1]-length(coef(fit)))
MSE_t2 = SSR_t2/(dim(test)[1]-length(coef(AIC.model)))
MSE_t3 = SSR_t3/(dim(test)[1]-length(coef(BIC.model)))
MSE_t4 = SSR_t4/(dim(test)[1]-length(coef(best_model)))
abs(MSE_t1)
## [1] 9.507035
abs(MSE t2)
## [1] 30.70467
```

abs(MSE_t3)

[1] 23.33937

abs(MSE_t4)

[1] 59.07952

Full model has the least MSE, so full model is the best model.