Computer Science 384 St. George Campus February 01, 2022 University of Toronto

Homework Assignment #2: Constraint Satisfaction **Due: February 18, 2022 by 11:59 PM** 

**Silent Policy**: A silent policy will take effect 24 hours before this assignment is due, i.e. no question about this assignment will be answered, whether it is asked on the discussion board, via email or in person.

**Late Policy**: Using grace days (you have 5 grace days for the entire semester) or 10% per day (up to 5 days). You must *notify us* through this form if you want to use your grace days for this assignment.

**Total Marks**: This part of the assignment represents 10% of the course grade.

### Handing in this Assignment

What to hand in on paper: Nothing.

What to hand in electronically: You must submit your assignment electronically. Download the assignment files from Quercus. Modify propagators.py, and puzzle\_csp.py appropriately so that they solve the problems specified in this document. **Submit your modified** propagators.py **and** puzzle\_csp.py **files.** You must also fill in and submit the acknowledgment form, acknowledgment\_form.pdf.

<u>How to submit:</u> Your login to MarkUs is your teach.cs username and password. It is your responsibility to include all necessary files in your submission. You can submit a new version of any file at any time, though the lateness penalty applies if you submit after the deadline. For the purposes of determining the lateness penalty, the submission time is considered to be the time of your latest submission.

#### **Extra Information**

<u>Clarifications:</u> Important corrections (hopefully few or none) and clarifications to the assignment will be posted on Quercus. You are responsible for monitoring Quercus announcements for any clarifications or corrections.

Questions: Questions about the assignment should be asked on Piazza.

## **Evaluation Details**

We will test your code electronically. You will be supplied with a testing script that will run a <u>subset</u> of the tests (tests.py). If your code fails all of the tests performed by the script (using Python version 3.10), you will receive zero marks. It's up to you to create test cases to further test your code—that's part of the assignment!

When your code is submitted, we will run a more extensive set of tests. You have to pass all of these more elaborate tests to obtain full marks on the assignment.

We will set a timeout of 120 seconds per board during marking. This 120 second time limit includes the time to create a model and find a solution. Solutions that time-out are considered incorrect. Ensure that your implementations perform well under this limit, and be aware that your computer may be quicker than

teach.cs (where we will be testing). We will not conduct end to end tests on boards with constraints whose domain is larger than six.

Your code will **not be** evaluated for partial correctness, it either works or it doesn't. It is your responsibility to hand in something that passes at least some of the tests in the provided testing script.

- Make certain that your code runs on teach.cs using Python3 (version 3.10) using only standard imports. This version is installed as "python3" on teach.cs. Your code will be tested using this version and you will receive zero marks if it does not run using this version.
- Do not add any non-standard imports from within the Python file you submit (the imports that are already in the template files must remain). Once again, non-standard imports will cause your code to fail the testing and you will receive zero marks.
- *Do not change the supplied starter code*. Your code will be tested using the original starter code, and if it relies on changes you made to the starter code, you will receive zero marks.

### Introduction

There are two parts to this assignment.

- 1. **Propagators**. You will implement two constraint propagators—a Forward Checking constraint propagator, and a Generalized Arc Consistence (GAC) constraint propagator
- 2. **Models**. You will implement three different CSP models: two grid-only puzzle models, and one full FunPuzz model (adding *cage* constraints to grid).

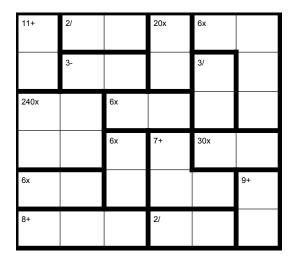
## What is supplied

- cspbase.py. Class definitions for the python objects Constraint, Variable, and BT.
- **propagators.py**. Starter code for the implementation of your two propagators. You will modify this file with the addition of two new procedures prop\_FC and prop\_GAC.
- puzzle\_csp.py. Starter code for the CSP models. You will modify three procedures in this file: binary\_ne\_grid, nary\_ad\_grid, and caged\_csp\_model.
- csp\_sample\_run.py. This file contains a sample implementation of two CSP problems.
- **tests.py**. Sample test cases. Run the tests with "python3 tests.py". This file will be released soon after the assignment is posted.

# **FunPuzz Formal Description**

The FunPuzz puzzle has the following formal description:

- FunPuzz consists of an  $n \times n$  grid where each cell of the grid can be assigned a number 1 to n. No digit appears more than once in any row or column. Grids range in size from  $3 \times 3$  to  $9 \times 9$ .
- FunPuzz grids are divided into heavily outlined groups of cells called *cages*. These *cages* come with a *target* and an *operation*. The numbers in the cells of each *cage* must produce the *target* value when combined using the *operation*.



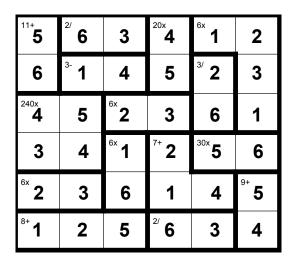


Figure 1: An example of a  $6 \times 6$  FunPuzz grid with its start state (left) and solution (right).

- For any given *cage*, the *operation* is one of addition, subtraction, multiplication or division. Values in a *cage* can be combined in any order: the first number in a *cage* may be used to divide the second, for example, or vice versa. Note that the four operators are "left associative" e.g., 16/4/4 is interpreted as (16/4)/4 = 1 rather than 16/(4/4) = 16.
- A puzzle is *solved* if all empty cells are filled in with an integer from 1 to *n* and all above constraints are satisfied.
- An example of a  $6 \times 6$  grid is shown in Figure 1. Note that your solution will be tested on  $n \times n$  grids where n can be from 3 to 9.

#### **Additional notes:**

- It is possible for a given cell to not participate in any cage constraints. That is still a valid FunPuzz board.
- For division, we are only concerned with divisions producing integer results throughout the operation.

# **Question 1: Propagators** (worth 55/100 marks)

You will implement Python functions to realize two constraint propagators—a Forward Checking (FC) constraint propagator and a Generalized Arc Consistence (GAC) constraint propagator. These propagators are briefly described below. The files cspbase.py and propagators.py provide the **complete input/out-put specification** of the two functions you are to implement.

Brief implementation description: The propagator functions take as input a CSP object csp and (optionally) a Variable newVar representing a newly instantiated Variable, and return a tuple of (bool,list) where bool is False if and only if a dead-end is found, and list is a list of (Variable, value) tuples that have been pruned by the propagator. In all cases, the CSP object is used to access variables and constraints of the problem, via methods found in cspbase.py.

#### You must implement:

prop\_FC (worth 25/100 marks)

A propagator function that propagates according to the FC algorithm that check constraints that have *exactly one uninstantiated variable in their scope*, and prune appropriately. If newVar is None, forward check all constraints. Otherwise only check constraints containing newVar.

prop\_GAC (worth 30/100 marks)

A propagator function that propagates according to the GAC algorithm, as covered in lecture. If newVar is None, run GAC on all constraints. Otherwise, only check constraints containing newVar.

## **Question 2: Models** (worth 45/100 marks)

You will implement three different CSP models using three different constraint types. The three different constraint types are (1) binary not-equal; (2) *n*-ary all-different; and (3) FunPuzz *cage*. The three models are (a) binary grid-only FunPuzz; (b) *n*-ary grid-only FunPuzz; and (c) complete FunPuzz. The CSP models you will build are described below. The file puzzle\_csp.py provides the **complete input/output specification**.

Brief implementation description: The three models take as input a valid FunPuzz grid, which is a list of lists, where the first list has a single element, N, which is the size of each dimension of the board, and each following list represents a *cage* in the grid. Cell names are encoded as integers in the range 11, ..., nn and each inner list contains the numbers of the cells that are included in the corresponding *cage*, followed by the *target* value for that *cage* and the *operation* (0='+', 1='-', 2='/', 3='\*'). If a list has two elements, the first element corresponds to a cell, and the second one—the *target*—is the value enforced on that cell.

For example, the model ((3), (11, 12, 13, 6, 0), (21, 22, 31, 2, 2), ....) corresponds to a 3x3 board<sup>1</sup> where

- 1. cells 11, 12 and 13 must sum to 6, and
- 2. the result of dividing some permutation of cells 21, 22, and 31 must be 2. That is, (C21/C22)/C23 = 2 or (C21/C23)/C22 = 2, or (C22/C21)/C23 = 2, etc...

<sup>&</sup>lt;sup>1</sup>Note that cell indexing starts from 1, e.g. 11 is the cell in the upper left corner.

All models need to return a CSP object, and a list of lists of Variable objects representing the board. The returned list of lists is used to access the solution. The grid-only models do not need to encode the *cage* constraints.

### You must implement:

binary\_ne\_grid (worth 10/100 marks)

A model of a FunPuzz grid (without *cage* constraints) built using only binary not-equal constraints for both the row and column constraints.

nary\_ad\_grid (worth 10/100 marks)

A model of a FunPuzz grid (without *cage* constraints) built using only <u>n-ary all-different</u> constraints for both the row and column constraints.

caged\_csp\_model (worth 25/100 marks)

A model built using your choice of (1) binary binary not-equal, or (2) n-ary all-different constraints for the grid, together with (3) FunPuzz cage constraints. That is, you will choose one of the previous two grid models and expand it to include FunPuzz cage constraints.

**Notes:** The CSP models you will construct can be space expensive, especially for constraints over many variables, (e.g., for *cage* constraints and those contained in the first binary\_ne\_grid grid CSP model). Also be mindful of the **time** complexity of your methods for identifying satisfying tuples, especially when coding the puzzle\_csp\_model.

HAVE FUN and GOOD LUCK!