# 0852617 曾鈺評 機器學習HW02\_2

# **Online Learning**

```
In [1]:
```

```
import numpy as np
```

## In [62]:

```
directory = "D:\\1091NCTU\Machine learning\\Homework\\"
rawdata = []
with open(directory+"testfile.txt") as file:
    for line in file:
        rawdata.append([int(i) for i in list(line.split("\n")[0])])
```

# In [96]:

```
def Factorial(number):
    result = 1
    for i in range(1, number+1, 1):
        result = result*i
    return result

def Combination(n,x):
    return Factorial(n) / (Factorial(x) * Factorial(n-x))

def Gamma(x):
    return Factorial(x-1)

def Beta(a, b):
    return (Gamma(a) * Gamma(b)) / Gamma(a+b)
```

#### In [137]:

```
alpha = int(input("alpha = "))
beta = int(input("beta = "))
```

```
alpha = 0
beta = 0
```

## In [138]:

```
for i in range(len(rawdata)):
    print("case %s:" %(i+1), end=' ')
    for j in rawdata[i]:
        print(j, end='')
    print("")
    n = len(rawdata[i])
    k = sum(rawdata[i])
    mu = k / n
    likelihood = Combination(n, k) * mu**k * (1-mu)**(n-k)
    print("Likelihood: %s" %likelihood)
    print("Beta prior: a= %s b=%s" %(alpha, beta))
    alpha = k + alpha
    beta = n - k + beta
    print("Beta posterior: a= %s b=%s\n" %(alpha, beta))
```

case 1: 0101010101001011010101
Likelihood: 0.16818809509277344

Beta prior: a= 0 b=0

Beta posterior: a= 11 b=11

case 2: 0110101

Likelihood: 0.29375515303997485

Beta prior: a= 11 b=11 Beta posterior: a= 15 b=14

case 3: 010110101101

Likelihood: 0.2286054241794335

Beta prior: a= 15 b=14 Beta posterior: a= 22 b=19

case 4: 0101101011101011010
Likelihood: 0.18286870706509092

Beta prior: a= 22 b=19 Beta posterior: a= 33 b=27

case 5: 111101100011110

Likelihood: 0.2143070548857833

Beta prior: a= 33 b=27 Beta posterior: a= 43 b=32

case 6: 101110111000110

Likelihood: 0.20659760529408

Beta prior: a= 43 b=32 Beta posterior: a= 52 b=38

case 7: 1010010111

Likelihood: 0.25082265600000003

Beta prior: a= 52 b=38 Beta posterior: a= 58 b=42

case 8: 11101110110

Likelihood: 0.2619678932864457

Beta prior: a= 58 b=42 Beta posterior: a= 66 b=45

case 9: 01000111101

Likelihood: 0.23609128871506807

Beta prior: a= 66 b=45 Beta posterior: a= 72 b=50

case 10: 110100111

Likelihood: 0.27312909617436365

Beta prior: a= 72 b=50 Beta posterior: a= 78 b=53

case 11: 01101010111

Likelihood: 0.24384881449471862

Beta prior: a= 78 b=53 Beta posterior: a= 85 b=57

# In [139]:

```
alpha = int(input("alpha = "))
beta = int(input("beta = "))
```

alpha = 10 beta = 1

## In [140]:

```
for i in range(len(rawdata)):
    print("case %s:" %(i+1), end=' ')
    for j in rawdata[i]:
        print(j, end='')
    print("")
    n = len(rawdata[i])
    k = sum(rawdata[i])
    mu = k / n
    likelihood = Combination(n, k) * mu**k * (1-mu)**(n-k)
    print("Likelihood: %s" %likelihood)
    print("Beta prior: a= %s b=%s" %(alpha, beta))
    alpha = k + alpha
    beta = n - k + beta
    print("Beta posterior: a= %s b=%s\n" %(alpha, beta))
```

case 1: 0101010101001011010101
Likelihood: 0.16818809509277344

Beta prior: a= 10 b=1 Beta posterior: a= 21 b=12

case 2: 0110101

Likelihood: 0.29375515303997485

Beta prior: a= 21 b=12 Beta posterior: a= 25 b=15

case 3: 010110101101

Likelihood: 0.2286054241794335

Beta prior: a= 25 b=15 Beta posterior: a= 32 b=20

case 4: 0101101011101011010
Likelihood: 0.18286870706509092

Beta prior: a= 32 b=20 Beta posterior: a= 43 b=28

case 5: 111101100011110

Likelihood: 0.2143070548857833

Beta prior: a= 43 b=28 Beta posterior: a= 53 b=33

case 6: 101110111000110

Likelihood: 0.20659760529408

Beta prior: a= 53 b=33 Beta posterior: a= 62 b=39

case 7: 1010010111

Likelihood: 0.25082265600000003

Beta prior: a= 62 b=39 Beta posterior: a= 68 b=43

case 8: 11101110110

Likelihood: 0.2619678932864457

Beta prior: a= 68 b=43 Beta posterior: a= 76 b=46

case 9: 01000111101

Likelihood: 0.23609128871506807

Beta prior: a= 76 b=46 Beta posterior: a= 82 b=51

case 10: 110100111

Likelihood: 0.27312909617436365

Beta prior: a= 82 b=51 Beta posterior: a= 88 b=54

case 11: 01101010111

Likelihood: 0.24384881449471862

Beta prior: a= 88 b=54 Beta posterior: a= 95 b=58

In [ ]: