Predicting Mathematics Achievement: A Machine Learning Approach Using TIMSS 2015 U.S. National Public-Use Data

Word count: 1995

Abstract

Using TIMSS 2015 U.S. national public-use data, this study shows how machine learning could be applied to large-scale international studies. The analysis provides a comparison of six commonly used machine learning models in identifying students with low mathematics performance, which would allow educators to effectively allocate resources to intervene and thus improve their performance. The results show that logistic regression, elastic net, and extreme gradient boosting all perform well in terms of balanced accuracy and sensitivity. Leveraging the high dimensionality of the data, this research analyzes 142 student and school variables and identifies characteristics that are associated with mathematics performance, including students' home education resources, attitudes toward mathematics, and use and possession of computers or tablets.

Keywords

Machine learning; TIMSS; Mathematics achievement; Large-scale educational research

Introduction

Objective

Poor mathematics achievement creates difficulties for students in everyday activities and leads to serious consequences in educational attainment and career advancement (Jordan, 2010; Geary, 2011). Identifying characteristics that could predict poor mathematics achievement would help educators allocate resources effectively and intervene in time. Using 2015 U.S. data from the Trends in International Mathematics and Science Study (TIMSS), this paper attempts to 1) provide a comprehensive evaluation of machine learning (ML) methods in analyzing international large-scale education data, and 2) identify student and school background characteristics that have the largest importance in the prediction.

Theoretical Framework

Existing literature has explored various factors that may be associated with students' mathematics achievement. Characteristics ranging from students' gender (McGraw et al., 2006), race (Brown-Jeffy, 2009), and family background (Wang, 2004) to teacher qualification (Darling-Hammond, 2000) and school resources (Burtless, 2011), to name a few, are believed to be significant determinants of achievement. However, most studies have employed conventional statistical methods and have focused on only a few theory-driven variables.

With the recent development of machine learning (ML), a number of data-driven techniques are now utilized by education researchers in areas including predicting dropout (Sansone, 2017) and course score (Polyzou & Karypis, 2016). However, only a handful of studies have focused on applying ML techniques to

large-scale international assessment data (Gabriel & Jason Signolet, 2018; Yoo, 2018), and none have compared the performance of different ML methods.

Significance

This study thus attempts to fill the research gaps identified above by comparing the performance of the six most common ML algorithms using TIMSS 2015 U.S. national public-use data. The methodology presented could also be applied to the analysis of data from other education systems. The study also contributes to the literature by leveraging the high dimensionality of the data, as it investigates as many student and school variables as possible to identify characteristics associated with mathematics performance. Being able to accurately predict students who would have low mathematics performances would allow in-time intervention to increase performance.

Data Source

TIMSS is an international comparative study designed to measure trends in mathematics and science achievement at the 4th and 8th grades, as well as collect information about educational contexts that may be related to student achievement (Provasnik et al., 2016). In 2015, 64 education systems participated in TIMSS. This paper analyzes data from the United States, specifically, the 8th-grade student achievement data as well as student and school background questionnaire data from the U.S. national public-use data file. The national public-use data file contains additional U.S.-specific information, such as students' race/ethnicity, which provides more context for data analysis.

Methods

Data preprocessing

As Figure 1 shows, after merging the student achievement data with student and school background questionnaire data, there were 10,221 observations with 572 variables. A binary outcome variable was created that equals 1 if the student is considered low-performing in mathematics (defined as having the average of all 5 plausible values for mathematics below the intermediate international benchmark) and 0 otherwise.¹

The data cleaning process included removing irrelevant variables (e.g., ID-related variables, file maintenance variables, weights, and plausible values), removing variables that have more than 15% missing data, removing variables that are highly correlated with each other, and standardizing variables. A more detailed data cleaning process is documented in Appendix A.

The data cleaning process resulted in 5,516 grade 8 students (54% of the original sample) with 143 student and school variables, as documented in Appendix B. As Table 1 shows, using the outcome variable as the stratifier, the remaining observations were randomly split into training and test datasets with the conventional ratio of 8:2.

¹ TIMSS defines four levels of student achievement, referred to as international benchmarks: Advanced, High, Intermediate, and Low. These international benchmarks provide a way to understand how students' proficiency in mathematics varies at different points on the TIMSS scale. Grade 8 students who perform below 400 are considered below the low international mathematics benchmark. Grade 8 students who perform at or above 400 but below 475 are considered to be at the low international mathematics benchmark (Mullis, Martin, Foy, & Hooper, 2016).

The training set was used for model construction and validation, where 5-fold cross-validation² is performed to tune hyperparameters that make the model perform the best on the training set. We then applied the tuned models to the test set for model evaluation, using a variety of the performance metrics detailed in the Results and Discussion section.

Machine Learning Models: Brief Introduction

Machine learning is the science of giving computers the ability to learn without being explicitly programmed (Samuel, 1959). This paper implemented six common ML algorithms to approach a supervised problem.³ The following section briefly describes each of these algorithms.⁴

Logistic Regression

Logistic regression is one of the most commonly used ML algorithms for binary classification. A sigmoid function is applied to map the linear regression output to continuous values from 0 to 1, which represent the probability of classification. A threshold classifier of 0.5 is used to convert the probability into either 0 or 1.5

Elastic Net

Elastic net is an extension of logistic regression. When the number of predictors becomes large, overfitting and multicollinearity become problems, which often plague logistic regression with degeneracies (Hastie & Qian, 2014). Penalized regression methods, such as elastic net, alleviate the problem by adding a penalty term to the model,

$$\lambda \sum_{j=1}^{P} (\alpha |\beta_j| + (1 - \alpha)\beta_j^2)$$

where λ controls the overall strength of the penalty and lpha controls the elastic net penalty.

Decision Tree

The decision tree model is one of the tree-based methods, which involve splitting the dataset recursively. At each step, the split is made based on the independent variable that results in the largest possible reduction in heterogeneity of the dependent variable. 8

Random Forest

Random forest is an extension of the decision tree model. It involves producing and combining multiple trees (hence "forest") to yield a single consensus prediction.⁹

² Technical details on cross-validation are provided by Hastie et al. (2001).

³ Machine learning algorithms can be divided into two main categories: supervised learning, where there is a defined output variable; and unsupervised learning, where the model is designed to find patterns.

⁴ A more detailed technical explanation is provided by James et al. (2014).

⁵ The logistic regression model is implemented by the "glm" R package (R Core Team, 2013).

⁶ When α = 1, it is the LASSO (Least Absolute Shrinkage and Selection Operator) model, and when α = 0, it is the Ridge model. The elastic net model is implemented by the "glmnet" R package. (Friedman, Hastie, & Tibshirani, 2010).

⁷ Splitting a dataset recursively means that the subsets that arise from a split are further split until a predetermined termination criterion is reached.

⁸ The decision tree model is implemented by the "rpart" R package (Therneau & Atkinson, 2018).

⁹ It is known that combining a large number of trees can often result in dramatic improvements in prediction accuracy, at the expense of some loss in interpretation. The random forest model is implemented by the "randomForest" R package (Liaw & Wiener, 2002).

Extreme Gradient Boosting

Extreme gradient boosting, like random forest, uses an ensemble of multiple trees to create a more powerful prediction model. Unlike random forest, which builds and combines a forest of randomly different trees in parallel, extreme gradient boosting builds a series of trees in such a way that when each tree is trained, it attempts to correct the mistakes, or misclassification, of the previous tree in the series. The final prediction is based on the aggregate results of all trees in the series. The model also reduces the risk of overfitting by heavily penalizing complexity.¹⁰

Neural Network

Neural network models are inspired by the way biological neural networks in the human brain process information. A simple form of neural network is called multi-layer perceptron, which has three components: an input layer, one or many hidden layer(s), and an output layer. ¹¹

Results and Discussion

Research Question 1: How do the selected machine learning methods compare in predicting low mathematic performers?

While accuracy is usually used as a performance metric, it would be biased when the data set is unbalanced (Zahedifard et al., 2015), as in this case. For example, a baseline model, which uses the simplest rule in predicting outcomes by always predicting the most frequent category, would predict that all 1,103 observations in the test set are in the "non-low-mathematics achiever" category and none are in the "low-mathematics achiever" category. This would have an accuracy of 852/1,103 = 0.772. In comparison, balanced accuracy, which is the harmonic mean of precision and recall, has proven to be useful in evaluating models with unbalanced categories (García, Mollineda, & Sánchez, 2009). Therefore, we primarily use balanced accuracy to evaluate and compare the models. The same baseline model would have a balanced accuracy of $\frac{1}{2}$ * (852/852 + 0/251) = 0.5. Table 2 lists additional metrics for finer details, including sensitivity/recall, specificity, positive predicted value/precision, and negative predicted value.

All six ML models performed above the baseline model. The decision tree model yielded a balanced accuracy of 65.5%, the lowest across all six models. Among the tree-based models, the random forest and extreme gradient boosting models showed improved performance against the decision tree model, with balanced accuracy of 70.0% and 74.9%, respectively. Logistic regression yielded the highest balanced accuracy (76.0%), 10 percentage points higher than the decision tree model and 26 percentage points higher than the baseline model.

Among the other metrics reported, sensitivity measures the percentage of low-performing grade 8 students who are correctly identified as being at risk of performing poorly in mathematics. And specificity measures the percentage of non-low-math-achiever students who are correctly identified as not at risk of performing poorly in mathematics. Given the context, it should be of policy interest for schools and other stakeholders to expect higher sensitivity from the model. In other words, it would be ideal to have as few cases as possible where students are predicted to be non-low-mathematics achievers when in fact they are at high risk of performing poorly. Logistic regression, again, topped all selected models in sensitivity (58.2%).

¹⁰ The extreme gradient boosting model is implemented by the "xgboost" R package (Chen, et al., 2018).

¹¹ A single hidden layer neural network model is implemented by the "nnet" R package (Venables & Ripley, 2002).

Research Question 2: Which variables have the most predictive value in predicting low mathematics performance?

Besides returning balanced accuracy for the test data, each of the six models computes variable importance scores for 142 predictor variables. Although the technical details of calculating the variable importance estimates differ across models (Kuhn, 2017), all methods, in essence, rank predictor variables based on the role each plays in predicting the outcome. One caveat is that such variable importance estimates give insight only into the magnitude, not the direction, of the relationship between the predictor variables and the dependent variable (Hall, Phan, & Ambati). We took the top 20 most important variables in each of the six models, which results in a list of 59 unique predictors. Among the 59 unique predictors, there are 16 predictors that appear in the top 20 lists of at least three models, as shown in Table 3. Three themes emerge from the list of the 16 most important variables in the prediction of whether students are low performing in mathematics.

The first theme is home environment support, which includes the home educational resources scale, and variables regarding students' use and possession of computers or tablets. In particular, the home educational resources scale appears in the top 20 lists of all six models.

The second theme is students' attitudes and engagement. Students' confidence in mathematics appears in the top 20 lists across all models, and students' confidence in science appears in three models. Students' educational expectations, their views on engaging teaching, and other student characteristics (including race and age) also play important roles in at least three models in predicting mathematics performance.

School environment is the third theme. Variables including the percentage of students eligible for free or reduced-price lunch, school principals' reporting on school discipline and schools' emphasis on academic success, and total instructional time all contribute significantly to the prediction in at least half of the models.

Conclusions

This study shows how machine learning could be applied to large-scale international studies. It also provides a comparison of six commonly used machine learning models in identifying students with low mathematics performance, which would allow educators to effectively allocate resources to intervene and thus improve their performance. The result shows that logistic regression, elastic net, and extreme gradient boosting all perform well in terms of balanced accuracy and sensitivity. Given that logistic regression is easier to interpret than the other models, it is preferred in this context.

Through analyzing 142 student and school variables, this research confirms the findings in the literature about characteristics that may be associated with mathematics performance, including students' home educational resources and attitudes toward mathematics. It also sheds light on a few variables that receive less research attention, including variables about students' use and possession of computers or tablets.

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Tables and Figures

Figure 1: Study design

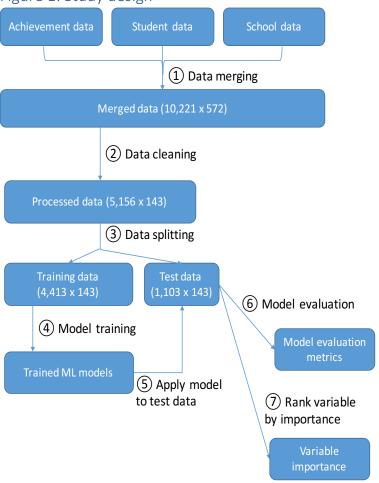


Table 1: Training and test data

| | N | Low-mathematics achievers | Non-low-mathematics achievers |
|-----------|-------|---------------------------|-------------------------------|
| Data | 5,516 | 1,256 | 4,260 |
| Training | | | |
| data | 4,413 | 1,005 | 3,408 |
| Test data | 1,103 | 251 | 852 |

Table 2: Evaluation measures of machine learning models

| | Model | | | | del | | |
|--------------------------|---|----------------------------|----------------|------------------|------------------|---------------------------------|-------------------|
| Evaluation measure | Equation | Logistic regressio n | Elastic net | Decision tree | Random forest | Extreme gradient boosting | Neural network |
| | (TP + TN) | | | | | | |
| Accuracy | (TP + TN + FP + FN) | 85.7% | 85.9% | 81.5% | 83.3% | 85.0% | 81.0% |
| Balanced accuracy | $\frac{1}{2} \times \left(\frac{TP}{TP + FN} + \frac{TN}{TN + FP} \right)$ | 76.0% | 75.0% | 65.5% | 70.0% | 74.9% | 69.1% |
| | <u> </u> | | | | | | |
| Sensitivity/Recall | TP + FN | 58.2% | 55.0% | 36.3% | 45.4% | 56.6% | 47.4% |
| Specificity | $\frac{TN}{TN + FP}$ | 93.8% | 95.0% | 94.8% | 94.5% | 93.3% | 90.8% |
| Positive predicted | <u> </u> | | | | | | |
| value/Precision | TP + FP | 73.4% | 76.2% | 67.4% | 70.8% | 71.4% | 60.4% |
| | <i>TN</i> | | | | | | |
| Negative predicted value | TN + FN | 88.4% | | | | | |

Note: TP = number of true positive cases; FP = number of false positive cases; TN = number of true negative cases; FN = number of false negative cases

Table 3: Variables selected by at least three machine learning models

| | | Appear in the top 20 most important variables | | | | | | |
|---|-----------------------|---|---------------------|-------------|------------------|------------------|---------------------------------|-------------------|
| Variable description | Variable source | Count | Logistic regression | Elastic net | Decision tree | Random forest | Extreme gradient boosting | Neural network |
| Home Educational Resources Scale | Student questionnaire | 6 | Х | Х | X | Х | Х | Х |
| Students Confident in Mathematics Scale | Student questionnaire | 6 | Х | Х | Х | Х | Х | Х |
| [US National Variable] Race/Ethnicity - White, Not Hispanic | Student questionnaire | 5 | × | х | | х | x | x |
| [US National Variable] Percentage of student elibigble for free or reduced- | School questionnaire | 4 | | | х | х | х | х |
| [US National Variable] How far in your education do you expect to go? | Student questionnaire | 4 | Х | | х | Х | х | |
| How often do you use a computer or tablet for schoolwork besides at home or | Student questionnaire | 4 | Х | Х | Х | | х | |
| Students' Views on Engaging Teaching in Mathematics Lessons Scale | Student questionnaire | 4 | х | | х | Х | х | |
| School Discipline Problems - Principals' Reports Scale | School questionnaire | 3 | | | х | Х | х | |
| School Emphasis on Academic Success – Principals' Reports Scale | School questionnaire | 3 | | | х | Х | х | |
| Total Instructional Time in Minutes | School questionnaire | 3 | | | Х | Х | Х | |
| Student Age | Student questionnaire | 3 | | | Х | Х | Х | |
| Students Confident in Sciences Scale | Student questionnaire | 3 | Х | | | Х | Х | |
| [US National Variable] Race/Ethnicity - | Student questionnaire | 3 | Х | Х | | | | Х |
| [US National Variable] Race/Ethnicity - | Student questionnaire | 3 | | Х | | | Х | Х |
| [US National Variable] Have you ever repeated a grade in elementary school? | Student questionnaire | 3 | Х | Х | | | | Х |
| [US National Variable] Do you have a computer or tablet that is shared with other people at home? | Student questionnaire | 3 | х | х | | | | х |

Appendix A – Technical Details in Data Preprocessing

The data cleaning process involved the following steps:

- 1. Create the binary outcome variable, [low_mathematics], which equals 1 if the student is considered low performing in mathematics (and 0 otherwise), defined as having the average of all 5 plausible values for mathematics below the intermediate international benchmark (475).
- 2. Remove ID-related variables (e.g., [idstud] student ID), file maintenances variables (e.g., [itdate] date of testing), weights (e.g., [totwgt] total student weight), plausible values (e.g., [bsmmat01] the first plausible value of mathematics), and string variables (e.g. [bsxg03bt] the U.S.-specific variable about language spoken at home, which is in strings)
- 3. For a few U.S.-specific variables, remove the international version of such variables because the U.S. versions provide more granular information. For example, for the background question, "how far in education do you expect to go," the U.S. version ([bsng08]) distinguishes between "finish master's degree" and "finish doctorate degree," while the international version ([bsbg08]) only has "finish postgraduate degree."
- 4. For all derived scale variables (e.g., [bsbgscm] "Student Confident in Mathematics/SCL"), remove their index versions (e.g., [bsdgscm] "Student Confident in Mathematics/IDX"), and remove the questionnaire-level variables that these scale variables are derived from (e.g., from [bsbm19a] "I usually do well in mathematics" to [bsbm19i] "mathematics makes me confused")
- 5. Remove variables that have more than 15% missing. 12 The threshold of 15% is chosen to maintain at least half of the original samples after list-wise deletion, which is considered the safest method of handling missing data (Allison, 2001). Increasing the threshold will lead to a smaller sample size after list-wise deletion, while decreasing it will lead to a smaller number of predictors. 13
- 6. Dummy-code all binary variables. Convert Liker scale variables (e.g., [bsbg08]) to continuous. For non-ordinal variables (e.g., [msrace2] race/ethnicity), dummy code each variable level and remove the last level (e.g., the newly coded [msrace2_other]).
- 7. Construct a correlation matrix among all remaining variables to identify variable pairs that are highly correlated (> 0.95) with each other and remove the variable with the largest mean absolution correlation (e.g., [bcbg07b] "total instructional time/minutes" is highly correlated with [bcdg07hy] "total instructional hours per year," and the latter is removed).
- 8. Standardize all variables so that they are on the same scale with a mean of 0 and standard deviation of 1 (Lantz, 2013).

This data cleaning process resulted in 5,516 grade 8 students (54% of the original sample) with 143 student and school variables.

¹² Variable levels such as "Not administered" and "Omitted or invalid" are counted as missing.

¹³ In robustness tests where 10% and 20% were used as thresholds, respectively, the findings are consistent with what is documented in the Results and Discussion section.

Appendix B – Variables used in machine learning models

| | Variable Name | Variable Label |
|----|-----------------|---|
| 1 | low_mathematics | outcome variable: low-mathematics-achiever |
| 2 | bnrgcal1 | calculator survey\use of calculator |
| 3 | bsbg06a | gen\home possess\computer tablet own |
| 4 | bsbg06b | gen\home possess\computer tablet shared |
| 5 | bsbg06c | gen\home possess\study desk |
| 6 | bsbg06d | gen\home possess\own room |
| 7 | bsbg06e | gen\home possess\internet connection |
| 8 | bsbg06f | gen\home possess\own mobile phone |
| 9 | bsbg06g | gen\home possess\gaming system |
| 10 | bsbg06h | gen\home possess\ <country specific=""></country> |
| 11 | bsbg10a | gen\born in <country></country> |
| 12 | bsbg14a | gen\internet use\access textbooks |
| 13 | bsbg14b | gen\internet use\access assignments |
| 14 | bsbg14c | gen\internet use\collaborate with classmates |
| 15 | bsbg14d | gen\internet use\communicate with teacher |
| 16 | bsbg14e | gen\internet use\find info to aid in math |
| 17 | bsbg14f | gen\internet use\find info to aid in science |
| 18 | bcbg08a | gen\have place for schoolwork |
| 19 | bcbg09a | gen\student achievement used to assign\math |
| 20 | bcbg09b | gen\student achievement used to assign\science |
| 21 | bcbg11a | gen\existing science laboratory |
| 22 | bcbg11b | gen\existing assistance during exp |
| 23 | bcbg12 | gen\have school library |
| 24 | bcbg17a | gen\use incentives\math |
| 25 | bcbg17b | gen\use incentives\science |
| 26 | bcbg17c | gen\use incentives\other |
| 27 | bcbg22a | gen\degrees in education leadership\isced 7 |
| 28 | bcbg22b | gen\degrees in education leadership\isced 8 |
| 29 | bnrgcal2 | calculator survey\frequency of using calculator |
| 30 | bsbg03 | gen\often speak <lang of="" test=""> at home</lang> |
| 31 | bsbg05 | gen\digital information devices |
| 32 | bsbg11 | gen\about how often absent from school |
| 33 | bsbg12 | gen\how often breakfast on school days |
| 34 | bsbg13a | gen\how often use computer tablet\home |
| 35 | bsbg13b | gen\how often use computer tablet\school |
| 36 | bsbg13c | gen\how often use computer tablet\other |
| 37 | bsbs25ab | sci\how often teacher give you homework/science |
| 38 | bsbm25ba | math\how many minutes spent on homework/mathematics |
| 39 | bsbm26aa | math\extra lessons last 12 month\mathematics |

| 40 | bsbs26ab | sci\extra lessons last 12 month\science |
|----|----------|---|
| 41 | bsbm26ba | math\extra lessons how many month\mathematics |
| 42 | bsbs26bb | sci\extra lessons how many month\science |
| 43 | bsbs37a | sci\agree\learn science will help me |
| 44 | bsbs37b | sci\agree\need science to learn other things |
| 45 | bsbs37c | sci\agree\need science to get into <uni></uni> |
| 46 | bsbs37d | sci\agree\need science to get job i want |
| 47 | bsbs37e | sci\agree\like job involving science |
| 48 | bsbs37f | sci\agree\get ahead in the world |
| 49 | bsbs37g | sci\agree\more job opportunities |
| 50 | bsbs37h | sci\agree\parents think science important |
| 51 | bsbs37i | sci\agree\important to do well in science class |
| 52 | bsbm38aa | math\how often tch give you hmwk\mat |
| 53 | bsdmwkhw | weekly time spent on math homework |
| 54 | bsdswkhs | weekly time spent on science homework |
| 55 | bcbg03a | gen\students background\economic disadva |
| 56 | bcbg03b | gen\students background\economic affluen |
| 57 | bcbg04 | gen\percent of students < lang of test> |
| 58 | bcbg05a | gen\how many people live in area |
| 59 | bcbg05b | gen\immediate area of sch location |
| 60 | bcbg06a | gen\free meals\breakfast |
| 61 | bcbg06b | gen\free meals\lunch |
| 62 | bcbg07c | gen\instructional days in 1 calender week |
| 63 | bcbg16a | gen\fill teaching vacancies\math |
| 64 | bcbg16b | gen\fill teaching vacancies\science |
| 65 | bcbg16c | gen\fill teaching vacancies\other |
| 66 | bcbg18a | gen\degree probs teach\arriving late at school |
| 67 | bcbg18b | gen\degree probs teach\absenteeism |
| 68 | bcbg21 | gen\highest level of formal education |
| 69 | bcdg03 | school composition by std background |
| 70 | bcbg07a | gen\instructional days per year |
| 71 | bcbg07b | gen\total instructional time\minutes |
| 72 | bcbg10 | gen\total number computers |
| 73 | bcbg19 | gen\years principal altogether |
| 74 | bcbg20 | gen\years principal at this school |
| 75 | itsex | sex of students |
| 76 | bsdage | students age |
| 77 | bsbgher | home educational resources/scl |
| 78 | bsbgssb | students sense of school belonging/scl |
| 79 | bsbgsb | student bullying/scl |
| 80 | bsbgslm | students like learning mathematics/scl |

| 81 | bsbgeml | engaging teaching in math lessons/scl |
|-----|--|--|
| 82 | bsbgscm | student confident in mathematics/scl |
| 83 | bsbgsvm | students value mathematics/scl |
| 84 | bsbgsls | students like learning science/scl |
| 85 | bsbgesl | engaging teaching in science lessons/scl |
| 86 | bsbgscs | student confident in sciences/scl |
| 87 | bsbgsvs | students value science/scl |
| 88 | bcbgsrs | instr aff by sci res shortage-prncpl/scl |
| 89 | bcbgeas | school emph on acad success-prncpl/scl |
| 90 | bcbgdas | school discipline problems-prncpl/scl |
| 91 | bsng07a.Less.than.hi gh.school | nat\derived\highest lvl edu\mother |
| 92 | bsng07a.Some.high. school | nat\derived\highest lvl edu\mother |
| 93 | bsng07a.High.school .graduate | nat\derived\highest IvI edu\mother |
| 94 | bsng07a.Associate.s. degree2.year.colleg e.program. | nat\derived\highest lvl edu\mother |
| 95 | bsng07a.Bachelor.s. degree4.year.colleg e.program. | nat\derived\highest lvl edu\mother |
| 96 | bsng07a.Master.s.de gree.or.professional. degreeMDDDSla wyerminister. | nat\derived\highest lvl edu\mother |
| 97 | bsng07a.Doctorate Ph.Dor.Ed.D | nat\derived\highest lvl edu\mother |
| 98 | bsng07b.Less.than.hi gh.school | nat\derived\highest lvl edu\father |
| 99 | bsng07b.Some.high. school | nat\derived\highest lvl edu\father |
| 100 | bsng07b.High.school .graduate | nat\derived\highest lvl edu\father |
| 101 | bsng07b.Associate.s. degree2.year.colleg e.program. | nat\derived\highest lvl edu\father |
| 102 | bsng07b.Bachelor.s. degree4.year.colleg e.program. | nat\derived\highest lvl edu\father |
| 103 | bsng07b.Master.s.de gree.or.professional. degreeMDDDSla wyerminister. | nat\derived\highest IvI edu\father |
| 104 | bsng07b.Doctorate Ph.Dor.Ed.D | nat\derived\highest lvl edu\father |
| 105 | bsbg09a.YES | gen\mother born in the us |
| 106 | bsbg09a.NO | gen\mother born in the us |
| 107 | bsbg09b.YES | gen\father born in the us |
| 108 | bsbg09b.NO | gen\father born in the us |

| 110 | msrace2.BlackNot. | |
|---------|--|--|
| | Hispanic | *nat\derived race-collapsed* |
| 111 | msrace2.Hispanic | *nat\derived race-collapsed* |
| 112 | msrace2.Asian | *nat\derived race-collapsed* |
| 113 | msrace2.Two.or.mor e.races | *nat\derived race-collapsed* |
| 114 1 | bcxg07.Regular.publi c.school | nat\type of school |
| 115 | bcxg07.A.regular.pu blic.school.with.a.m agnet.program | nat\type of school |
| 116 | bcxg07.A.magnet.sc hool.or.school.with. a.special.program.e mphasis | nat\type of school |
| 11/ | bcxg07.Charter.scho ol | nat\type of school |
| 118 | bcxg07.Privateinde pendent. | nat\type of school |
| 1 114 1 | bcxg07.Privatereligi ously.affiliated. | nat\type of school |
| 120 | bsxg04a | nat\activ outside school\sports team |
| 121 | bsxg04b | nat\activ outside school\music instrumnt |
| 122 | bsxg04c | nat\activ outside school\other class |
| 123 | bsxg04d | nat\activ outside school\club |
| 124 | bsxg05a | nat\participated in activ\science fair |
| 125 | bsxg05b | nat\participated in activ\science club |
| 126 | bsxg05c | nat\participated in activ\science comp |
| 127 | bsxg14a | nat\repeat grade\elementary |
| 128 | bsxg14b | nat\repeat grade\middle |
| 129 | bcxg20b | nat\teacher eval\math\oberv by external persons |
| 130 | bcxg20c | nat\teacher eval\math\student achieve |
| 131 | bcxg20d | nat\teacher eval\math\teacher peer review |
| 132 | bcxg21b | nat\teacher eval\science\oberv by external persons |
| 133 | bcxg21c | nat\teacher eval\science\student achieve |
| 134 | bcxg21d | nat\teacher eval\science\teacher peer review |
| 135 | bsng08 | nat\derived\how far educ |
| 136 | bsxg13b | nat\days absent last month |
| 137 | bsxg30 | nat\diff test compared oth tests |
| 138 | bsxg31 | nat\how hard tried compared oth tests |
| 139 | bsxg32 | nat\how important to do well |
| 140 | bcxg06 | nat\percent of students lep/ell |
| 141 | bcxg09 | nat\avg income lvl of sch immediate area |
| 142 | pctfrpl | *nat\percent stud free reduce lunch-categorized* |
| 143 | pubpriv | *nat\public private school indicator* |