Feedback — Homework 4

Help Center

You submitted this quiz on **Fri 11 Mar 2016 1:25 PM CST**. You got a score of **400.00** out of **400.00**. However, you will not get credit for it, since it was submitted past the deadline.

Question 1

Neural Network and Deep Learning

A fully connected Neural Network has $L = 2$; $d^{(0)} = 5,\ d^{(1)} = 3,\ d^{(2)} = 1$. If only products of the form $w_{ij}^{(\ell)} x_i^{(\ell-1)}$, $w_{ij}^{(\ell+1)} \delta_j^{(\ell+1)}$, and $x_i^{(\ell-1)} \delta_j^{(\ell)}$ count as operations (even for $x_0^{(\ell-1)} = 1$), without counting anything else, which of the following is the total number of operations required in a single iteration of backpropagation (using SGD on one data point)?

Your Answer		Score	Explanation
○ 53			
○ none of the other choices			
◉ 47	✔	20.00	
○ 43			
○ 59			
Total		20.00 / 20.00	

Question 2

Consider a Neural Network without any bias terms $x_0^{(\ell)}$. Assume that the network contains $d^{(0)} = 10$ input units, 1 output unit, and 36 hidden units. The hidden units can be arranged in any number of layers $\ell = 1, \cdots, L-1$, and each layer is fully connected to the layer above it. What is the minimum possible number of weights that such a network can have?

Your Answer	Score	Explanation

○ 44

○ 43

● 46 ✔ 20.00

○ none of the other choices

○ 45

Total 20.00 / 20.00

Question 3

Following Question 2, what is the maximum possible number of weights that such a network can have?

Your Answer		Score	Explanation
○ 500			
○ 520			
○ 510			
○ 490			
● none of the other choices	✔	20.00	
Total		20.00 / 20.00	

Question 4

Autoencoder

Assume an autoencoder with $\tilde{d} = 1$. That is, the $d \times \tilde{d}$ weight matrix W becomes a $d \times 1$ weight vector $\mathbf{w}$, and the linear autoencoder tries to minimize

$E_{in}(\mathbf{w}) = \frac{1}{N} \sum_{n=1}^{N} \|\mathbf{x}_n - \mathbf{w}\mathbf{w}^T\mathbf{x}_n\|^2$.

We can solve this problem with stochastic gradient descent by defining

$\mathrm{err}_n(\mathbf{w}) = \|\mathbf{x}_n - \mathbf{w}\mathbf{w}^T\mathbf{x}_n\|^2$

and calculate $\nabla_{\mathbf{w}}\mathrm{err}_n(\mathbf{w})$. What is $\nabla_{\mathbf{w}}\mathrm{err}_n(\mathbf{w})$?

Your Answer		Score	Explanation
$2(\mathbf{x}_n^T\mathbf{w})^2\mathbf{x}_n + 2(\mathbf{x}_n^T\mathbf{w})(\mathbf{w}^T\mathbf{w})\mathbf{w} - 4(\mathbf{x}_n^T\mathbf{w})\mathbf{w}$			
$(4\mathbf{w} - 4)(\mathbf{x}_n^T\mathbf{x}_n)$			
none of the other choices			
$2(\mathbf{x}_n^T\mathbf{w})^2\mathbf{w} + 2(\mathbf{x}_n^T\mathbf{w})(\mathbf{w}^T\mathbf{w})\mathbf{x}_n - 4(\mathbf{x}_n^T\mathbf{w})\mathbf{x}_n$	✔	20.00	
$(4\mathbf{x}_n - 4)(\mathbf{w}^T\mathbf{w})$			
Total		20.00 / 20.00	

Question 5

Following Question 4, assume that noise vectors ϵ_n are generated i.i.d. from a zero-mean, unit var iance Gaussian distribution and added to $\mathbf{x}_n$ to make $\tilde{\mathbf{x}}_n = \mathbf{x}_n + \epsilon_n$, a noisy version of $\mathbf{x}_n$. Then, the linear denoising autoencoder tries to minimize

$E_{in}(\mathbf{w}) = \frac{1}{N}\sum_{n=1}^N \|\mathbf{x}_n - \mathbf{w}\mathbf{w}^T(\mathbf{x}_n + \epsilon_n)\|^2$.

For any fixed $\mathbf{w}$, what is $\mathcal{E}(E_{in}(\mathbf{w}))$, where the expectation $\mathcal{E}$ is taken over the noise generation process?

Your Answer		Score	Explanation
$\frac{1}{N}\sum_{n=1}^N \|\mathbf{x}_n - \mathbf{w}\mathbf{w}^T\mathbf{x}_n\|^2 + d\mathbf{w}^T\mathbf{w}$			
$\frac{1}{N}\sum_{n=1}^N \|\mathbf{x}_n - \mathbf{w}\mathbf{w}^T\mathbf{x}_n\|^2 + \mathbf{w}^T\mathbf{w}$			
$\frac{1}{N}\sum_{n=1}^N \|\mathbf{x}_n - \mathbf{w}\mathbf{w}^T\mathbf{x}_n\|^2 + \frac{1}{d}\mathbf{w}^T\mathbf{w}$			
$\frac{1}{N}\sum_{n=1}^N \|\mathbf{x}_n - \mathbf{w}\mathbf{w}^T\mathbf{x}_n\|^2$ + (\mathbf{w}^T \mathbf{w})^2	✔	20.00	
none of the other choices			
Total		20.00 / 20.00	

Question 6

Nearest Neighbor and RBF Network

Consider getting the 1 Nearest Neighbor hypothesis from a data set of two examples $(\mathbf{x}_+, +1)$ and $(\mathbf{x}_-, -1)$. Which of the following linear hypothesis $g_{LIN}(\mathbf{x}) = \text{sign}(\mathbf{w}^T\mathbf{x} + b)$ (where $\mathbf{w}$ does not include $b = w_0$) is equivalent to the hypothesis?

Your Answer		Score	Explanation
○ $\mathbf{w} = 2(\mathbf{x}_+ - \mathbf{x}_-)$, $b = +\mathbf{x}_+^T\mathbf{x}_-$			
○ $\mathbf{w} = 2(\mathbf{x}_- - \mathbf{x}_+)$, $b = -\mathbf{x}_+^T\mathbf{x}_-$			
○ none of the other choices			
○ $\mathbf{w} = 2(\mathbf{x}_- - \mathbf{x}_+)$, $b = +\|\mathbf{x}_+\|^2 - \|\mathbf{x}_-\|^2$			
◉ $\mathbf{w} = 2(\mathbf{x}_+ - \mathbf{x}_-)$, $b = -\|\mathbf{x}_+\|^2 + \|\mathbf{x}_-\|^2$	✔	20.00	
Total		20.00 / 20.00	

Question 7

Consider an RBF Network hypothesis for binary classification

$g_{RBFNET}(\mathbf{x}) = \text{sign}\big(\beta_+ \exp(-\|\mathbf{x} - \boldsymbol{\mu}_+\|^2) + \beta_- \exp(-\|\mathbf{x} - \boldsymbol{\mu}_-\|^2)\big)$

and assume that $\beta_+ > 0 > \beta_-$. Which of the following linear hypothesis

$g_{LIN}(\mathbf{x}) = \text{sign}(\mathbf{w}^T\mathbf{x} + b)$ (where $\mathbf{w}$ does not include $b = w_0$) is equivalent to $g_{RBFNET}(\mathbf{x})$?

Your Answer		Score	Explanation
◉ $\mathbf{w} = 2(\boldsymbol{\mu}_+ - \boldsymbol{\mu}_-)$, $b = \ln\left\|\frac{\beta_+}{\beta_-}\right\| - \|\boldsymbol{\mu}_+\|^2 + \|\boldsymbol{\mu}_-\|^2$	✔	20.00	
○ $\mathbf{w} = 2(\boldsymbol{\mu}_- - \boldsymbol{\mu}_+)$, $b = \ln\left\|\frac{\beta_-}{\beta_+}\right\| + \|\boldsymbol{\mu}_+\|^2 - \|\boldsymbol{\mu}_-\|^2$			
○ $\mathbf{w} = 2(\beta_+\boldsymbol{\mu}_+ + \beta_-\boldsymbol{\mu}_-)$, $b = -\beta_+\|\boldsymbol{\mu}_+\|^2 + \beta_-\|\boldsymbol{\mu}_-\|^2$			
○ $\mathbf{w} = 2(\beta_+\boldsymbol{\mu}_+ + \beta_-\boldsymbol{\mu}_-)$, $b = +\beta_+\|\boldsymbol{\mu}_+\|^2 - \beta_-\|\boldsymbol{\mu}_-\|^2$			
○ none of the other choices			
Total		20.00 / 20.00	

Question 8

Assume that a full RBF network (page 9 of class 214) using $\mathrm{RBF}(\mathbf{x}, \boldsymbol{\mu}) = [[\mathbf{x} = \boldsymbol{\mu}]]$ is solved for squared error regression on a data set where all inputs $\mathbf{x}_n$ are different. What are the optimal coefficients β_n for each $\mathrm{RBF}(\mathbf{x}, \mathbf{x}_n)$?

Your Answer		Score	Explanation
○ $\|\mathbf{x}_n\| y_n$			
○ y_n^2			
○ none of the other choices			
◉ y_n	✔	20.00	
○ $\|\mathbf{x}_n\|^2 y_n^2$			
Total		20.00 / 20.00	

Question 9

Matrix Factorization

Consider matrix factorization of $\tilde{d} = 1$ with alternating least squares. Assume that the $\tilde{d} \times N$ user factor matrix V is initialized to a constant matrix of 1. After step 2.1 of alternating least squares (page 10 of lecture 215), what is the optimal w_m, the $\tilde{d} \times 1$ movie `vector' for the m-th movie?

Your Answer		Score	Explanation
◉ the average rating of the m-th movie	✔	20.00	
○ the total rating of the m-th movie			
○ the maximum rating of the m-th movie			
○ the minimum rating of the m-th movie			
○ none of the other choices			
Total		20.00 / 20.00	

Question 10

Assume that for a full rating matrix R, we have obtained a perfect matrix factorization $\mathrm{R} = \mathrm{V}^T\mathrm{W}$. That is, $r_{nm} = \mathbf{v}_n^T\mathbf{w}_m$ for all n, m. Then, a new user $(N+1)$ comes. Because we do not have any information for the type of the movie she likes, we initialize her feature vector $\mathbf{v}_{N+1}$ to $\frac{1}{N}\sum_{n=1}^{N}\mathbf{v}_n$, the average user feature vector. Now, our system decides to recommend her a movie m with the maximum predicted score $\mathbf{v}_{N+1}^T\mathbf{w}_m$. What would the movie be?

Your Answer		Score	Explanation
○ the movie with the smallest rating variance			
○ the movie with the largest minimum rating			
○ none of the other choices			
○ the movie with the largest maximum rating			
◉ the movie with the largest average rating	✔	20.00	
Total		20.00 / 20.00	

Question 11

Experiment with Backprop neural Network

Implement the backpropagation algorithm (page 16 of lecture 212) for d-M-1 neural network with $\tanh$-type neurons, **including the output neuron**. Use the squared error measure between the output $g_{NNET}(\mathbf{x}_n)$ and the desired y_n and backprop to calculate the per-example gradient. Because of the different output neuron, your $\delta_1^{(L)}$ would be different from the course slides! Run the algorithm on the following set for training (each row represents a pair of $(\mathbf{x}_n, y_n)$; the first column is $(\mathbf{x}_n)_1$; the second one is $(\mathbf{x}_n)_2$; the third one is y_n):
hw4_nnet_train.dat
and the following set for testing:
hw4_nnet_test.dat

Fix $T = 50000$ and consider the combinations of the following parameters:

- the number of hidden neurons M
- the elements of $w_{ij}^{(\ell)}$ chosen independently and uniformly from the range $(-r, r)$
- the learning rate η

Fix $\eta = 0.1$ and $r = 0.1$. Then, consider $M \in \{1, 6, 11, 16, 21\}$ and repeat the experiment for 500 times. Which M results in the lowest average E_{out} over 500 experiments?

Your Answer		Score	Explanation
○ 11			
○ 1			
○ 21			
○ 16			
◉ 6	✔	20.00	
Total		20.00 / 20.00	

Question 12

Following Question 11, fix $\eta = 0.1$ and $M = 3$. Then, consider $r \in \{0, 0.1, 10, 100, 1000\}$ and repeat the experiment for 500 times. Which r results in the lowest average E_{out} over 500 experiments?

Your Answer		Score	Explanation
○ 1000			
○ 10			
○ 100			
◉ 0.1	✔	20.00	
○ 0			
Total		20.00 / 20.00	

Question 13

Following Question 11, fix $r = 0.1$ and $M = 3$. Then, consider $\eta \in \{0.001, 0.01, 0.1, 1, 10\}$ and repeat the experiment for 500 times. Which η results in the lowest average E_{out} over 500

experiments?

Your Answer		Score	Explanation
0.01	✔	20.00	
0.001			
0.1			
10			
1			
Total		20.00 / 20.00	

Question 14

Following Question 11, deepen your algorithm by making it capable of training a d-8-3-1 neural network with $\tanh$-type neurons. Do not use any pre-training. Let $r = 0.1$ and $\eta = 0.01$ and repeat the experiment for 500 times. Which of the following is true about E_{out} over 500 experiments?

Your Answer		Score	Explanation
$0.00 \leq E_{out} < 0.02$			
none of the other choices			
$0.06 \leq E_{out} < 0.08$			
$0.02 \leq E_{out} < 0.04$	✔	20.00	
$0.04 \leq E_{out} < 0.06$			
Total		20.00 / 20.00	

Question 15

Experiment with 1 Nearest Neighbor

Implement any algorithm that `returns' the 1 Nearest Neighbor hypothesis discussed in page 8

of lecture 214. $g_{\text{nbor}}(\mathbf{x}) = y_m$ such that $\mathbf{x}$ closest to $\mathbf{x}_m$
Run the algorithm on the following set for training:
hw4_knn_train.dat
and the following set for testing:
hw4_knn_test.dat

Which of the following is closest to $E_{in}(g_{\text{nbor}})$?

Your Answer		Score	Explanation
0.2			
0.1			
0.0	✔	20.00	
0.3			
0.4			
Total		20.00 / 20.00	

Question 16

Following Question 15, which of the following is closest to $E_{out}(g_{\text{nbor}})$?

Your Answer		Score	Explanation
0.32			
0.28			
0.30			
0.26			
0.34	✔	20.00	
Total		20.00 / 20.00	

Question 17

Now, implement any algorithm for the k Nearest Neighbor with $k = 5$ to get $g_{5\text{-nbor}}(\mathbf{x})$. Run the algorithm on the same sets in Question 15 for training/testing.

Which of the following is closest to $E_{in}(g_{5\text{-nbor}})$?

Your Answer		Score	Explanation
○ 0.1			
○ 0.4			
◉ 0.2	✔	20.00	
○ 0.0			
○ 0.3			
Total		20.00 / 20.00	

Question 18

Following Question 17, Which of the following is closest to $E_{out}(g_{5\text{-nbor}})$

Your Answer		Score	Explanation
◉ 0.32	✔	20.00	
○ 0.28			
○ 0.30			
○ 0.34			
○ 0.26			
Total		20.00 / 20.00	

Question 19

Experiment with k-Means

Implement the k-Means algorithm (page 16 of lecture 214).Randomly select k instances from $\{\mathbf{x}_n\}$ to initialize your $\boldsymbol{\mu}_m$ Run the algorithm on the following set for training:
hw4_kmeans_train.dat

and repeat the experiment for 500 times. Calculate the clustering E_{in} by
$\frac{1}{N}\sum_{n=1}^{N}\sum_{m=1}^{M}[[\mathbf{x}_n \in S_m]]\|\mathbf{x}_n - \boldsymbol{\mu}_m\|^2$
as described on page 13 of lecture 214 for $M = k$.

For $k = 2$, which of the following is closest to the average E_{in} of k-Means over 500 experiments?

Your Answer		Score	Explanation
2.0			
1.0			
0.5			
1.5			
2.5	✔	20.00	
Total		20.00 / 20.00	

Question 20

For $k = 10$, which of the following is closest to the average E_{in} of k-Means over 500 experiments?

Your Answer		Score	Explanation
1.0			
1.5	✔	20.00	
0.5			
2.5			
2.0			
Total		20.00 / 20.00	