CZ4041: Tutorial Week 10

Due on March 25, 2021 at 8:30am

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Problem 1

Given the distance matrix shown in Table 1, use a dendrogram to show how to perform agglomerative hierarchical clusturing algorithm with Single Link on the distance matrix.

Table 1: Distance matrix.

| | P1 | P2 | P3 | P4 | P5 |
|----|------|-----|-----|------|-----|
| P1 | 0 | 0.9 | 0.1 | 0.65 | 0.2 |
| P2 | 0.9 | 0 | 0.7 | 0.6 | 0.5 |
| P3 | 0.1 | 0.7 | 0 | 0.4 | 0.3 |
| P4 | 0.65 | 0.6 | 0.4 | 0 | 0.8 |
| P5 | 0.2 | 0.5 | 0.3 | 0.8 | 0 |

Solution

1) Merge P1 & P3 (0.1)

| | P1&P3 | P2 | P4 | P5 |
|-------|-------|-----|-----|-----|
| P1&P3 | 0 | 0.7 | 0.4 | 0.2 |
| P2 | 0.7 | 0 | 0.6 | 0.5 |
| P4 | 0.4 | 0.6 | 0 | 0.8 |
| P5 | 0.2 | 0.5 | 0.8 | 0 |

2) Merge P1/P3 & P5 (0.2)

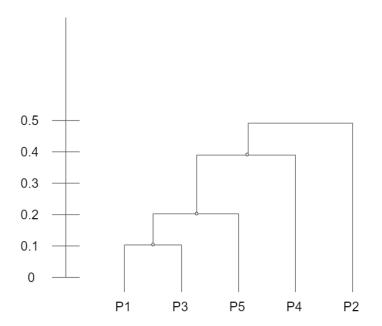
| | P1/P3/P5 | P2 | P4 |
|----------|----------|-----|-----|
| P1/P3/P5 | 0 | 0.5 | 0.4 |
| P2 | 0.5 | 0 | 0.6 |
| P4 | 0.4 | 0.6 | 0 |

3) Merge P1/P3/P5 & P4 (0.4)

| | P1/P3/P4/P5 | P2 |
|-------------|-------------|-----|
| P1/P3/P4/P5 | 0 | 0.5 |
| P2 | 0.5 | 0 |

4) Merge P1/P3/P4/P5 & P2 (0.5)

Therefore, the dendrogram showing the hierarchical clustering is shown below:



Problem 2

On the 59th page of the lecture notes "Lecture 10", use a dendrogram to show how to perform hierarchical clustering with Complete Link on the similarity matrix.

| | P1 | P2 | Р3 | P4 | P5 |
|----|------|------|------|------|------|
| P1 | 1.00 | 0.90 | 0.10 | 0.65 | 0.20 |
| P2 | 0.90 | 1.00 | 0.70 | 0.60 | 0.50 |
| Р3 | 0.10 | 0.70 | 1.00 | 0.40 | 0.30 |
| P4 | 0.65 | 0.60 | 0.40 | 1.00 | 0.80 |
| P5 | 0.20 | 0.50 | 0.30 | 0.80 | 1.00 |

Similarity matrix

Solution

1) Merge P1 & P2 (0.9)

| | P1&P2 | Р3 | P4 | P5 |
|-------|-------|-----|-----|-----|
| P1&P2 | 1 | 0.1 | 0.6 | 0.2 |
| P3 | 0.1 | 1 | 0.4 | 0.3 |
| P4 | 0.6 | 0.4 | 1 | 0.8 |
| P5 | 0.2 | 0.3 | 0.8 | 1 |

2) Merge P4 & P5 (0.8)

| | P1&P2 | Р3 | P4&P5 |
|-------|-------|-----|-------|
| P1&P2 | 1 | 0.1 | 0.2 |
| P3 | 0.1 | 1 | 0.3 |
| P4&P5 | 0.2 | 0.3 | 1 |

3) Merge P4/P5 & P3 (0.3)

| | P1&P2 | P3&P4&P5 |
|----------|-------|----------|
| P1&P2 | 1 | 0.1 |
| P3&P4&P5 | 0.1 | 1 |

4) Merge P1/P2 & P3/P4/P5 (0.1)

Therefore, the dendrogram showing the hierarchical clustering is shown below:

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