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%% PROGRAMMING TOOLS AND METHODS FOR MECHATRONICS ENGINEERS
% HW#5 :Done by Yusri Al-Sanaani
% This program used to solve PDE-heat equation using ADI method.
close all; clear all ;clc
%% initializations
dx=1/30; dy=1/30; dt=.01;           % step size in (X,Y)direction & time
x=0:dx:1; y=0:dy:1; t=0:dt:1;      % x,y,&time vectors
nx=length(x); ny=length(y); l=length(t);
%% TRIGONAL MATRIX TO FIND A1 of first left hand side
alpha=1;
a1=((2/dt)+((2*alpha)/(dy^2))); a2=(-1*alpha)/(dy^2);
b1=((2/dt)-((2*alpha)/(dx^2)));
A1=diag((a1*ones(nx,1)))+diag(a2*ones(nx-1,1),1)+diag(a2*ones(nx-1,1),-1);
A1(1,1:3)=[1 0 0];A1(end,end-2:end)=[0 0 1];
%% TRIGONAL MATRIX TO FIND A2 of second left hand side
a3=((2/dt)+((2*alpha)/(dx^2))); a4=(-1*alpha)/(dx^2);
b2=((2/dt)-((2*alpha)/(dy^2)));
A2=diag((a3*ones(ny,1)))+diag(a4*ones(ny-1,1),1)+diag(a4*ones(ny-1,1),-1);
A2(1,1:3)=[1 0 0];A2(end,end-2:end)=[0 0 1];
%%
T=zeros(nx,ny,l);                  % Temperature matrix
for w=1:l
    T(end,:,w)=zeros(1,nx);        % BC in X-direction
    T(:,end,w)=sin(pi*x);          % BC in Y-direction
end
Thalf=T;                           % inititation of half-time step matrix
Tfull=T;                           % inititation of full-time step matrix
%% looping through all times
for k=2:l
    for i=2:nx-1                   % looping through each raw
        F1l=-a4*T(i-1,:,k-1)+b1*T(i,:,k-1)-a4*T(i+1,:,k-1); % Updates F1 matrix from
Equ.#1
        F1=F1l';
        F1(1,1)=0; F1(end,1)=sin(pi*x(i));
        Ty=A1\F1;
        Thalf(i,:,k)=Ty;          % sol. for all lines is ready in Thalf matrix
    end
    for j=2:ny-1                   % looping through each column
        F2=-a2*Thalf(:,j-1,k)+b2*Thalf(:,j,k)-a2*Thalf(:,j+1,k);% Updates F2 matrix from
Equ.#2
        F2(1,1)=0;F2(end,1)=0;
        Tx=A2\F2;
        Tfull(:,j,k)=Tx;          % sol. for all lines is ready in Tfull matrix
    end
    T(:, :,k)=Tfull(:, :,k);       % Temperaturein full-time matrix
end
for j=2:5:l;
    surf(x,y,T(:, :,j));axis([0 1 0 1 0 1]);
    xlabel('X'),ylabel('Y'),zlabel('Temperature'),title('Temperature Profile')
    pause(0.2)
end

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