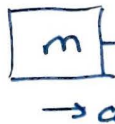


Engineering is purposeful use of science. Science provides an understanding of natural phenomena. Abstraction provides bridge between real-world / experimental data and practitioners / engineers who want to use specific phenomena to achieve their goals.

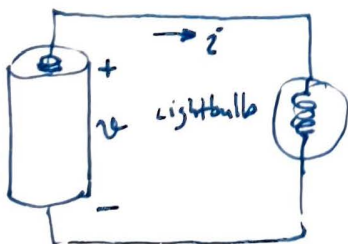
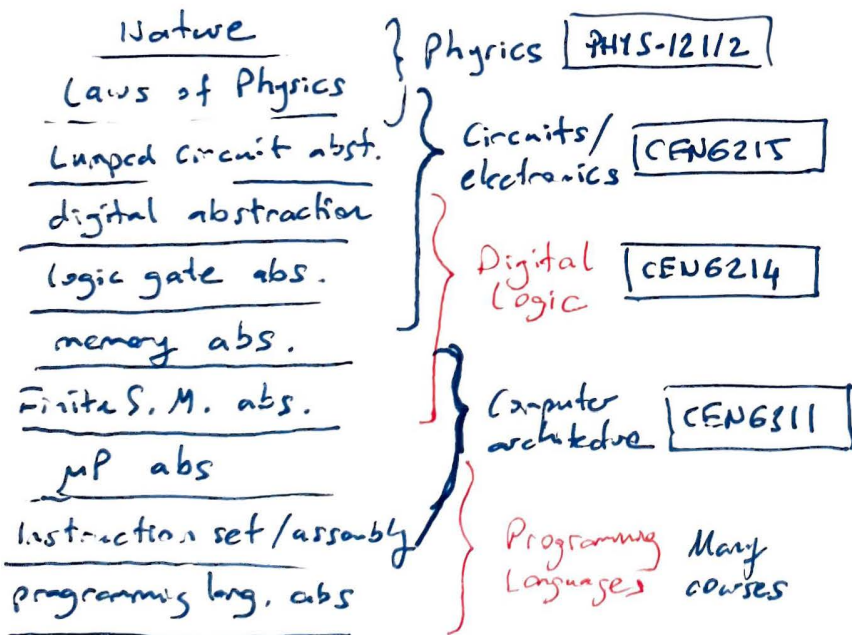
Newton's laws of motion :  $F = ma$  (Model / abstraction)

Einstein :  $m = m_0 / \sqrt{1 - v^2/c^2}$

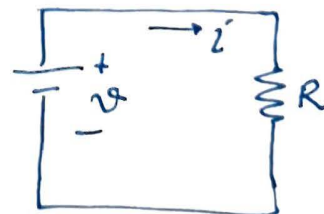
  $F$  : Actually complex but this model ignores many details about the system.

Electrical engineering and computer science is the purposeful use of Maxwell's equations (abstractions). Elk. Eng creates a new abstraction : Lumped circuit abstraction !

There are also other abstractions :



Model

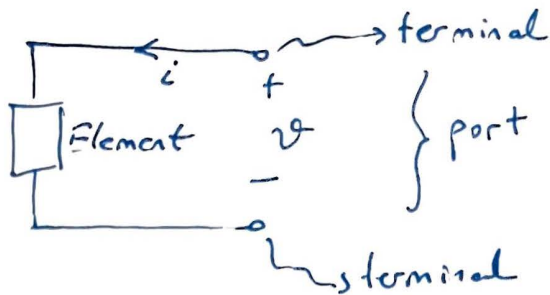


$$i = \frac{v}{R} \quad (\Leftrightarrow) \quad v = R i$$

# Lumped Elements / Block box approach

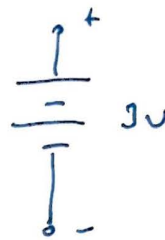
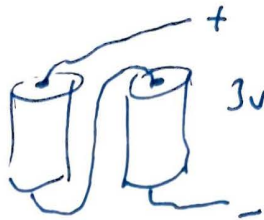
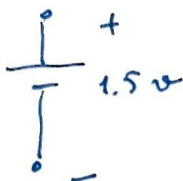
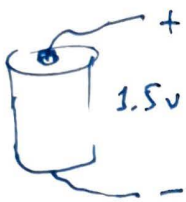
(2)

Two-terminal elements:



Element: battery, resistance, capacitor, inductor...

Batteries:



$$p = v \cdot i \text{ (Power in Watt)}$$

if  $p$  is constant over interval  $T$ , energy  $w$  is supplied:

$$w = P \cdot T \text{ (Joules)} \quad \text{or} \quad w = \int_{t_1}^{t_2} v(t) i(t) dt$$

Watt-seconds

\* if battery supplies 1 W power over 1 second, it delivers 1 Joule energy.

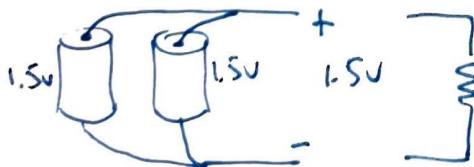
\* Car battery: 12 V, 50 Ah (Ampere-hours)

It can provide 1 A for 50 hours.

100 A for 30 minutes

$$\text{Energy stored} = 12 \cdot 50 = 600 \text{ W.hours} = 600 \cdot 3600 = 2.16 \cdot 10^6 \text{ Joules}$$

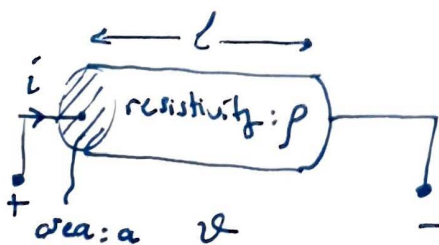
\* To increase the energy, double batteries in parallel:



Power is dissipated here in the form of heat or light  
 $v = R \cdot i$

$$v = 1.5 \text{ V}, R = 10 \Omega \text{ (lightbulb)} \Rightarrow i = \frac{v}{R} = 150 \text{ mA}$$

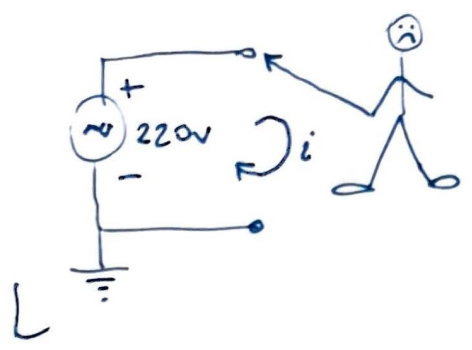
Study: [ ... T, G, M, k, m,  $\mu$ , p, f ... ]



$R = \rho \cdot \frac{l}{a}$  resistance of a piece of material is proportional to its length, inversely prop. to its cross-sectional area.

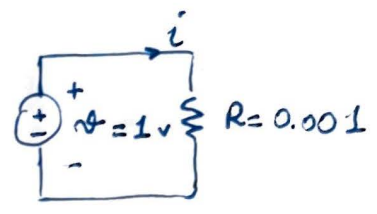
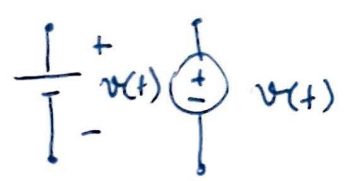
For a wire:  $R = \rho \cdot \frac{l}{\pi r^2}$

Question: What kills a human? Voltage or current?



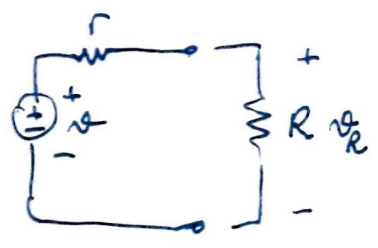
$i \geq 100 \text{ mA}$  kills!  
 $R \approx 2 \text{ k}\Omega$

\* Ideal Voltage Source, wire, resistor



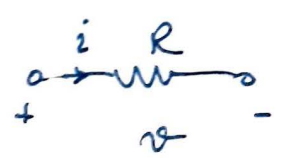
$i = 1000 \text{ A}$  (?)  
 not possible for a simple source to provide 1000 A.

Voltage source is modeled as:



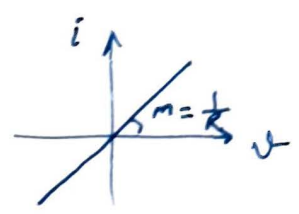
$r$  is unwanted internal resistance. e.g.  $r = 0.1 \Omega$   
 even for  $R = 0.001$   $i \approx \frac{1}{0.1} = 10 \text{ A}$

$\Rightarrow v_R \approx 0 \text{ V}$



$v = R \cdot i$  (ohm's law)  
 $i = G \cdot v$  ( $R = \frac{1}{G}$ )

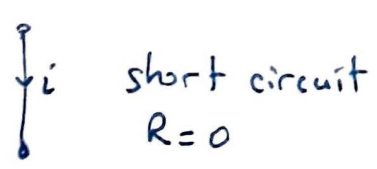
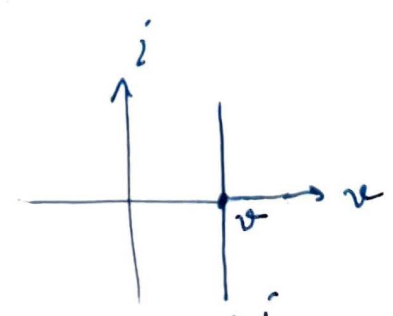
$R$ : resistance (ohm)  
 $G$ : conductance (siemens)



(R)

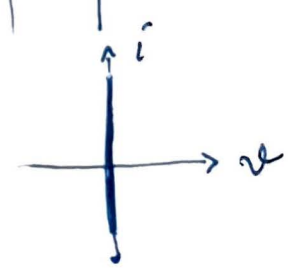
$v-i$  characteristic

ideal voltage source:

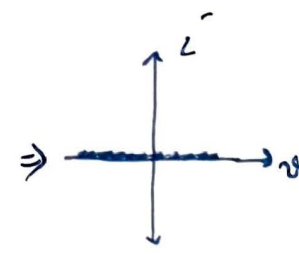


short circuit  
 $R = 0$

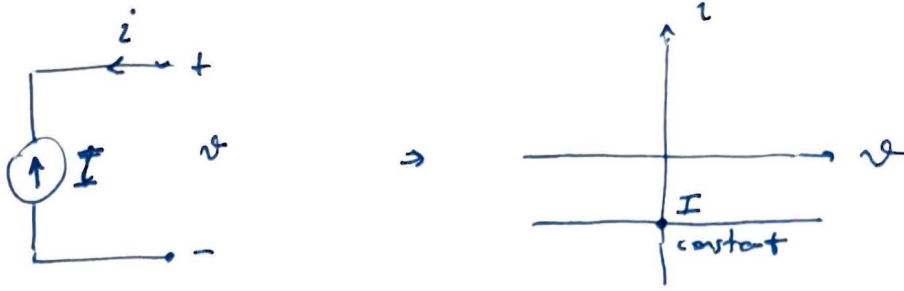
$\Rightarrow$



open circuit  
 $R = \infty$



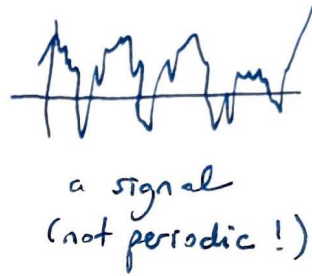
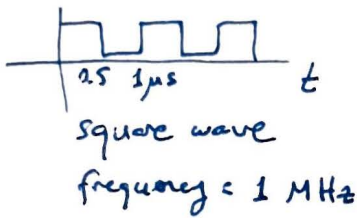
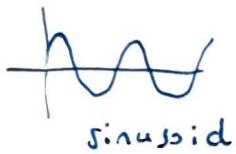
ideal current source :



## SIGNALS

**ANALOG** : signals in physical world. Spanning continuous values.

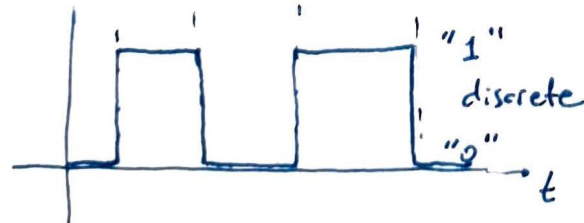
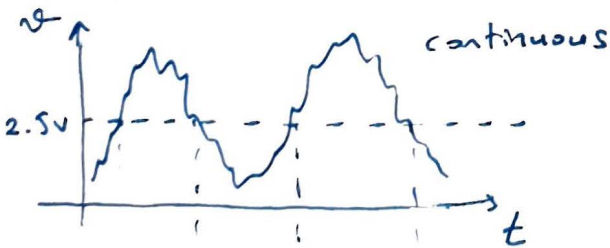
- How many values a voltage source can take between 0V and 5V ?  
The answer is infinite !  $\infty$



$$v(t) = A \sin(\omega t + \phi)$$

$A$  : amplitude  
 $\omega$  : frequency  
 $\phi$  : phase  
 $t$  : time

## **DIGITAL**



digital abstraction :  
signal is quantized into two values.  
 $\Rightarrow$  binary signal.

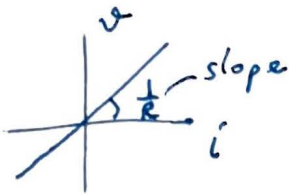
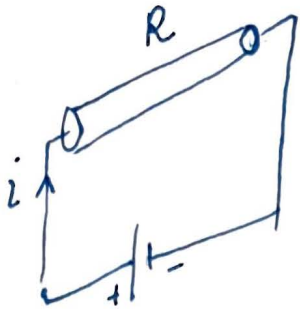
Advantage is "Better noise immunity"



# Other Lumped Devices

(5)

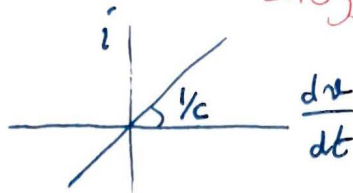
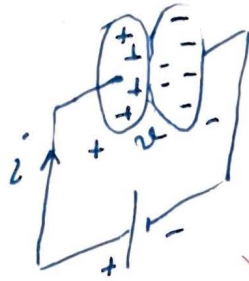
## Resistance



$$v = R \cdot i$$

resistance (Ohm:  $\Omega$ )

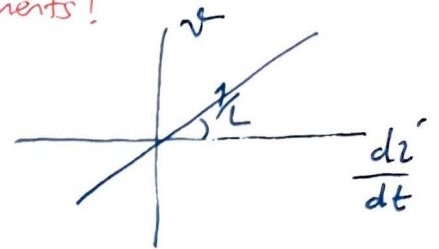
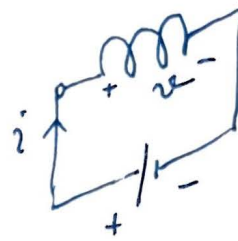
## Capacitance



$$i = C \frac{dv}{dt}$$

capacitance (Farads: F)

## Inductance



$$v = L \frac{di}{dt}$$

inductance (Henry: H)

Energy storage elements!

- \* Capacitance is a measure of the ability of a device to store energy in the form of separated charge or in the form of an electric field.
- \* Inductance is a measure of the ability of a device to store energy in the form of moving charge or in the form of magnetic field.
- \* They store energy and can give it back!
- \* Resistance is a measure of the ability of a device to dissipate power irreversibly!