



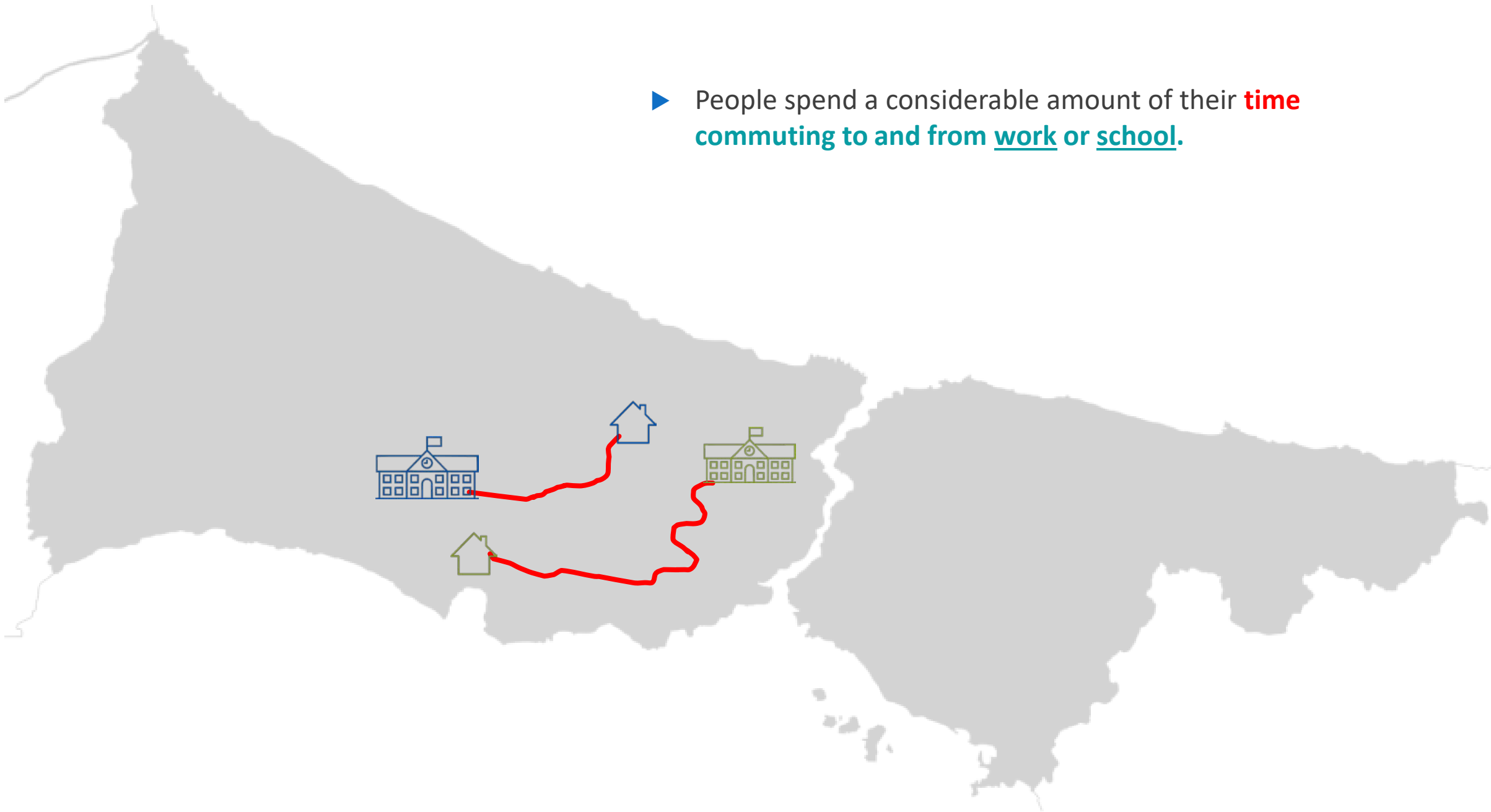
An Agent-based Home Exchange Model To Reduce Commuting Times of University Students

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ISTANBUL, TURKEY

- ▶ People spend a considerable amount of their **time** commuting to and from work or school.



► The question is;

“What if we exchange our homes?”



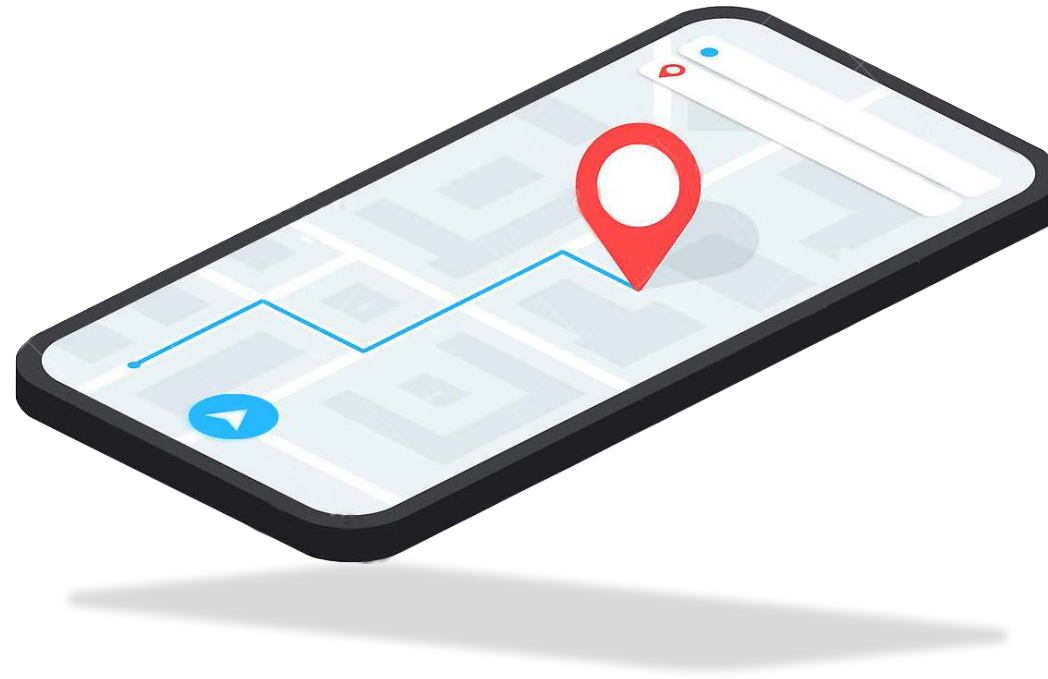
- 
- ▶ The question is;

“What if we exchange our homes?”

- ▶ This model can **reduce commute times** in big cities?

Home Exchange Model for University Students

- ▶ In order to contribute to developing smart and sustainable urban planning policies, this study proposes **home exchange model** for university students to **reduce commuting times**.
- ▶ This study aims at developing a computer application to improve the feasibility of smart and sustainable city concepts.
- ▶ In accordance with this purpose, **a problem specific matching algorithm** has been designed for home exchange problem and the algorithm has been applied on a virtual data.
- ▶ The results of the home exchange model are presented.



- ▶ MoovIt is a **mobile application** and a **web service** that **provides** travelers with **public transit data**, including the best route for their journey.
- ▶ **Users also can participate** in MoovIt Community and contribute with sending active reports about their travel experience, such as bus congestion levels, cleanliness, and more to help others have a better travel experience.
- ▶ **MoovIt analyzes usage data and travel patterns** and **compiles the MoovIt Public Transit Index** with statistics about the **average commute times** for different cities across the world.



Commute Time

moovit **INSIGHTS**

Moovit Public Transit Index

How long do people usually commute in Istanbul by public transit everyday?

The average amount of time people spend commuting with public transit, for example to and from work, on a weekday.

91 min

How many people have a long commute every day with public transit in Istanbul, Turkey?

The percentage of transit riders who ride public transit for more than 2 hours every day. This includes travel by Tram, Metro, Train, Bus, Ferry, Cable Car & Funicular.

30%



Waiting Time

How long do people usually wait at a station in Istanbul every day?

The average amount of time people wait at a stop or station for their Tram, Metro, Train, Bus, Ferry, Cable Car & Funicular line on a weekday.

19 min

How many people in Istanbul usually wait a long time at a transit station?

The percentage of people who wait for over 20 minutes on average for their transit line every day, for example to and from work.

36%



1

creating
home and
university
databases

2

constructing
a travel time
distance
matrix

3

initial state
distribution

4

home
exchange
matching

This study
consists of
four steps

university database

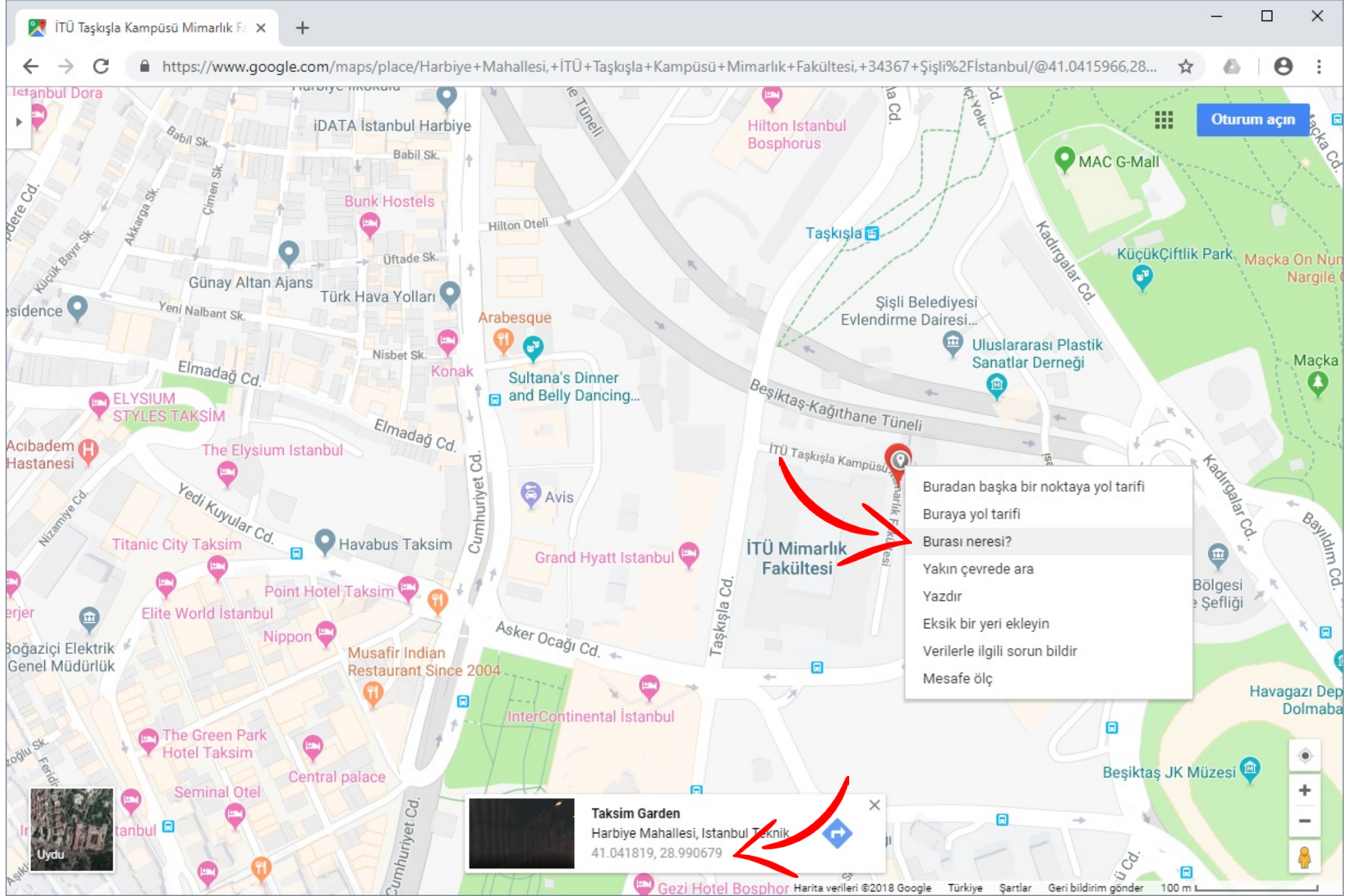
- **25 university campus locations**, which are located at European side of Istanbul city, have been chosen for university database.

- | | |
|-----------------------------------|-----------------------------------------|
| 1. Altınbaş Üniversitesi | 14. İTÜ Ayazağa Yerleşkesi |
| 2. Bahçeşehir Üniversitesi | 15. İTÜ Taşkışla Yerleşkesi |
| 3. Beykent Üniversitesi | 16. İstanbul Üniversitesi Tıp Fakültesi |
| 4. Boğaziçi Üniversitesi | 17. Cerrahpaşa Tıp Fakültesi |
| 5. Galatasaray Üniversitesi | 18. İstanbul Yeni Yüzyıl Üniversitesi |
| 6. Haliç Üniversitesi | 19. İstinye Üniversitesi |
| 7. İstanbul Arel Üniversitesi | 20. Kadir Has Üniversitesi |
| 8. İstanbul Aydın Üniversitesi | 21. Koç Üniversitesi |
| 9. İstanbul Bilgi Üniversitesi | 22. MEF Üniversitesi |
| 10. İstanbul Bilim Üniversitesi | 23. MSGSÜ Mimarlık Fakültesi |
| 11. İstanbul Gelişim Üniversitesi | 24. Nişantaşı Üniversitesi |
| 12. İstanbul Kültür Üniversitesi | 25. Yıldız Teknik Üniversitesi |
| 13. İstanbul Rumeli Üniversitesi | |

Table 1. University campus locations, which are located at European side of Istanbul city.

1

creating
home and
university
databases



home database

- For home database, rental house search sites have been browsed. The search filtered by number of rooms and rental price then **180 home locations** have been chosen.

ZINGAT GAYRİMENKUL BİLGİ SİSTEMLERİ A.Ş. [TR] | https://www.zingat.com/istanbul-avrupa-kiralik-daire?page=1&page_size=20&listingTypeId=2&propertyTypeId=64&location=istanbul

zingat Satılık **Kiralık**

🏠 > Kiralık Daire > İstanbul Kiralık Daire

Gayrimenkul Tipi
Daire ▼

İl, İlçe, Mahalle
İstanbul (Avrupa) ▼

Fiyat (TL)
1.500 - 2.500... ▼

Metrekare (m²) ▼

Oda Sayısı
2+1, 3+1 ▼

İstanbul Kiralık Daire (1.783 sonuç bulundu.)

Figure 2. The search filtered by number of rooms (2+1 and 3+1), rental price (1500-2000) and location (Istanbul-European side).

1

creating
home and
university
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BAĞCILAR EVREN MAHALLESİ'NE x Google Haritalar x 41°02'20.3"N 28°49'41.5"E - Google x +

← → ↺ ZINGAT GAYRİMENKUL BİLGİ SİSTEMLERİ A.Ş. [TR] | https://www.zingat.com/bagcilar-evren-mahallesinde-site-icinde-kiralik-3-1-daire-1875929i ☆ ⚙️ 👤 ⋮

zingat Satılık **Kiralık** Günlük Kiralık Projeler Zingat Rehber Giriş Yap Üye Ol İLAN VER

🏠 > Kiralık Daire > İstanbul Kiralık Daire > Bağcılar Kiralık Daire > Güneşli Kiralık Daire

BAĞCILAR EVREN MAHALLESİ'NDE SITE İÇİNDE KİRALIK 3+1 DAİRE 1.850 TL

📍 Güneşli, Bağcılar, İstanbul ilan No: 1875929

Fotoğraf Harita / Yakın Çevre Sokak Görünümü 360° 360 Görünüm

Yakın Çevre Harita Uydu Uzaklık 1 Km

Yakın Çevre Harita Uydu Uzaklık 1 Km

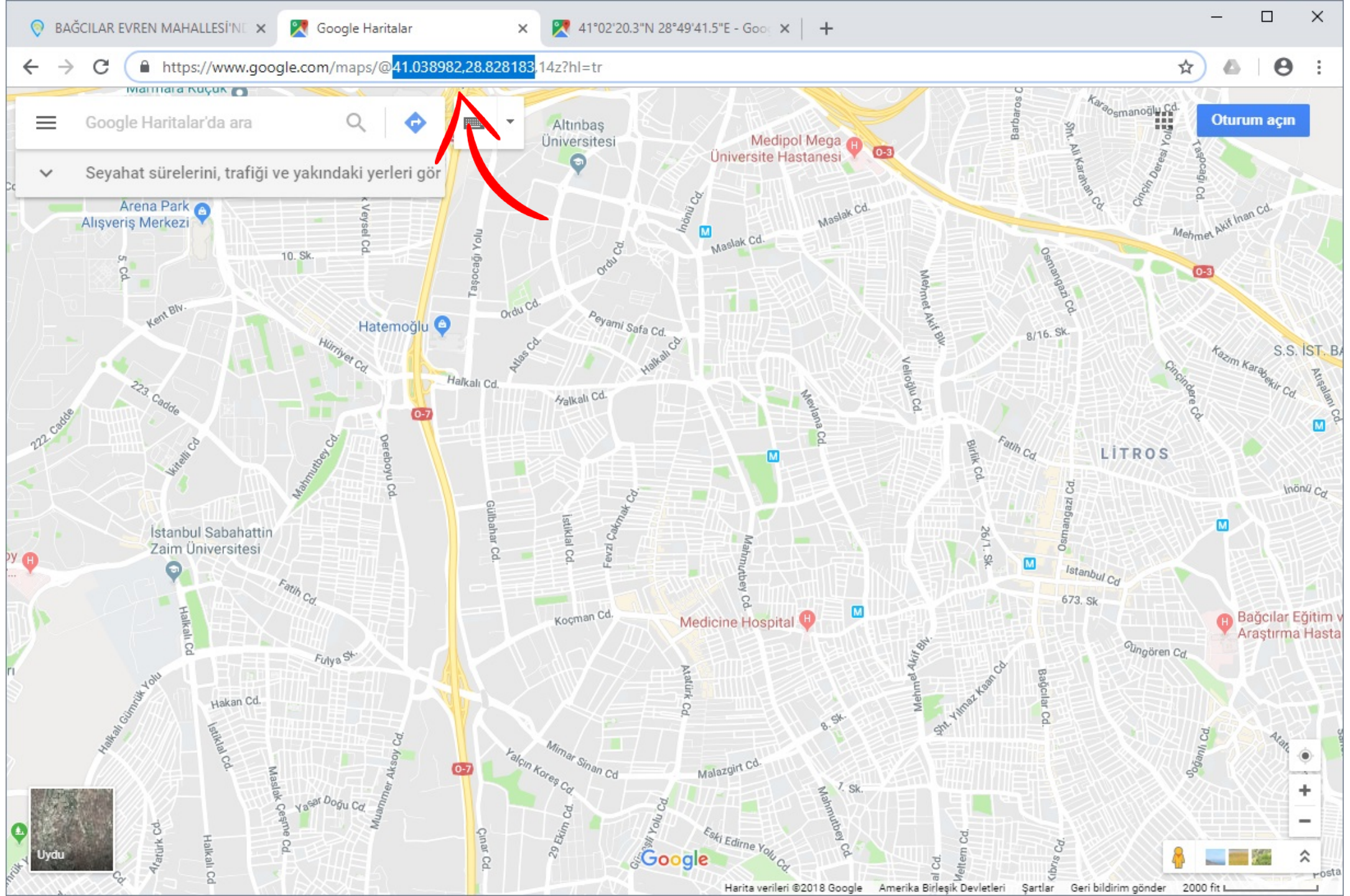
Google

https://maps.google.com/maps?ll=41.038982,28.828183&z=14&t=m&hl=tr&gl=US&mapclient=apiv3

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1

creating
home and
university
databases



1

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home and
university
databases

BAĞCILAR EVREN MAHALLESİ'NE x Google Haritalar x 41°02'20.3"N 28°49'41.5"E - Google x

← → ↺ https://www.google.com/maps/place/41°02'20.3"N+28°49'41.5"E/@41.038986,28.8259943,17z/data=!4m5!3m4!1s0x0:0x0!8m2!3d41.038982!4d28... ☆

41.038982,28.828183

41°02'20.3"N 28°49'41.5"E
41.038982, 28.828183

Yol tarifi

KAYDET YAKIN ÇEVRE TELEFONUNUZA GÖNDERİN PAYLAŞ

2RQH+H7 Litros, Fatih Mahallesi, Esenler/İstanbul
Eksik bir yeri ekleyin

Uydu

Gülistan Evleri Çiğdem Eczanesi Mert Dügün Sarayı EB GARAJ

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Konut Veritabanı 180.txt - Not Defteri	
Dosya	Düzen
41.017275,28.621058	
41.015626,28.641038	
41.002118,28.64206	
41.01041,28.658824	
41.013632,28.659682	
41.104785,28.669164	
40.976901,28.674569	
41.015713,28.682207	
41.012953,28.68434	
41.001278,28.7044	
40.997326,28.706803	
40.978818,28.715384	
40.98939,28.717436	
40.982883,28.718141	
40.974487,28.72847	
41.036703,28.76596	
41.111333,28.768331	
41.03424,28.77197	
41.117742,28.772708	
41.054337,28.773355	
40.989602,28.777756	
41.04739,28.77837	
40.979266,28.779856	
41.065337,28.780409	
40.990265,28.78094	
40.993374,28.782763	
41.044663,28.783879	
41.043424,28.79051	
41.020506,28.791522	

Üniversite Veritabanı 25.txt - Not Defteri	
Dosya	Düzen
41.057462, 28.820425	Altınbaş Üniversitesi Mahmutbey, Dİlmenler Cd. No. 26 Bağcılar, İstanbul
41.042474, 29.009247	Bahçeşehir Üniversitesi Çırağan Caddesi Osmanpaşa Mektebi Sokak No: 4-6 3453 Beşiktaş
41.117575, 29.003741	Beykent Üniversitesi Ayazağa Mahallesi, Hadım Kuru Yolu Caddesi, No:19 Sarıyer/İSTANBUL
41.085028, 29.050936	Boğaziçi Üniversitesi Boğaziçi Üniversitesi 34342 Bebek/İstanbul Türkiye
41.046197, 29.019900	Galatasaray Üniversitesi Galatasaray Üniversitesi Çırağan Cad. No:36 34349 Ortaköy/İSTANBUL
41.056287, 28.950828	Haliç Üniversitesi Sütlüce Mahallesi, İmrahor Caddesi, No:11, Beyoğlu, İstanbul
41.055397, 28.500257	İstanbul Arel Üniversitesi -Türkoba Mah. Erguvan Sokak No: 26/K Tepekent-B.Çekmece
40.992238, 28.797837	İstanbul Aydın Üniversitesi Florya Halit Aydın Kampüsü Beşyol Mah. İnönü Cad. No: 38/8 Post
41.067305, 28.945449	İstanbul Bilgi Üniversitesi Eski Silahtarağa Elektrik Santrali Kazım Karabekir Cad
41.069329, 29.012314	İstanbul Bilim Üniversitesi Büyükdere Cad. No:120 Esentepe-Şişli İSTANBUL
40.998341, 28.698959	İstanbul Gelişim Üniversitesi Cihangir Mahallesi Şehit Jandarma Komando Er Hakan Ö
40.995333, 28.867355	İstanbul Kültür Üniversitesi Ataköy Yerleşkesi, 34156 Bakırköy / İSTANBUL
41.079226, 28.270118	İstanbul Rumeli Üniversitesi Yeni Mahalle Mah. Mehmet Silivri Cad. No: 38/8 Post
41.105567, 29.023021	İstanbul Teknik Üniversitesi İTÜ Ayazağa Yerleşkesi yeni Rektörlük Binası Kat:2 MA
41.041266, 28.989501	İstanbul Teknik Üniversitesi Harbiye Mahallesi, İTÜ Taşkışla Kampüsü Mimarlık Fakül
41.015658, 28.932926	İstanbul Üniversitesi Tıp Fakültesi Topkapı Mahallesi, Turgut Özal Millet Cd, 3409
41.005466, 28.940293	İstanbul Üniversitesi Cerrahpaşa Tıp Fakültesi Kampüsü Cerrah Paşa Mahallesi, Cerr
41.016437, 28.906749	İstanbul Yeni Yüzyıl Üniversitesi Topkapı Dr. Azmi Ofloğlu Yerleşkesi Maltepe Mah
41.014710, 28.905237	İstinye Üniversitesi Maltepe Mahallesi, 34010 Zeytinburnu/İstanbul
41.024739, 28.959062	Kadir Has Üniversitesi Cibali Mahallesi 34083 Fatih/İstanbul
41.212741, 29.087227	Koç Üniversitesi Mühendislik Fakültesi Rumelifeneri Mahallesi, Rumelifeneri Yolu,
41.108889, 29.008604	MEF Üniversitesi Huzur Mh., Maslak Ayazağa Cd. No:4, 34396 Sarıyer/İstanbul
41.029705, 28.988940	Mimar Sinan Güzel Sanatlar Üniversitesi Mimarlık Fakültesi Pürtelaş Hasan Efendi M
41.070346, 28.961813	Nişantaşı Üniversitesi Merkez Mahallesi, Hasbahçe Cd. No:88, 34406 Kağıthane/İstan
41.052082, 29.010615	Yıldız Teknik Üniversitesi Yıldız Mh., 34349 Beşiktaş/İstanbul

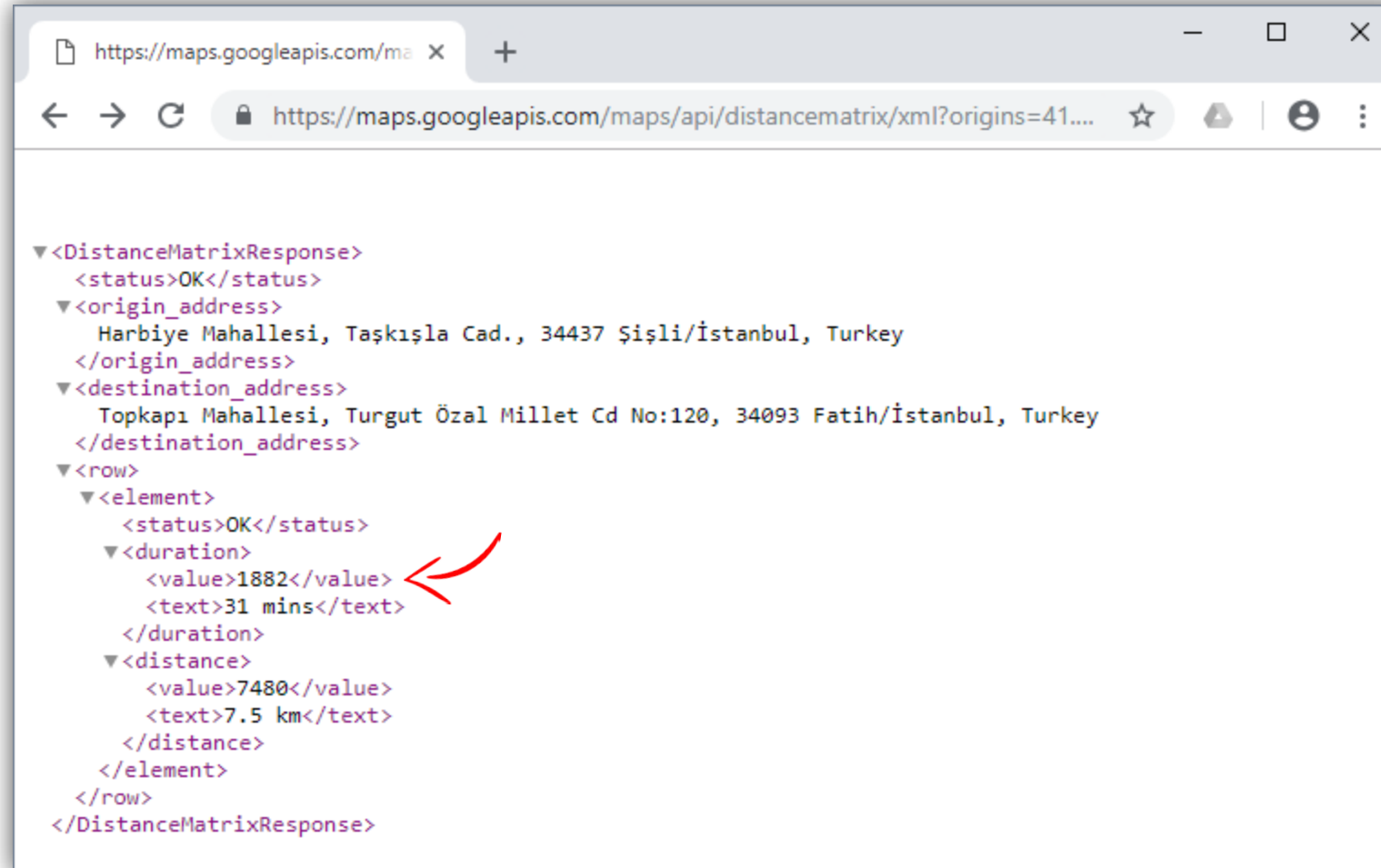
Figure 6. Home and university location databases .

Distance Matrix API

- ▶ In the second step, public transport travel times from homes to university campuses have been acquired from Distance Matrix API service.
- ▶ The Distance Matrix API is a service that provides **travel distance** and **time** for a matrix of origins and destinations [2].
- ▶ Distance Matrix API can be accessed through an HTTP interface, with requests constructed as a URL string, using **origins**, **destinations** and **optional parameters**, along with an **API key**.
- ▶ A Distance Matrix API request takes the following form:
 - ▶ `https://maps.googleapis.com/maps/api/distancematrix/outputFormat?parameters`

sample request and response (XML)

`https://maps.googleapis.com/maps/api/distancematrix/xml?origins=41.041266,28.989501&destinations=41.015658,28.932926
&units=metric&language=en-US&mode=transit&traffic_model=best_guess&key=YOUR_API_KEY`



```
<?xml version='1.0' encoding='UTF-8'>
<DistanceMatrixResponse>
  <status>OK</status>
  <origin_address>
    Harbiye Mahallesi, Taşkışla Cad., 34437 Şişli/İstanbul, Turkey
  </origin_address>
  <destination_address>
    Topkapı Mahallesi, Turgut Özal Millet Cd No:120, 34093 Fatih/İstanbul, Turkey
  </destination_address>
  <row>
    <element>
      <status>OK</status>
      <duration>
        <value>1882</value>
        <text>31 mins</text>
      </duration>
      <distance>
        <value>7480</value>
        <text>7.5 km</text>
      </distance>
    </element>
  </row>
</DistanceMatrixResponse>
```

Figure 7. Distance Matrix API service sample XML request and response [2]

2

constructing
a travel time
distance
matrix

parameters

PARAMETRE	VALUES
<i>outputFormat</i>	<i>json xml</i>
<i>origins</i>	<i>[latitude/longitude coordinates] [address]</i>
<i>destinations</i>	
<i>key</i>	<i>[YOUR_API_KEY]</i>
<i>mode</i>	<i>driving walking bicycling transit</i>
<i>transit_mode</i>	<i>bus subway train tram rail</i>
<i>transit_routing_preferences</i>	<i>less_walking fewer_transfer</i>
<i>traffic_model</i>	<i>best_guess pessimistic optimistic</i>
<i>departure_time</i>	<i>UTC time</i>
<i>arrival_time</i>	
<i>language</i>	<i>en tr ...</i>
<i>region</i>	
<i>avoid</i>	<i>tolls highways ferries indoor</i>
<i>units</i>	<i>metric imperial</i>

Table 2. Distance Matrix API service parameters [2]

2

constructing
a travel time
distance
matrix

```
Program.cs
11
12 static void Main(string[] args)
13 {
14
15     List<String> destinations = new List<String>();
16     destinations.Add("41.057462,28.820425"); // Altinbas
17     destinations.Add("41.042474,29.009247"); // Bahcesehir
18     destinations.Add("41.117575,29.003741"); // Beykent
19     destinations.Add("41.085028,29.050936"); // Bogazici
20     destinations.Add("41.045975,29.019902"); // Galatasaray
21     destinations.Add("41.056287,28.950828"); // Halic
22     destinations.Add("41.055397,28.500257"); // Arel
23     destinations.Add("40.992238,28.797837"); // Aydin
24     destinations.Add("41.067305,28.945449"); // Bilgi
25     destinations.Add("41.069329,29.012314"); // Bilim
26     destinations.Add("40.998341,28.698959"); // Gelisim
27     destinations.Add("40.995333,28.867355"); // Kultur
28     destinations.Add("41.079226,28.270118"); // Rumeli
29     destinations.Add("41.105567,29.023021"); // ITU Ayazaga
30     destinations.Add("41.041266,28.989501"); // ITU Taskisla
31     destinations.Add("41.015658,28.932926"); // Istanbul Capa
32     destinations.Add("41.005466,28.940293"); // Istanbul Cerrahpasa
33     destinations.Add("41.016437,28.906749"); // Yeni Yuzyil
34     destinations.Add("41.014710,28.905237"); // Istinye
35     destinations.Add("41.024739,28.959062"); // Kadir Has
36     destinations.Add("41.206130,29.075209"); // Koc
37     destinations.Add("41.108889,29.008604"); // MEF
38     destinations.Add("41.029705,28.988940"); // Mimar Sinan
39     destinations.Add("41.070346,28.961813"); // Nisantasi
40     destinations.Add("41.052082,29.010615"); // Yildiz Teknik
41
```

```
Program.cs
41
42 StringBuilder sb = new StringBuilder();
43 using (StreamReader sr = new StreamReader("origins_database.txt"))
44 {
45     String line = String.Empty;
46     while ((line = sr.ReadLine()) != null)
47     {
48         sb.AppendLine(line);
49         WebClient client = new WebClient();
50         client.QueryString.Add("key", "YOUR_API_KEY"); // TODO: &key=YOU
51         client.QueryString.Add("units", "metric");
52         client.QueryString.Add("language", "tr");
53         client.QueryString.Add("mode", "transit"); // transit_mode | tra
54         client.QueryString.Add("traffic_model", "best_guess"); // traffi
55         client.QueryString.Add("destinations", String.Join("|", destinat
56         client.QueryString.Add("origins", line);
57
58         Stream response = client.OpenRead("https://maps.googleapis.com/n
59         XmlDocument xmlDoc = new XmlDocument();
60         xmlDoc.Load(response);
61         XmlNodeList durations = xmlDoc.SelectNodes("//duration/value");
62
63         foreach (XmlNode duration in durations)
64             sb.Append(String.Format("{0} ", duration.InnerText));
65         sb.AppendLine();
66     }
67 }
68
69 using (StreamWriter sw = new StreamWriter("distance_matrix.txt", append:
70     sw.WriteLine(sb.ToString());
71
```

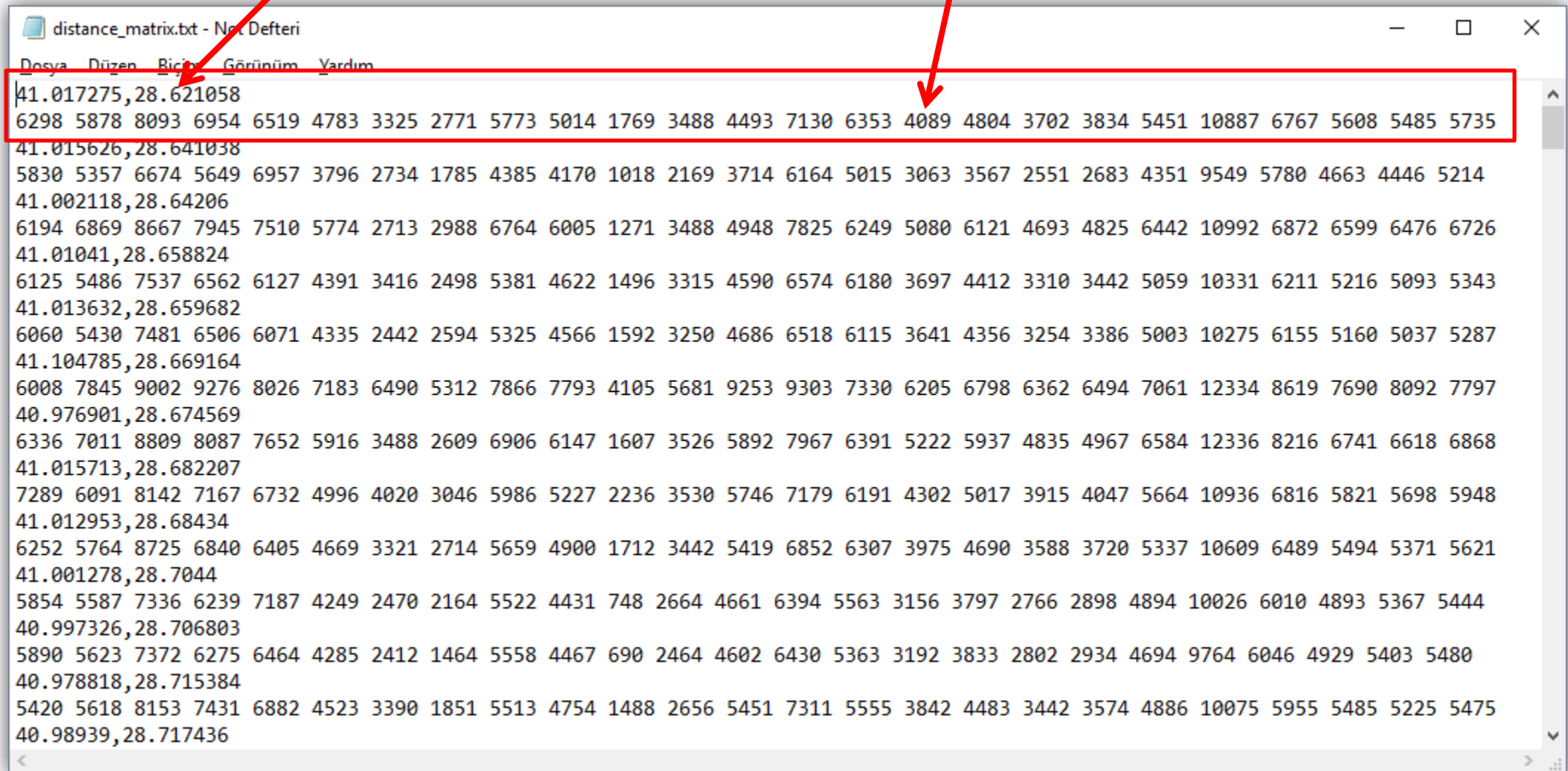
Figure 8. Distance matrix C# code, screenshots

2

constructing
a travel time
distance
matrix

home location
GPS coordinates

duration values to commute
university locations



41.017275,28.621058	6298	5878	8093	6954	6519	4783	3325	2771	5773	5014	1769	3488	4493	7130	6353	4089	4804	3702	3834	5451	10887	6767	5608	5485	5735
41.015626,28.641038	5830	5357	6674	5649	6957	3796	2734	1785	4385	4170	1018	2169	3714	6164	5015	3063	3567	2551	2683	4351	9549	5780	4663	4446	5214
41.002118,28.64206	6194	6869	8667	7945	7510	5774	2713	2988	6764	6005	1271	3488	4948	7825	6249	5080	6121	4693	4825	6442	10992	6872	6599	6476	6726
41.01041,28.658824	6125	5486	7537	6562	6127	4391	3416	2498	5381	4622	1496	3315	4590	6574	6180	3697	4412	3310	3442	5059	10331	6211	5216	5093	5343
41.013632,28.659682	6060	5430	7481	6506	6071	4335	2442	2594	5325	4566	1592	3250	4686	6518	6115	3641	4356	3254	3386	5003	10275	6155	5160	5037	5287
41.104785,28.669164	6008	7845	9002	9276	8026	7183	6490	5312	7866	7793	4105	5681	9253	9303	7330	6205	6798	6362	6494	7061	12334	8619	7690	8092	7797
40.976901,28.674569	6336	7011	8809	8087	7652	5916	3488	2609	6906	6147	1607	3526	5892	7967	6391	5222	5937	4835	4967	6584	12336	8216	6741	6618	6868
41.015713,28.682207	7289	6091	8142	7167	6732	4996	4020	3046	5986	5227	2236	3530	5746	7179	6191	4302	5017	3915	4047	5664	10936	6816	5821	5698	5948
41.012953,28.68434	6252	5764	8725	6840	6405	4669	3321	2714	5659	4900	1712	3442	5419	6852	6307	3975	4690	3588	3720	5337	10609	6489	5494	5371	5621
41.001278,28.7044	5854	5587	7336	6239	7187	4249	2470	2164	5522	4431	748	2664	4661	6394	5563	3156	3797	2766	2898	4894	10026	6010	4893	5367	5444
40.997326,28.706803	5890	5623	7372	6275	6464	4285	2412	1464	5558	4467	690	2464	4602	6430	5363	3192	3833	2802	2934	4694	9764	6046	4929	5403	5480
40.978818,28.715384	5420	5618	8153	7431	6882	4523	3390	1851	5513	4754	1488	2656	5451	7311	5555	3842	4483	3442	3574	4886	10075	5955	5485	5225	5475
40.98939,28.717436																									

Figure 9. Distance Matrix output

initial state distribution

- ▶ In the third step, the initial state distribution has been created in order **to simulate real life** situation.
- ▶ In order to make real and virtual data closer, it is also tried to make the gap between average commuting time of virtual data and average commuting time in real life closer.
- ▶ According to Istanbul city public transit index report released by Moovit public transport application,
 - ▶ the daily average amount of time that people spend commuting roundtrip with public transit on a weekday is **91 minutes** and
 - ▶ the daily average amount of time that people spend waiting at a stop or station on a weekday is **19 minutes**. [1]

tournament selection

- ▶ **Tournament selection** method has been preferred to create initial state distribution.
- ▶ Tournament selection is a method of selecting an individual from a population of individuals in a population-based search algorithm.
- ▶ In this method, tournament size (k) number of individuals are chosen from the population at random then the best among them is selected.
- ▶ **Selection pressure** can be controlled by the parameter of **tournament size**.

tournament selection



- ▶ tournament size (k) = 4
- ▶ 4 home locations are chosen randomly

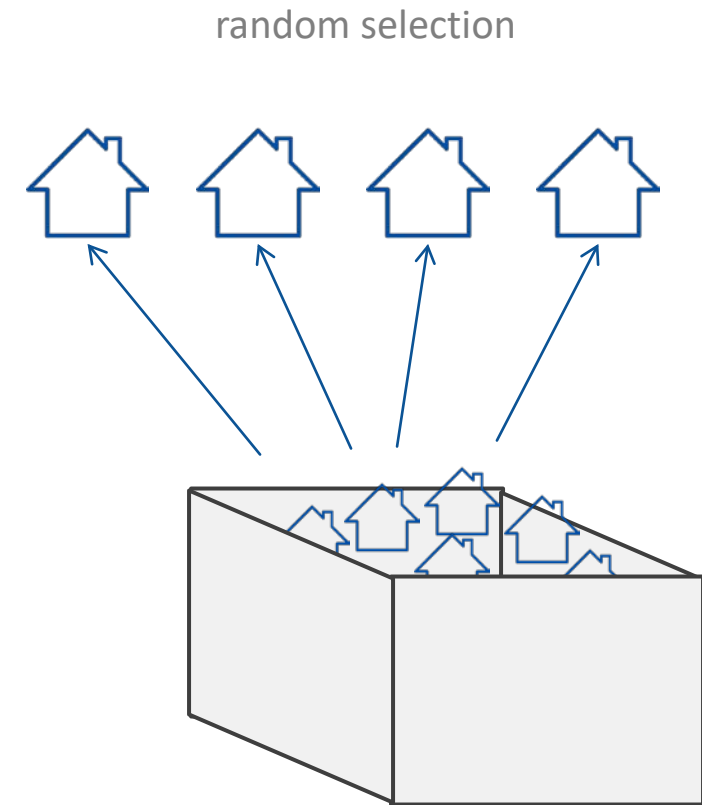


Figure 10a. Tournament selection

tournament selection

survival of the fittest



- ▶ the closest among them is selected and paired.

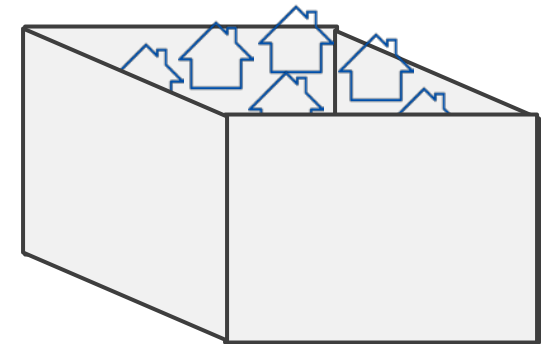


Figure 10b. Tournament selection

tournament selection

- ▶ This iteration is repeated until **each university** is paired with **6 homes**.
- ▶ **150 home** locations are selected and paired with **25 university** locations

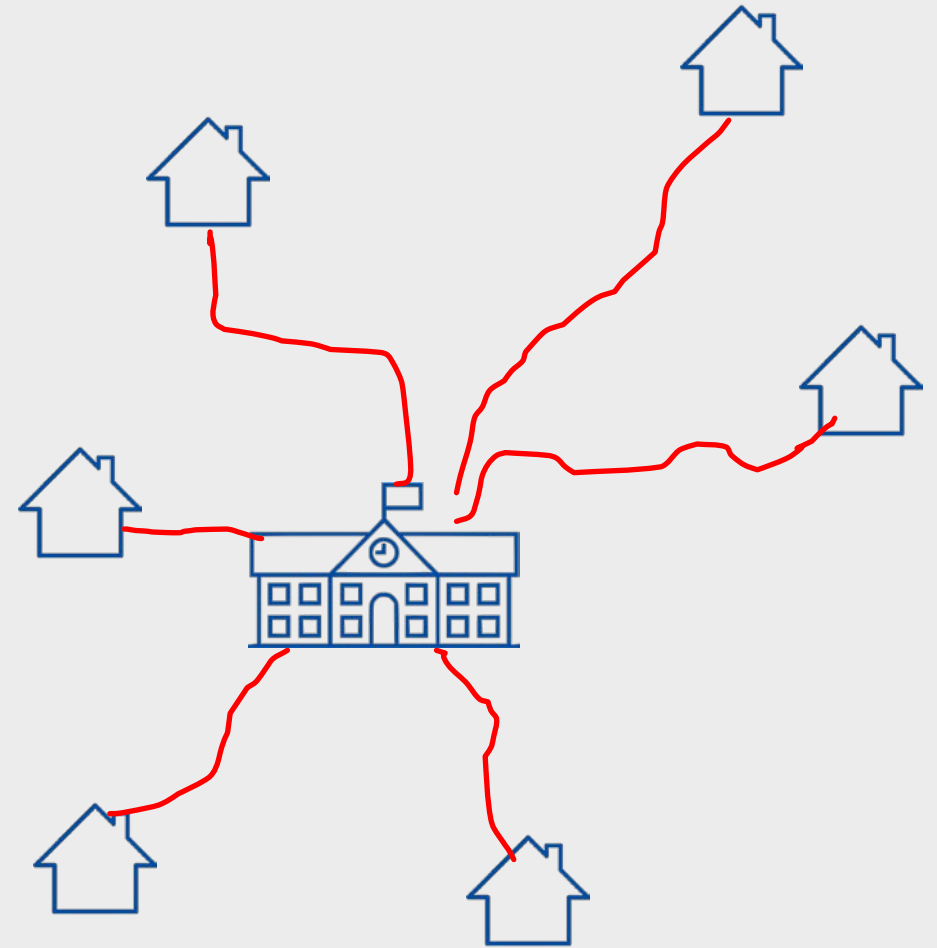


Figure 10c. Tournament selection

3

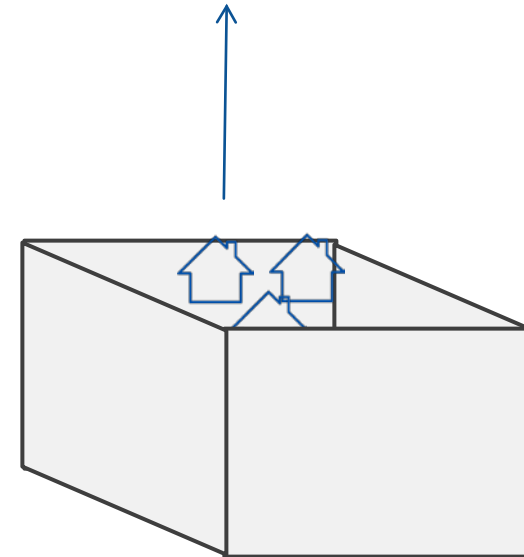
initial state
distribution

tournament selection

- ▶ Finally, **150 of 180** homes in home database are selected for initial state distribution.
- ▶ **30** homes are not selected.
- ▶ **Extreme values** are eliminated.
- ▶ Initial state distribution can simulate real life much closer.



150 home locations are selected for initial state distribution



30 home locations are not selected and eliminated

Figure 10d. Tournament selection

tournament selection

- ▶ tournament size parameter = **4**
- ▶ At the end, average roundtrip commuting time of initial state distribution is calculated as **88 minutes**.
- ▶ According to Istanbul city public transit index report released by Moovit public transport application,
 - ▶ the daily average amount of time that people spend commuting roundtrip with public transit on a weekday is **91 minutes**

3

initial state
distribution

tournament selection

3

initial state
distribution

```
117
118 // TOURNAMENT SELECTION
119 for (int college_index = 0; college_index < 25; college_index++)
120 {
121     for (int i = 0; i < 6; i++)
122     {
123         Agent currentBest = agents_loaded[rnd.Next(0, agents_loaded.Count)];
124
125         for (int k = 1; k < 4; k++) // Tournament Size K = 4
126         {
127             Agent agent = agents_loaded[rnd.Next(0, agents_loaded.Count)];
128             if (agent.Values[college_index] < currentBest.Values[college_index])
129                 currentBest = agent;
130         }
131
132         currentBest.Index = college_index;
133         agents_loaded.Remove(currentBest);
134         agents.Add(currentBest);
135     }
136 }
137
```

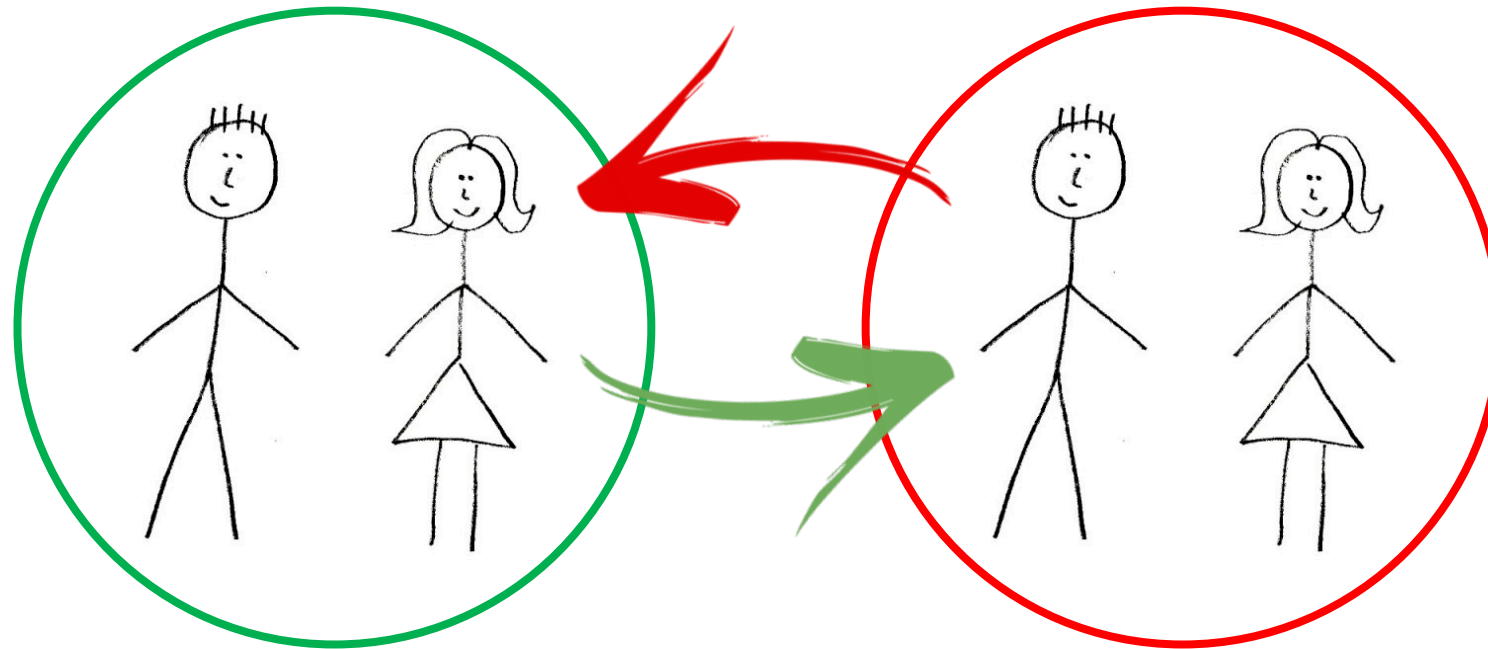
Line 136, Column 9 Spaces: 4 C#

Figure 11. Tournament selection C# code, screenshots

matching theory

- ▶ matching, allocation and exchange of discrete resources [3]
- ▶ In 1962 David Gale and Lloyd Shapley published one of the most influential papers in matching theory starting the literature in matching theory [3][4].
- ▶ This study introduces;
 - ▶ suitable solution concept called **stability** and
 - ▶ **two-sided matching** model
 - ▶ **deferred acceptance** algorithm

stability



unstable match

- ▶ In the stable matching problem, if there is a man and a woman who would **prefer to be matched** with each other **more than** their current matches

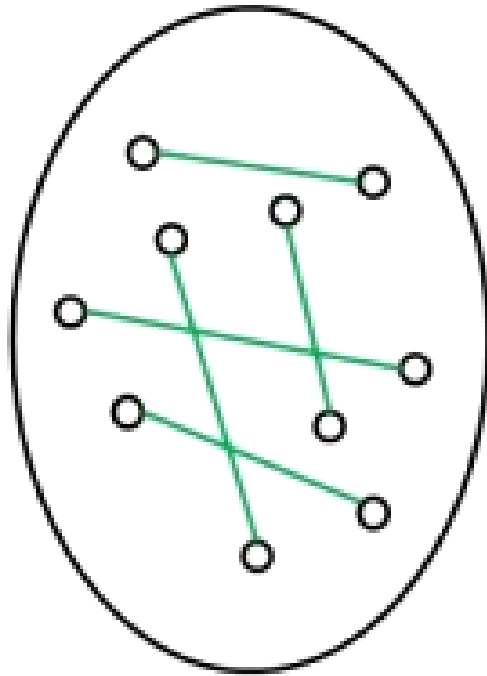
Figure 12. Stability, unstable match

one-sided and two-sided matching

- ▶ **two-sided matching** model
 - ▶ two sides, such as firms and workers, students and schools, or men and women, that need to be matched with each other.
 - ▶ **stable marriage** problem
- ▶ **one-sided matching** model
 - ▶ matching agents are in the same set
 - ▶ **stable roommates** and **housing market** problem

one-sided and two-sided matching

Irving's
Stable Roommates
Algorithm



Gale-Shapley's
Stable Marriage
Algorithm

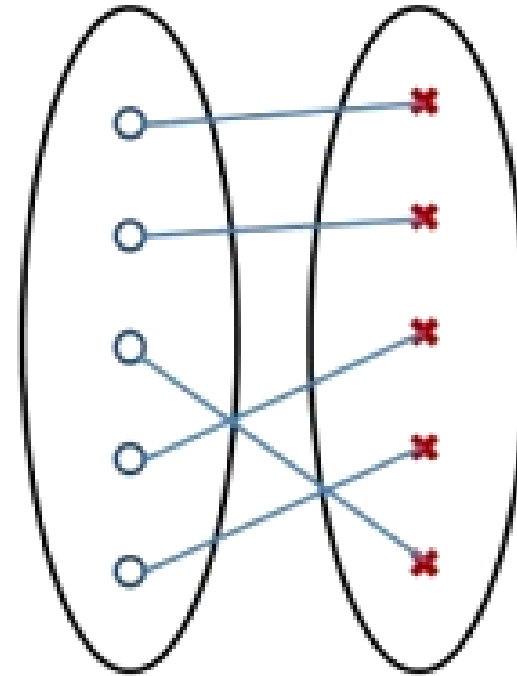


Figure 13. One-sided and two-sided matching [3]

stable marriage matching algorithm

- ▶ The Gale-Shapley Algorithm to compute the stable matching for two-sided markets, such as the **stable marriage** problem and **the college-admissions** problem
 - ▶ **two-sided** matching algorithm [4]
- ▶ To solve **home exchange** problem, **one-sided** matching algorithm is need.

4

home
exchange
matching

matching algorithms for **home exchange** problem

- ▶ Irving's Algorithm [5]
 - ▶ **stable roommates** problem
- ▶ Gale's the top trading cycle algorithm [6]
 - ▶ **housing market** problem
- ▶ Proposed Algorithm
 - ▶ **home exchange matching** problem

stable roommates matching algorithm

- ▶ Irving's Algorithm to compute the stable matching for one-sided matchings such as the **stable roommates** problem [5]
 - ▶ **one-sided** matching algorithm
 - ▶ **stability**
- ▶ each agent has a preference list of **all other agents** and **all agents** are matched
- ▶ In home-exchange problem, each agent has a preference list of **only the agents** such that **a match reduces travel times** for both sides.

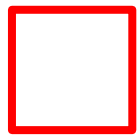
Stable Roommate

Stage 1

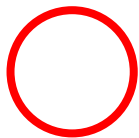
- ▶ Everybody proposes to their favorite. Order does not matter.
- ▶ Proposal recipients then pick their most best proposer and reject the rest.
- ▶ Those who got rejected keep proposing until accepted.
- ▶ If someone gets rejected by everyone else then no stable matching exists.

Stable Roommate

+ ← → -



makes a
proposal



accepts a
proposal



rejects

A	B	D	F	C	E
B	D	E	F	A	C
C	D	E	F	A	B
D	F	C	A	E	B
E	F	C	D	B	A
F	A	B	D	C	E

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

makes a proposal

accepts a proposal

rejects

+

←

→

-

A	B	D	F	C	E
B	D	E	F	A	C
C	D	E	F	A	B
D	F	C	A	E	B
E	F	C	D	B	A
F	A	B	D	C	E

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

makes a proposal

accepts a proposal

rejects

+

←

→

-

A	B	D	F	C	E
B	D	E	F	A	C
C	D	E	F	A	B
D	F	C	A	E	B
E	F	C	D	B	A
F	A	B	D	C	E

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

makes a proposal

accepts a proposal

×

rejects

+

←

→

-

A	B	D	F	C	E
B	D	E	F	A	C
C	D	E	F	A	B
D	F	C	A	E	B
E	F	C	D	B	A
F	A	B	D	C	E

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

+

←

→

-

A	<div>B</div>	D	F	C	E
B	<div>D</div>	E	F	<div>A</div>	C
C	<div>D</div>	E	F	A	B
D	F	<div>C</div>	A	E	<div>B</div>
E	F	C	D	B	A
F	A	B	D	C	E

makes a proposal

accepts a proposal

X

 rejects

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

makes a proposal

accepts a proposal

rejects

+

←

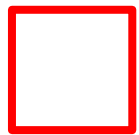
→

-

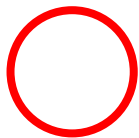
A	B	D	F	C	E
B		E	F	A	C
C	D	E	F	A	B
D	F	C	A	E	
E	F	C	D	B	A
F	A	B	D	C	E

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate



makes a
proposal



accepts a
proposal



rejects

4

home
exchange
matching



A	<div><div>B</div></div>	D	F	C	E
B		<div><div>E</div></div>	F	<div><div>A</div></div>	C
C	<div><div>D</div></div>	E	F	A	B
D	<div><div>F</div></div>	<div><div>C</div></div>	A	E	
E	F	C	D	<div><div>B</div></div>	A
F	A	B	<div><div>D</div></div>	C	E

Table 3. Stable Roommate Algorithm workflow process

A	B	D	F	C	E
B		E	F	A	C
C	D	E	F	A	B
D	F	C	A	E	
E	F	C	D	B	A
F	A	B	D	C	E

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

makes a
proposal

accepts a
proposal

rejects

+

←

→

-

A	<div>B</div>	D	F	C	E
B		<div>E</div>	F	<div>A</div>	C
C	<div>D</div>	E	F	A	B
D	<div>F</div>	<div>C</div>	A	E	
E	<div>F</div>	C	D	<div>B</div>	A
F	A	B	<div>D</div>	C	<div>E</div>

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

makes a
proposal

accepts a
proposal

rejects

+

←

→

-

A	B	D	F	C	E
B		E	F	A	C
C	D	E	F	A	B
D	F	C	A	E	
E		C	D	B	A
F	A	B	D	C	

Table 3. Stable Roommate Algorithm workflow process




	makes a proposal
	accepts a proposal
	rejects

Table 3. Stable Roommate Algorithm workflow process

A	B	D	F	C	E
B		E	F	A	C
C	D	E	F	A	B
D	F	C	A	E	
E		C	D	B	A
F	A	B	D	C	

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

Stage 2

- ▶ Everyone rejects those potential partners less desirable than their current accepted one.

4

Stable Roommate

makes a proposal

accepts a proposal

✗

rejects

+

←

→

-

A	B	D	F	C	E
B		E	F	A	C
C	D	E	F	A	B
D	F	C	A	E	
E		C	D	B	A
F	A	B	D	C	

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

+

←

→

-

A	B	D	F	C	E
B		E	F	A	C
C	D	E	F	A	B
D	F	C	A	E	
E		C	D	B	A
F	A	B	D	C	

makes a proposal

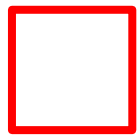
accepts a proposal

X

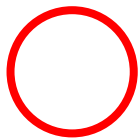
rejects

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate



makes a
proposal



accepts a
proposal



rejects



A	B	D	F		E
B		E	F	A	C
C	D	E	F		B
D	F	C	A	E	
E		C	D	B	A
F	A	B	D	C	

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

+

←

→

-

A	B	D	F		E
B		E	F	A	C
C	D	E	F		B
D	F	C	A	E	
E		C	D	B	A
F	A	B	D	C	

makes a proposal

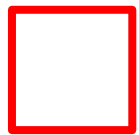
accepts a proposal

X

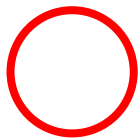
rejects

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate



makes a
proposal



accepts a
proposal



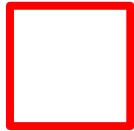
rejects




A	B	D	F		
B		E	F	A	C
C	D	E	F		B
D	F	C	A	E	
E		C	D	B	
F	A	B	D	C	

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

 makes a
proposal

 accepts a
proposal

 rejects

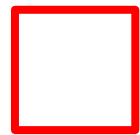
+

-

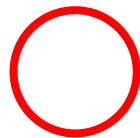
A	B	D	<div>F</div>	
B		E	F	<div>A</div> C
C	D	<div>E</div>	F	B
D	F	<div>C</div>	A	E
E		C	D	<div>B</div>
F	A	B	<div>D</div>	C

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate



makes a
proposal



accepts a
proposal



rejects



A	B	D	F	
B		E	F	A
C	D	E	F	
D	F	C	A	E
E		C	D	B
F	A	B	D	C

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

makes a proposal

accepts a proposal

×

rejects

+

←

→

-

A	B	D	F	
B		E	F	A
C	D	E	F	
D	F	C	A	E
E		C	D	B
F	A	B	D	C

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

makes a proposal

accepts a proposal

×

rejects

+

←

→

-

A	B	D	F	
B		E	F	A
C	D	E		
D	F	C	A	E
E		C	D	B
F	A	B	D	

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

+

←

→

-

A	B	D	F	
B		E	F	A
C	D	E		
D	F	C	A	E
E		C	D	B
F	A	B	D	

makes a proposal

accepts a proposal

X

rejects

Table 3. Stable Roommate Algorithm workflow process

A	B	F	
B		E	F
C	D	E	
D	F	C	E
E		C	D
F	A	B	D

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

+

←

→

-

A	B	(F)	
B		E	F (A)
C	D	(E)	
D	F	(C)	E
E		C	D (B)
F	A	B	(D)

□

makes a proposal

○

accepts a proposal

×

rejects

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

+

←

→

-

A	B	F	
B	E	F	A
C	D	E	
D	F	C	
E	C	B	
F	A	B	D

□

makes a proposal

○

accepts a proposal

×

rejects

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

Stage 3

- ▶ Find a participant who has more than one choice.
- ▶ Write their second preference X , then the last preference, Y of X .
- ▶ Repeat previous step until the starting player appears again.
- ▶ Every second preference and last preference then reject symmetrically.
- ▶ Do this until everybody has only one option.

Stable Roommate

A

+ ← → -

A has more than one choice

A	B	F	
B	E	F	A
C	D	E	
D	F	C	
E	C		B
F	A	B	D

Table 3. Stable Roommate Algorithm workflow process

4

home
exchange
matching

Stable Roommate

A

F

A has more than one choice

F is the second choice of A

+ ← → -

A	B	F	
B		E	F A
C	D	E	
D	F	C	
E		C	B
F	A	B	D

Table 3. Stable Roommate Algorithm workflow process

4

home
exchange
matching

Stable Roommate

A D

F

A has more than one choice

F is the second choice of A

D is the last choice of F

+ ← → -

A	B	F		
B	E		F	A
C	D	E		
D	F	C		
E	C		B	
F	A	B	D	

Table 3. Stable Roommate Algorithm workflow process

4

home
exchange
matching

Stable Roommate

A	D
F	C

A has more than one choice

F is the second choice of A

D is the last choice of F

C is the second choice of D

+ ← → -

A	B	F	
B	E	F	A
C	D	E	
D	F	C	
E	C		B
F	A	B	D

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

A D E

F C

A has more than one choice

F is the second choice of A

D is the last choice of F

C is the second choice of D

E is the last choice of C

+ ← → -

A	B	F		
B	E		F	A
C	D	E		
D	F	C		
E	C		B	
F	A	B	D	

Table 3. Stable Roommate Algorithm workflow process



4

home
exchange
matching

Stable Roommate

A	D	E
F	C	B

A has more than one choice
F is the second choice of A
D is the last choice of F
C is the second choice of D
E is the last choice of B
B is the second choice of E

+

←

→

-

A	B	F	
B	E	F	A
C	D	E	
D	F	C	
E	C	B	
F	A	B	D

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

A	D	E	A
F	C	B	

- A has more than one choice
- F is the second choice of A
- D is the last choice of F
- C is the second choice of D
- E is the last choice of C
- B is the second choice of E
- A is the last choice of B

+

←→

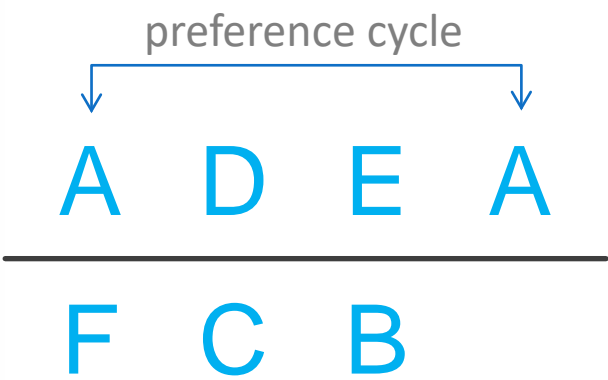
-

A	B	F	
B		E	F
C	D	E	
D	F	C	
E		C	B
F	A	B	D

Table 3. Stable Roommate Algorithm workflow process



Stable Roommate



+

←

→

-

A	B	F	
B	E	F	A
C	D	E	
D	F	C	
E	C	B	
F	A	B	D

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

A D E A
F C B

+ ← → -

A	B	F	
B	E	F	A
C	D	E	
D	F	C	
E	C		B
F	A	B	D

Table 3. Stable Roommate Algorithm workflow process

4

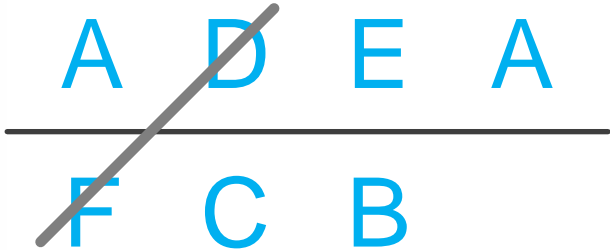
home
exchange
matching



4

home
exchange
matching

Stable Roommate



+

←

→

-

A	B	F	
B	E	F	A
C	D	E	
D	C		
E	C	B	
F	A	B	

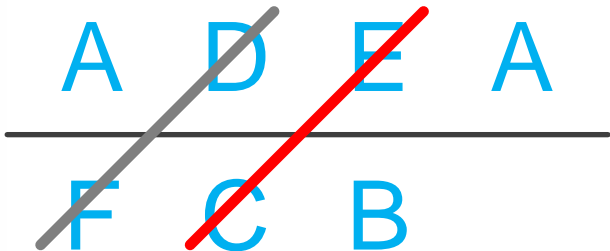
Table 3. Stable Roommate Algorithm workflow process



4

home
exchange
matching

Stable Roommate



+ ←————→ -

A	B	F	
B	E	F	A
C	D	E	
D	C		
E	C	B	
F	A	B	

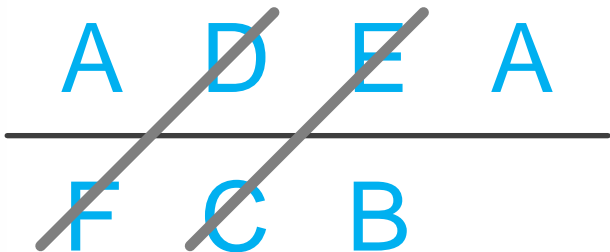
Table 3. Stable Roommate Algorithm workflow process



4

home
exchange
matching

Stable Roommate

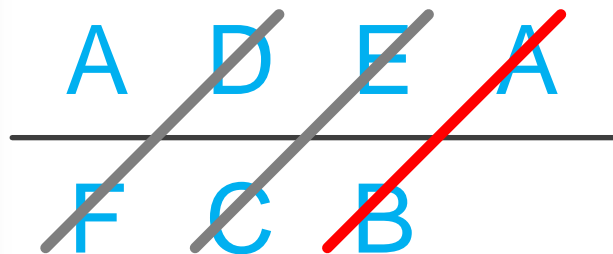


+ ← → -

A	B	F	
B	E	F	A
C	D		
D	C		
E		B	
F	A	B	

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate



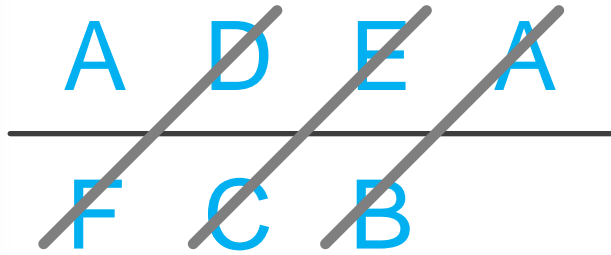
	+ ←-----→ -			
A	B		F	
B		E	F	A
C	D			
D		C		
E				B
F	A	B		

Table 3. Stable Roommate Algorithm workflow process

4

home
exchange
matching

Stable Roommate



+ ← → -

A		F
B	E	F
C	D	
D	C	
E		B
F	A	B

Table 3. Stable Roommate Algorithm workflow process

4

home
exchange
matching

Stable Roommate

B

B has more than one choice

+ ← → -

A	F
B	E F
C	D
D	C
E	B
F	A B

Table 3. Stable Roommate Algorithm workflow process

4

home
exchange
matching

Stable Roommate

B

F

B has more than one choice

F is the second choice of B

+ ← → -

A	F
B	E F
C	D
D	C
E	B
F	A B

Table 3. Stable Roommate Algorithm workflow process

4

home
exchange
matching

Stable Roommate

B B

F

B has more than one choice

F is the second choice of B

B is the last choice of F

+ ← → -

A	F
B	E F
C	D
D	C
E	B
F	A (B)

Table 3. Stable Roommate Algorithm workflow process

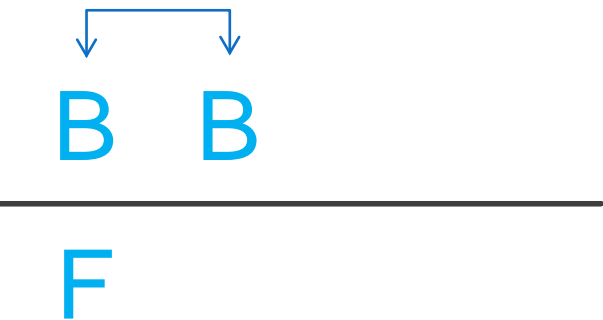


4

home
exchange
matching

Stable Roommate

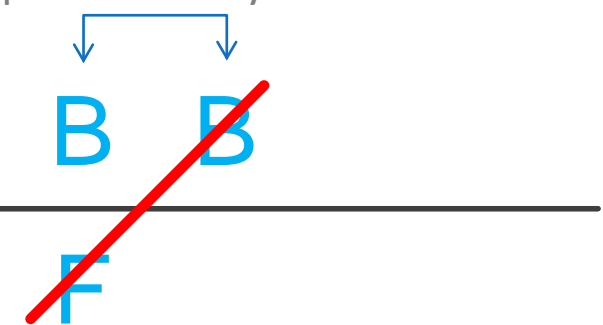
preference cycle



A	F
B	E F
C	D
D	C
E	B
F	A B

Table 3. Stable Roommate Algorithm workflow process

preference cycle



Stable Roommate

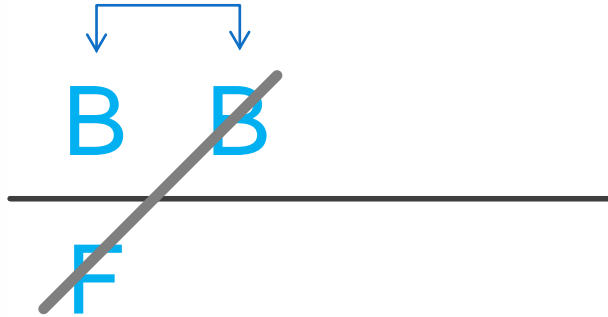
+ ←-----→ -

A	F	
B	E	F
C	D	
D	C	
E	B	
F	A	B

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

preference cycle



+ ← → -

A	F
B	E
C	D
D	C
E	B
F	A

Table 3. Stable Roommate Algorithm workflow process

4

home
exchange
matching



4

home
exchange
matching

Stable Roommate

A — F
B — E
C — D

+

-

A	F
B	E
C	D
D	C
E	B
F	A

Table 3. Stable Roommate Algorithm workflow process

Stable Roommate

A — F
B — E
C — D

+ ← → -

A	B	D	F	C	E
B	D	E	F	A	C
C	D	E	F	A	B
D	F	C	A	E	B
E	F	C	D	B	A
F	A	B	D	C	E

Table 3. Stable Roommate Algorithm workflow process

```

while there are unmatched agents do

    let a1 be first unmatched agent
    a1 proposes to its first preference a2 who has not rejected it previously

    if a2 has not received a proposal before then
        a2 accepts a1

    else
        if a2 prefers a1 over its current match a3 then
            a2 accepts a1
            reject symmetrically (a2, a3)
        else
            reject symmetrically (a1, a2)
        end if
    end if
end while

for all a2 holding proposal from a1 do
    reject symmetrically all (a2, a3) where a2 prefers a1 over a3
end for

for all cycles in (p1...pn+1) and (q1...qn) such that:
    qi is the second preference of pi and pi+1 is the last preference of qi do

    for i = 1 .. n do
        rejects symmetrically (q1, pi+1)
    end for
end for

```

Figure 14. Pseudocode of Stable Roommate Algorithm

housing market matching algorithm

- ▶ Gale's the top trading cycle algorithm for the indivisible goods trading such as **housing market** problem [6]
 - ▶ agents **own a house**
 - ▶ a housing market is an exchange market where agents have the option to trade their house in order to get **a better one**
 - ▶ they have preferences over **all houses including their own**
 - ▶ the agents are allowed to exchange the houses in an **exchange economy**
 - ▶ monetary transfers are not available

housing market matching algorithm

- ▶ Gale's the top trading cycle algorithm
 - ▶ searches for **core cycles** in each iteration
 - ▶ allows cycle matching
 - ▶ $a \rightarrow b$
 - ▶ $b \rightarrow c$
 - ▶ $c \rightarrow a$
- ▶ In home exchange problem, **mutual exchange mechanism** is needed
 - ▶ **cycle matching is not practical**

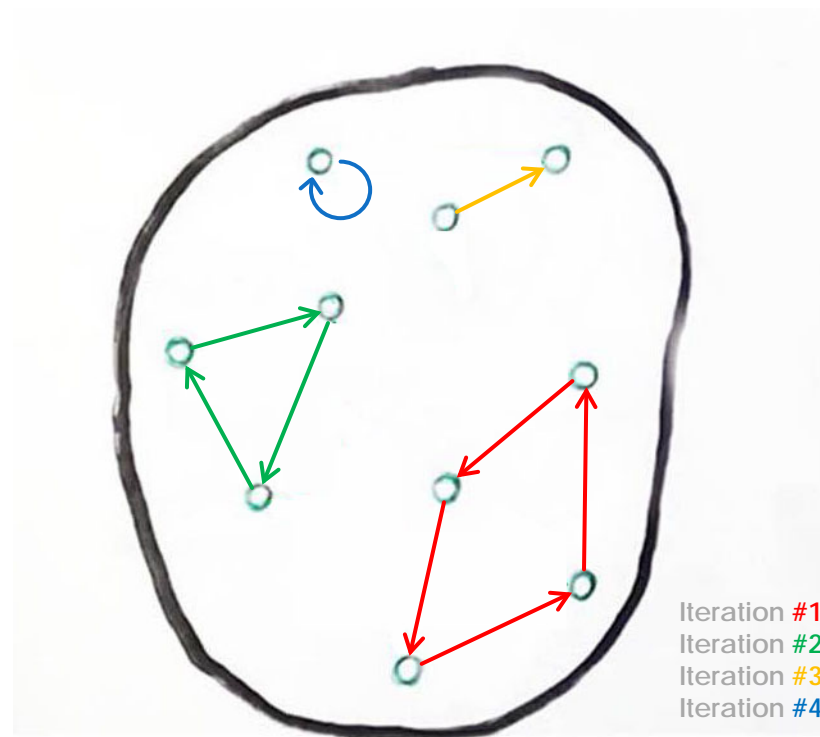
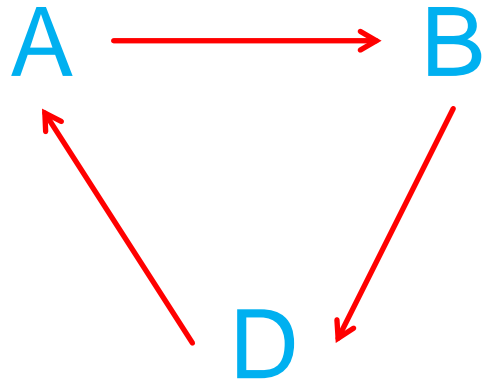


Figure 15. Top Trading Cycles (TTC)

Top Trading Cycles (TTC)

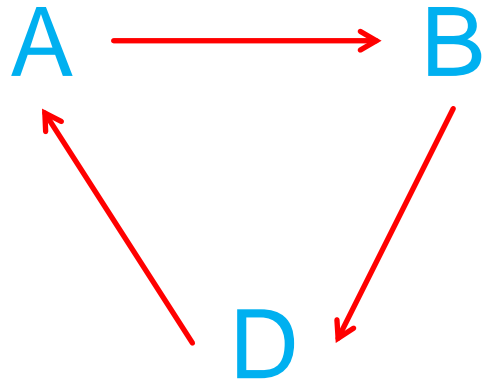


+ ← → -

A	B	D	F	C	E
B	D	E	F	A	C
C	D	E	F	A	B
D	A	C	F	E	B
E	F	C	D	B	A
F	A	B	D	C	E

Table 4. Top Trading Cycles (TTC) Algorithm workflow process

Top Trading Cycles (TTC)

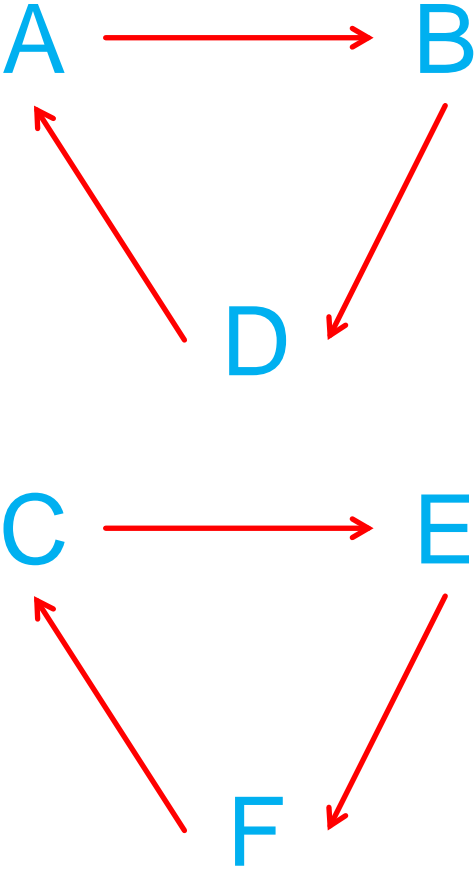


+ ← → -

C	E	F	
E	F	C	
F			C E

Table 4. Top Trading Cycles (TTC) Algorithm workflow process

Top Trading Cycles (TTC)

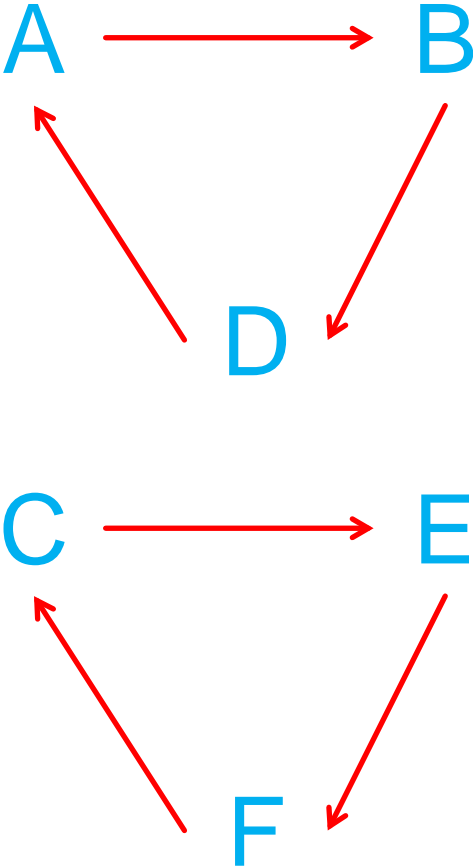


+ ←————→ -

C	E	F	
E	F	C	
F		C	E

Table 4. Top Trading Cycles (TTC) Algorithm workflow process

Top Trading Cycles (TTC)



+

←

→

-

Table 4. Top Trading Cycles (TTC) Algorithm workflow process

4

home
exchange
matching

```
while there are unmatched agents do

    let a1 be first unmatched agent
    empty cycle_pool

    loop
        if cycle_pool contains a1 then
            while a1 is not the first element of cycle_pool do
                remove the first element in cycle_pool
            end while
            break loop
        else
            add a1 to cycle_pool
            let a1 be the first agent in preference list of a1
        end if
    end loop

    foreach agent a1 in cycle_pool
        match a1 with its first_choice asymmetrically
    end for

    foreach agent in matchpool do
        remove matching agents and update preference list
    end for

end while
```

Figure 15. Pseudocode of Top Trading Cycles (TTC) Algorithm

preference-rank matching algorithm

- ▶ a problem-specific home exchange matching algorithm has been designed
- ▶ **agent-based** approach has been preferred to define and solve home exchange problem
 - ▶ each home location is considered as an agent
- ▶ each agent **has a preference list** of other agents for home exchange
 - ▶ preference list is **sorted by travel times** ascending order
- ▶ there is a **threshold level** to take an agent in preference list, which is assigned 10 minutes in this study.
 - ▶ a match must reduce travel times at least 10 minutes **for both agents**.

PREFERENCE_RANK

- ▶ This value is simply the answer of

“What is my index number in the preference list of the first agent in my preference list?” question

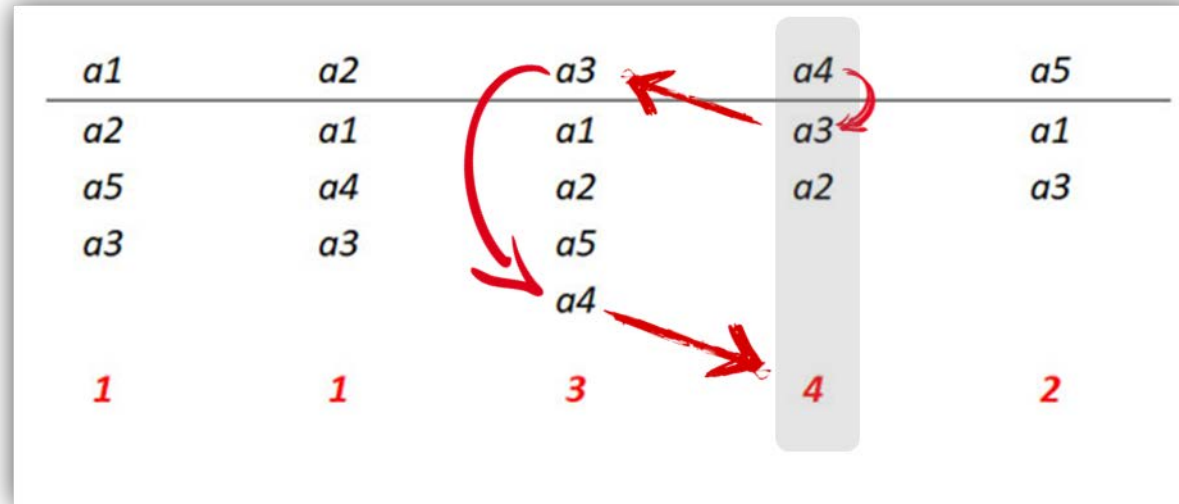


Figure 16. Preference Rank value for *a4*

home exchange matching algorithm

- ▶ the PREFERENCE_RANK value must be found for each agent
- ▶ the agent with **the smallest** PREFERENCE_RANK value is **paired with its first choice**
 - ▶ tie is broken by random selection
- ▶ When a match is found,
 - ▶ paired agents are removed from matching pool
 - ▶ other agents update their preference lists
 - ▶ the agents with empty preference list are also removed from matching pool
- ▶ the process is repeated until there is no agent in matching pool

Preference-Rank

(4)

	1	2	3	4	5
A	B	D	E	C	F
B	D	E	F	A	C
C	D	E	F	A	B
D	F	C	A	E	B
E	F	C	D	B	A
F	A	B	D	C	E

Table 5. Preference-Rank Algorithm workflow process

Preference-Rank

		1	2	3	4	5
(4)	A	B	D	E	C	F
(5)	B	D	E	F	A	C
	C	D	E	F	A	B
	D	F	C	A	E	B
	E	F	C	D	B	A
	F	A	B	D	C	E

Table 5. Preference-Rank Algorithm workflow process

Preference-Rank

		1	2	3	4	5
(4)	A	B	D	E	C	F
(5)	B	D	E	F	A	C
(2)	C	D	E	F	A	B
	D	F	C	A	E	B
	E	F	C	D	B	A
	F	A	B	D	C	E

Table 5. Preference-Rank Algorithm workflow process

Preference-Rank

		1	2	3	4	5
(4)	A	B	D	E	C	F
(5)	B	D	E	F	A	C
(2)	C	D	E	F	A	B
(3)	D	F	C	A	E	B
	E	F	C	D	B	A
	F	A	B	D	C	E

Table 5. Preference-Rank Algorithm workflow process

Preference-Rank

		1	2	3	4	5
(4)	A	B	D	E	C	F
(5)	B	D	E	F	A	C
(2)	C	D	E	F	A	B
(3)	D	F	C	A	E	B
(5)	E	F	C	D	B	A
	F	A	B	D	C	E

Table 5. Preference-Rank Algorithm workflow process

Preference-Rank

		1	2	3	4	5
(4)	A	B	D	E	C	F
(5)	B	D	E	F	A	C
(2)	C	D	E	F	A	B
(3)	D	F	C	A	E	B
(5)	E	F	C	D	B	A
(5)	F	A	B	D	C	E

Table 5. Preference-Rank Algorithm workflow process

Preference-Rank

		1	2	3	4	5
(4)	A	B	D	E	C	F
(5)	B	D	E	F	A	C
(2)	C	D	E	F	A	B
(3)	D	F	C	A	E	B
(5)	E	F	C	D	B	A
(5)	F	A	B	D	C	E

Table 5. Preference-Rank Algorithm workflow process

Preference-Rank

		1	2	3	4	5
(4)	A	B	D	E	C	F
(5)	B	D	E	F	A	C
(2)	C	D	E	F	A	B
(3)	D	F	C	A	E	B
(5)	E	F	C	D	B	A
(5)	F	A	B	D	C	E

Table 5. Preference-Rank Algorithm workflow process

C — D

Preference-Rank

	1	2	3	4	5
A	B	D	E	C	F
B	D	E	F	A	C
C	D	E	F	A	B
D	F	C	A	E	B
E	F	C	D	B	A
F	A	B	D	C	E

Table 5. Preference-Rank Algorithm workflow process



C — D

4

home
exchange
matching

Preference-Rank

	1	2	3	4	5
A	B		E		F
B		E	F	A	
E	F			B	A
F	A	B			E

Table 5. Preference-Rank Algorithm workflow process



C — D

4

home
exchange
matching

Preference-Rank

(3)

	1	2	3	4	5
A	B		E		F
B		E	F	A	
E	F			B	A
F	A	B			E

Table 5. Preference-Rank Algorithm workflow process



C — D

4

home
exchange
matching

Preference-Rank

		1	2	3	4	5
(3)	A	B		E		F
(2)	B		E	F	A	
	E	F			B	A
	F	A	B			E

Table 5. Preference-Rank Algorithm workflow process



C — D

4

home
exchange
matching

Preference-Rank

		1	2	3	4	5
(3)	A	B		E		F
(2)	B		E	F	A	
(3)	E	F			B	A
	F	A	B			E

Table 5. Preference-Rank Algorithm workflow process



C — D

4

home
exchange
matching

Preference-Rank

		1	2	3	4	5
(3)	A	B		E		F
(2)	B		E	F	A	
(3)	E	F			B	A
(3)	F	A	B			E

Table 5. Preference-Rank Algorithm workflow process



C — D

4

home
exchange
matching

Preference-Rank

		1	2	3	4	5
(3)	A	B		E		F
(2)	B		E	F	A	
(3)	E	F			B	A
(3)	F	A	B			E

Table 5. Preference-Rank Algorithm workflow process



C — D

4

home
exchange
matching

Preference-Rank

		1	2	3	4	5
(3)	A	B		E		F
(2)	B		E	F	A	
(3)	E	F			B	A
(3)	F	A	B			E

Table 5. Preference-Rank Algorithm workflow process



C — D

B — E

4

home
exchange
matching

Preference-Rank

	1	2	3	4	5
A	B		E		F
B		E	F	A	
E	F			B	A
F	A	B			E

Table 5. Preference-Rank Algorithm workflow process



C — D
B — E

4

home
exchange
matching

Preference-Rank

	1	2	3	4	5
A					F
F	A				

Table 5. Preference-Rank Algorithm workflow process

Preference-Rank

C — D
B — E

	1	2	3	4	5
A					F
F	A				

Table 5. Preference-Rank Algorithm workflow process

Preference-Rank

C — D
B — E
A — F

	1	2	3	4	5

Table 5. Preference-Rank Algorithm workflow process

4

home exchange matching

```
foreach a1 in agents do
  foreach a2 in agents do
    if a1 prefers a2 and a2 prefers a1
      add a2 in preference_list of a1
    end if
  end for
end for

while true
  foreach agent in match_pool do
    if preference_list of agent is empty
      remove agent from match_pool
    else
      find the preferred_value
    end if
  end for

  if there are no agents in match_pool
    break

  m1 = agent which has the smallest preferred_value
  m2 = first_choice of m1

  match m1 and m2

  remove m1 and m2 from match_pool

  foreach agent in match_pool do
    remove m1 and m2 in preference_list
  end for
end while
```

Figure 17. Pseudocode of Preference-Rank Algorithm

4

home
exchange
matching

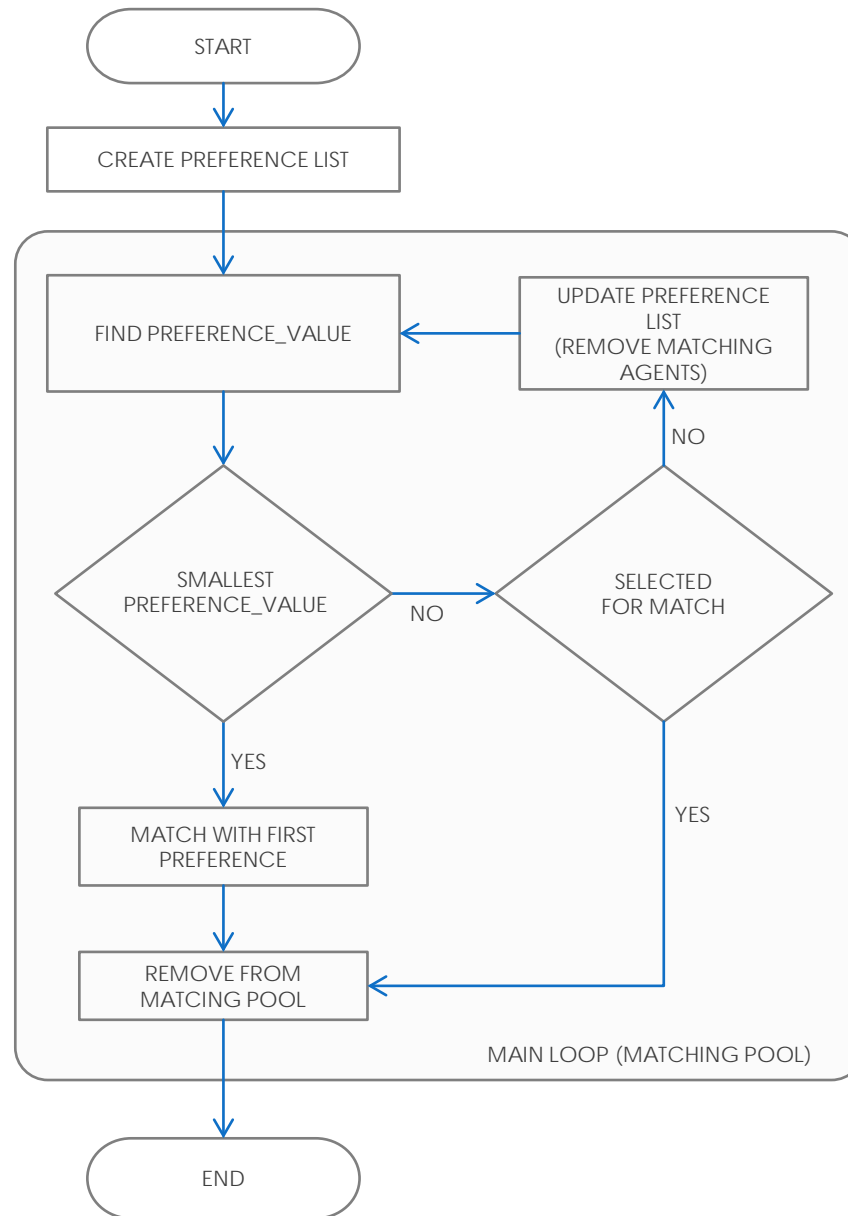


Figure 18. Flowchart of Preference-Rank Algorithm

results

```
67:[41.007699,28.907034] 3927 2082 1845 01:05:27 00:34:42 00:30:45
102:[41.046367,28.980021] 2347 1628 719 00:39:07 00:27:08 00:11:59

65:[41.049628,28.902819] 2429 1169 1260 00:40:29 00:19:29 00:21:00
139:[41.131613,29.028815] 2956 2075 881 00:49:16 00:34:35 00:14:41

58:[41.040409,28.881815] 4342 2818 1524 01:12:22 00:46:58 00:25:24
148:[41.074586,29.037992] 3235 2538 697 00:53:55 00:42:18 00:11:37

60:[40.998398,28.893576] 2999 1067 1932 00:49:59 00:17:47 00:32:12
104:[41.047918,28.982896] 2124 1413 711 00:35:24 00:23:33 00:11:51

93:[41.072382,28.952554] 2256 907 1349 00:37:36 00:15:07 00:22:29
87:[41.015240,28.948254] 2583 1351 1232 00:43:03 00:22:31 00:20:32

31 Matches Have Been Found.
Matching Ratio 41,3

Among Matching Agents (62)
Improvement 54,47
Average Travel Time Before Match 00:53:04
Average Travel Time After Match 00:24:10

In Whole System (150)
Improvement 26,41
Average Travel Time Before Match 00:44:00
Average Travel Time After Match 00:32:22
```

Figure 19. Screenshot of the program output.

results

agent-67
agent-102
GPS coordinates

before match

after match

difference

values in time
format

67: [41.007699, 28.907034]	3927	2082	1845	01:05:27	00:34:42	00:30:45
102: [41.046367, 28.980021]	2347	1628	719	00:39:07	00:27:08	00:11:59
65: [41.049628, 28.902819]	2429	1169	1260	00:40:29	00:19:29	00:21:00
139: [41.131613, 29.028815]	2956	2075	881	00:49:16	00:34:35	00:14:41
58: [41.040409, 28.881815]	4342	2818	1524	01:12:22	00:46:58	00:25:24
148: [41.074586, 29.037992]	3235	2538	697	00:53:55	00:42:18	00:11:37
60: [40.998398, 28.893576]	2999	1067	1932	00:49:59	00:17:47	00:32:12
104: [41.047918, 28.982896]	2124	1413	711	00:35:24	00:23:33	00:11:51
93: [41.072382, 28.952554]	2256	907	1349	00:37:36	00:15:07	00:22:29
87: [41.015240, 28.948254]	2583	1351	1232	00:43:03	00:22:31	00:20:32

31 Matches Have Been Found.
Matching Ratio 41,3

Among Matching Agents (62)

Improvement 54,47

Average Travel Time Before Match 00:53:04

Average Travel Time After Match 00:24:10

In Whole System (150)

Improvement 26,41

Average Travel Time Before Match 00:44:00

Average Travel Time After Match 00:32:22

Figure 19. Screenshot of the program output.

results

Matching Algorithm	Matching		Among Matching Agents			In Whole System		
			Commute times			Commute times		
	Agents	Ratio	Before Match (min)	After Match (min)	Improvements (%)	Before Match (min)	After Match (min)	Improvements (%)
Stable Roommates	63,28	42,19	53:12	27:52	47,65	44:39	33:58	23,88
Preference-Rank	63,29	42,19	53:09	27:50	47,65	44:39	33:58	23,87
Top Trading Cycles	62,99	42	53:14	27:32	48,26	44:39	33:52	24,10

Table 6: Matching algorithms results of 150 home and 25 university locations (average of 1000 successful runs)

4

home
exchange
matching

results

```
for (int k = 0; k < 7; k++)
{
    for (int i = 0; i < 180; i++)
    {
        List<int> generatedValues = new List<int>();

        for (int j = 0; j < 40; j++)
        {
            foreach (var realValue in realValues)
            {
                int t = realValue + random.Next(-300, 300);
                if (t < 300) t = 300;
                generatedValues.Add(t);
            }
        }
    }
}
```

Figure 20. C# programming language code used in virtual data generation process

results

			Among Matching Agents			In Whole System		
Matching			Commute times			Commute times		
Matching Algorithm	Agents	Ratio	Before Match (min)	After Match (min)	Improvements (%)	Before Match (min)	After Match (min)	Improvements (%)
Stable Roommates	513,38	51,34	50:08	24:20	51,46	43:15	30:00	30,61
Preference-Rank	518,88	51,89	49:57	24:15	51,45	43:15	29:54	30,83
Top Trading Cycles	505,25	50,53	50:18	23:16	53,73	43:15	29:35	31,56

Table 7: Matching algorithms results of 1000 home and 1000 university locations (average of 1000 successful runs)

4

home
exchange
matching

results

- ▶ **30,83%** improvement in whole system
51,45% improvement among only matching agents are observed
- ▶ Average one-way commute time **among matching agents** is reduced from **49 minutes 57 seconds** to **24 minutes 15 seconds**.
- ▶ Average one-way commute time **in whole system** is reduced from **43 minutes 15 seconds** to **29 minutes 54 seconds**.

4

home
exchange
matching

discussion

- ▶ All those three algorithms has proved more than **50 percent** improvement among matching agents and more than **30 percent** improvement in whole system.

discussion

- ▶ Home exchange model that is proposed in this study can also be applied on **tenants**.
 - ▶ Considering these improvement rates, in the case that the study is extended with tenants, significant improvement rates can be achieved for both matching agents and on whole system.
 - ▶ In this way, this model may contribute to reduce commuting times in large populated cities.
- ▶ There are some certain **limitations** about home exchange model.
 - ▶ in this model, only commute times and physical conditions are considered.
 - ▶ there may be custom preferences to choose a location, such as
 - ▶ being close to parents, families, friends or
 - ▶ school district etc.

Source Codes and Database Files

<https://github.com/yusufbuyruk/home-exchange>

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