CSEJ21 - Introduction to Alporthums

Honework 1

1) a)
$$\lim_{n\to\infty} \frac{\log^{2}(n^{2}+1)}{n} \xrightarrow{\text{lim}} \frac{2n}{n^{2}+1} \xrightarrow{\text{lim}} \frac{2n}{2n} = 0$$

10 $\log^{2}(n^{2}+1) \in O(n)$. True.

b)
$$\lim_{n\to\infty} \frac{\sqrt{n^2+n}}{n} = \lim_{n\to\infty} \sqrt{\frac{n^2+n}{n^2}} = \lim_{n\to\infty} \sqrt{1+\frac{1}{n}} = 1$$

c)
$$\lim_{n\to\infty} \frac{n^{n-1}}{n^n} = \lim_{n\to\infty} \frac{1 \cdot n \cdot n}{n \cdot n \cdot n} = \lim_{n\to\infty} \frac{1}{n} = 0$$

$$\lim_{N\to\infty}\frac{(2^{n}+n^{2})}{4^{n}}=\lim_{N\to\infty}\left(\frac{1}{2}\right)^{n}+\frac{n^{2}}{4^{n}}=\lim_{N\to\infty}\left(\frac{1}{2}\right)^{n}+\lim_{N\to\infty}\frac{n^{2}}{4^{n}}=0+0=0$$

e)
$$\lim_{n\to\infty} \frac{2 \log_2 n^2}{3 \log_2 n^2} = \lim_{n\to\infty} \frac{\frac{2}{5} \log_2 n}{6 \cdot \log_2 n} \xrightarrow{\text{like on } \atop \text{limon the } \atop \text{limon the } \atop \text{limon } \atop \text{l$$

H)
$$\lim_{n\to\infty} \frac{\log_2 \sqrt{n}}{(\lg_2 n)^2} = \lim_{n\to\infty} \frac{1}{\lg_2 n} = \lim_{n\to\infty} \frac{1}{2 \cdot \lg_2 n} = 0$$

$$lg_2^{r_1} \in O(lg_2^{r_1})^2$$
($lg_2^{r_1})^2 \not\in O(lg_2^{r_1})$) Statement is false.

10° > 2° > 0° = 8 len > 02 lgn > 02 > 50 > lgn

(Young Ca Kar 161044007

=) 10^-21

Let ax, bx if ax) bx, a>b.

=) 2ⁿ-n³

 $\lim_{n\to\infty} \frac{n^3}{2^n} = 0$ (from growth function of function $(x^2 < a^x)$) so $2^n > n^3$

=) 13-8 lgn

 $-f^{legn} = n^{legs} = n^{\gamma} \quad \text{so} \quad n^{\gamma} = s^{legn}$

=) glyn = n2lyn

gly = n?

lim at len len len len lim 1 = 0//

10 8 m > 12 lgn

=) $n^2 lgn - n^2$

 $\lim_{n\to\infty} \frac{n^2}{n^2 \log n} = \lim_{n\to\infty} \frac{1}{\log n} = 0/n$

12 lega > 12

=) n2 - VA

12- 11/2

fet xq-xb xqxb iff 016

20 V5 > 1V

=) 5n-lgpn

 $\lim_{n\to\infty}\frac{lgn}{\sqrt{n}}=)$ assume $n=x^2$

lm 2/9x = lm 2 = 0/1

80 Nu> Bau

- 3) a) In this function the bosic operation is composison operators. Since there is no nested loops or recursive calls in the function complexity only depends on loop. Loops iterates only size of through times. So complexity is $O(n) = \Omega(n) = \Omega(n)$
 - b) In this function, if we exomine the pattern of this loop, wherever even number assigned to i, count is increased in the next iteration. After that loops iterates one more time and calculates i=(i-1)*; statement and percents even: and repeated some pattern. So we assure this eas every elestatement it increases count. The growth of i is depends on else statement.

Since $i=i^2-i$ Statement increases i exponentially the complexity is $O(\log(\log n))$.

$$\int x^{2} \log x \, dx = \frac{x^{3} \log x}{9} - \int x^{2} \, dx = \frac{x^{3} \log x}{9} - \frac{x^{3}}{9} = \frac{x^{3} (3 \log x - 1)}{9} = \frac{1}{1} \text{ fett put this }$$

$$u = \log x \quad v = \frac{x^{3}}{9}$$

$$v' = \frac{1}{x} \quad v = \frac{x^{3}}{9}$$

$$\int \frac{(3 \log x - 1)}{9} \left[x \left[(3 \log x - 1) \right] \left[x \left[(3 \log x - 1) \right] \right] + \frac{1}{9}$$

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$$\int \frac{(3 \log x - 1)}{9} \left[x \left[(3 \log x - 1) \right] \left[(3 \log x - 1) \right] + \frac{1}{9}$$

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difer south.

$$\frac{n^{2}(3\ln - 1)}{g} - \frac{0.13\log 0 - 1}{g} \leq \int (k) \leq (n+1)^{2} (3\log (n+1) - 1) + \frac{1}{g}$$

$$\frac{\log 0}{g} \text{ is unique.}$$

For this post, Let's try this;

$$L + \int_{x^{2}} \sqrt{2g \times dx} = L + \left(\frac{x^{2}(\log x - 1)}{g} \right) = L + n^{2} \left(\frac{\log n - 1}{g} \right) + \frac{1}{g}$$

$$80 \quad \text{Statement becomes};$$

$$n^{2} \left(\frac{\log n - 1}{g} \right) + \frac{10}{g} \leq \int (k) \leq (n+1)^{2} \left(\frac{3\log (n+1) - 1}{g} \right) + \frac{1}{g}$$

$$80 \quad \int (k) \in \mathcal{D} \left(\frac{n^{2} \log n}{g} \right)$$

6)
$$\int_{0}^{\infty} f(x) dx \leq f(x) \leq \int_{0}^{\infty} f(x) dx$$

$$\frac{1}{x_{1}}\int_{1}^{1} \leq f(x) \leq \frac{1}{x_{1}}\int_{1}^{1+x_{1}} = \frac{1}{x_{1}}\int_{1}^{1+x_{2}} \leq f(x) \leq \frac{1}{(1+x_{1})}\int_{1}^{1+x_{2}} dx$$

c)
$$\int_{2}^{1} \frac{1}{2\sqrt{x}} dx \leq \int_{2}^{1} (x) \leq \int_{2}^{1} \frac{1}{2\sqrt{x}} dx$$

d)
$$\int_{-\frac{\pi}{2}}^{1} dx \leq \int_{-\frac{\pi}{2}}^{1} dx$$
 $\ln x \leq \int_{-\frac{\pi}{2}}^{1} dx \leq \int_{-\frac{\pi}{2}}^{1} dx$
 $\ln (n+1) \leq \int_{-\frac{\pi}{2}}^{1} dx \leq \int_{-\frac{\pi}{2}}^{1} dx$
 $\int_{-\frac{\pi}{2}}^{1} dx \leq \int_{-\frac{\pi}{2}}^{1} dx \leq \int_{-\frac{\pi}{2}}^{1} dx \leq \int_{-\frac{\pi}{2}}^{1} dx$
 $\int_{-\frac{\pi}{2}}^{1} dx \leq \int_{-\frac{\pi}{2}}^{1} dx \leq \int_{-\frac{\pi}$

$$1 + \int \frac{1}{x} dx \ge f(k)$$

$$1 + \ln x \int \ge g(x)$$

5) Best case: first element is searching element.

Worst case: Element does not in the lists or LED= \times (last element) $W(n) \in O(n) \text{ which } n \text{ is legath of list.}$

Yusuf Can Kan 161044007