

# Manual of plotastrodata

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## 1 Read Data

The data class `AstroData` can take a fits file.

```
from plotastrodata.analysis_utils import AstroData  
  
d = AstroData(fitsimage='file_name.fits')
```

`AstroData` can take more arguments, such as `Tb` and `sigma`. `Tb=True` means the data values will be converted from flux densities in the unit of  $\text{Jy beam}^{-1}$  to brightness temperatures in the unit of K. `sigma` specifies how to measure the noise level of the data values: for example, the default option of 'hist' means to use the histogram of the data values. The argument of `pvpa` is the position angle of the PV cut direction in the unit of degree, which will be used to calculate the spatial resolution of the PV diagram.

The data class `AstroFrame` is necessary to form the `AstroData` instance in a useful format. `AstroFrame` can take quantities related to coordinate ranges.

```
from plotastrodata.analysis_utils import AstroFrame  
  
f = AstroFrame(vmin=-5.0, vmax=5.0, vsys=2.0,  
               center='00h00m00s 00d00m00s', rmax=3.0)
```

`vmin`, `vmax`, and `vsys` are in the unit of  $\text{km s}^{-1}$ . `rmax` is in the unit of arcsec. Instead of `rmax`, other arguments (`xmin`, `xmax`, `ymin`, `ymax`, `xoff`, `yoff`) can be used to adjust the x and y ranges in more detail. When an argument of `fitsimage` is given, the central coordinates `center` is read from the given fits file; the rest frequency is also read from the fits file, which is used for the frequency-velocity conversion. Moreover, an argument of `dist` can specify the distance used to change the unit of spatial coordinates from arcsec to au. An argument of `swapxy` is used to swap the x and y coordinates. An argument of `pv` must be `True` when the `AstroData` instance to be read is a position-velocity (PV) diagram, i.e., the first and second axes are the spatial and velocity coordinates. When `quadrants=True`, the first and third (or second and fourth) quadrants of the PV diagram will be averaged. `xflip` and `yflip` will be used to determine the plotting direction of the x and y axes, respectively; these have a meaning only when a figure is made from the data set.

Forming the `AstroData` instance needs the following command.

```
f.read(d)
```

After this command, the `AstroData` instance has useful attributes in the format of numpy array: a 1D array of `d.x` (as well as `d.y` and `d.v`), a 2D or 3D array of `d.data`, a 1D array of `d.beam`, and a float of `d.sigma`. `d.x` and `d.y` are the relative coordinates in the unit of arcsec from the

given **center**. Similarly, **d.v** is the relative coordinate in the unit of  $\text{km s}^{-1}$  from the given **vsys**. **d.beam** is the beam components `array([bmaj, bmin, bpa])`, where **bmaj** and **bmin** are in the unit of arcsec, while **bpa** is in the unit of degree. When **Tb=True** above, the data values are converted to the brightness temperature and stored as **d.data**. **d.sigma** is the noise level measured in the way specified above in the same unit as **d.data**. AstroData can take two more arguments, **restfreq** and **cfactor**. **restfreq** is used to explicitly set the rest frequency in the unit of Hz, which is used to convert frequency to velocity and  $\text{Jy beam}^{-1}$  to K. When this argument is zero (**restfreq=0**), the frequency axis is not converted to velocity. When the unit of the frequency/velocity axis in the input fits header is m/s, **f.read(d)** divides the coordinate by 1000. The argument **cfactor** specifies a constant factor that **d.data** is multiplied by. This will be useful when one wants to change the intensity unit from  $\text{Jy beam}^{-1}$  to  $\text{mJy beam}^{-1}$ .

In addition to the input attributes, **f.read(d)** adds three attributes to the AstroData instance **d**: **fitsimage\_org**, **sigma\_org**, and **fitsheader**. **fitsimage\_org** saves the input **fitsimage**, while **fitsimage** is updated to None after **f.read(d)**. Similarly, **sigma\_org** saves the input **sigma**, which may be a string, while **sigma** is updated to the calculated value. **fitsheader** is the fits header in the format of `astropy.io.fits.open(fitsimage)[0]`.

When **pv=True** in **AstroFrame**, the **read** method changes the **beam** attribute of the AstroData instance. The first element will be the velocity resolution. The second element of **beam** will be  $1/\sqrt{\cos^2(\text{bpa} - \text{pvpa})/\text{bmaj}^2 + \sin^2(\text{bpa} - \text{pvpa})/\text{bmin}^2}$ . This is calculated from the intersection of the beam ellipse and the PV cut line. The third element will be 0; thus, the velocity resolution (first element) is regarded as the vertical length by default when this “beam” is plotted in a PV diagram. The original beam will be stored in **beam\_org**.

## 2 Analyze Data

AstroData also has handy methods to analyze the 2D/3D data.

The **binning** method rebins the 2D/3D data with a given width for each coordinate.

```
d.binning(width=[5, 4, 2])
```

This command takes an average over 5 channels in the velocity direction, 4 pixels in the y direction, and 2 pixels in the x direction. The number of channels and pixels are decreased accordingly after this method. If the length of **width** is 2, the two values are regarded as the widths for the y and x directions.

The **centering** method sets the coordinates so that the spatial center and the systemic velocity have the exact zero coordinates by interpolation.

```
d.centering(includexy=True, includev=False)
```

This command adjusts the x and y coordinates but does not adjust the velocity coordinate. This method will be useful when one wants to quickly get a radial profile along a line passing the center or a PV diagram (using the **rotate** method together).

The **circularbeam** method makes the beam shape circular by additional 2D Gaussian convolution. This method takes no argument.

```
d.circularbeam()
```

The new beam has the major and minor axes same as the old major axis. This method also updates the attribute of `d.beam` accordingly.

The `deproject` method deprojects the 2D/3D data with a given position angle (P.A.) and inclination angle.

```
d.deproject(pa=45, incl=45)
```

`pa` is the position angle from the north to the east in the unit of degree. `incl` is the inclination angle; `incl=0` means the face-on configuration and thus no deprojection. This command replaces `d.data` and `d.beam` with the deprojected data and the deprojected beam, respectively.

The `fit2d` method performs MCMC fitting to the 2D image of `d.data` or `d.data[chan]`, where `chan` is the channel number, by using `emcee` or `ptemcee` through the class of `plotastrodata.fitting_utils.EmceeCorner`.

```
res = d.fit2d(chan=12, model=model, bounds=bounds,
             kwargs_fit={'nwalkersperdim': 2, 'nsteps': 1000, 'nburnin': 500},
             kwargs_plotcorner={'savefig': 'corner.png'})
```

`model` is a function with the shape of `model(par, x, y)`, where `par` is the list of parameters. `bounds` is the 2D list of the parameter boundary in the shape of `[[p0,min, p1,min, ...], [p0,max, p1,max, ...]]`. `kwargs_fit` and `kwargs_plotcorner` are the arguments for the methods of `EmceeCorner.fit` and `EmceeCorner.plotcorner`, respectively. `nsteps` includes the number the burn-in steps. The output `res` is a dictionary consisting of `popt`, `plow`, `pmid`, `phigh`, `model`, and `residual`. The first four keys provide the best, lower percentile, 50 percentile, and higher percentile parameters. The last two keys provide the model and residual 2D images.

The `histogram` method returns the bins and the histogram in the bins of the attribute of `d.data` by using `numpy.histogram()`.

```
hbin, hist = d.histogram(bins=10)
```

The arguments are the same as those for `numpy.histogram()`. The bins (`hbin`) have the same length as the histogram (`hist`), which is different from the original `numpy.histogram`.

The `gaussfit2d` method performs the 2D Gaussian fitting to the 2D image of `d.data` or `d.data[chan]`, where `chan` is the channel number, by using `scipy.optimize.curve_fit`.

```
res = d.gaussfit2d(chan=12)
```

This command performs the fitting to the channel of 12 in `d.data`. For 2D data, the `chan` argument can be omitted. The output (`res` here) is a dictionary having keys of `popt`, `pcov`, `model`, and `residual`. `popt` and `pcov` are the optimized parameters (peak intensity, central x, central y, major FWHM, minor FWHM, and P.A.) and their covariance. The `model` and `residual` are 2D arrays with the same shape of the fitted 2D array.

The `mask` method puts `numpy.nan` on pixels that satisfies a given condition.

```
d.mask(dataformask=d2.data, includepix=[1e-3, 100], excludepix=[50, 200])
```

This command puts `numpy.nan` on pixels of `d.data` where `d2.data` is outside `[1e-3, 100]` or inside `[50, 200]`, where `d2` is an `AstroData` instance different from `d`. This method will be useful when one wants to put a mask on a moment 1 map using the values of a moment 0 map.

The `profile` method makes line profiles at given spatial positions.

```
v, f, g = d.profile(xlist=[-0.5, 0.2], ylist=[1, 0.8], ellipse=[0.3, 0.2, 45])
```

This command makes line profiles at (x,y)=(-0.5, 1) and (0.2, 0.8) in the unit of arcsec. The intensity of each profile is an average over a boxcar ellipse with the major axis of 0.3 arcsec, the minor axis of 0.2 arcsec, and the P.A. of 45 degrees. Instead of `xlist` and `ylist`, coordinate strings can be input using an argument of `coords`: `coords=['00h00m00.0s 00d00m00.0s', '11h11m11.1s 11d11m11.1s']`. When `ellipse` is omitted, the profile is made by picking up the values at the closest pixel to the given position. When the ellipse size is not so large compared to the pixel size, the integer argument `ninterp` may be useful; this makes the pixel size `ninterp` times finer by interpolation. When the boolean argument `flux` is True, the output profile has the unit of Jy. Additionally, when the boolean argument `gaussfit` is True, the profiles will be fitted with a 1D Gaussian function. The output `v` above is `d.v`. The output `f` above is a list of 1D-array profiles, i.e., 2D array. The output `g` is a list of dictionaries; each dictionary has keys of `best` and `error` (square root of the diagonal components of the covariance).

The `rotate` method rotates the attribute `d.data` by the given angle in the unit of degree by interpolation.

```
d.rotate(pa=45)
```

When a pixel refers to a position outside the original image, this pixel has `numpy.nan` after this method.

The `slice` method makes a radial profile for a 2D image or a PV diagram for a 3D image along a given direction and length by interpolation.

```
r, f = d.slice(length=3, pa=45, dx=0.2)
```

This commands makes a radial profile (or PV diagram) along a cut with a length of 3 arcsec at P.A.=45 degrees with a separation of 0.2 arcsec. The output `r` and `f` are both 1D arrays of the positional offsets and the intensity at the positions. When the separation `dx` is omitted, the absolute value of the x pixel size is adopted.

The `todict` method returns the attributes as a dictionary.

```
a = d.todict()
```

This output includes keys of `data`, `x`, `y`, `v`, `fitsimage`, `beam`, `Tb`, `restfreq`, `cfactor`, `sigma`, and `center`. This dictionary can be input to methods of `PlotAstroData` as `**a`.

The `writetofits` method exports the instance as a fits file.

```
d.writetofits(fitsimage='new_file_name.fits')
```

The output fits file reuses the header components of the fits file used to make the `AstroData` instance ('`file_name.fits`' above); some header components are automatically updated after the above-mentioned methods for analysis, such as `CDEL1`.

### 3 Plot Data

The class `PlotAstroData` can take an `AstroData` instance through the method of `d.todict()`.

```
from plotastrodata.plot_utils import PlotAstroData

p = PlotAstroData(rmax=3.0)
p.add_color(**d.todict())
p.add_scalebar(length=50 / 140, label='50 au')
p.set_axis()
p.savefig('figure_name.png')
```

These commands make a color map using the `AstroData` instance `d`. `PlotAstroData` can take the same arguments as `AstroFrame` to define the plotting ranges; particularly `rmax` (also, `vmin` and `vmax` for a cube or a PV diagram) is necessary. The method `p.add_color()` can take a fits file directly instead of the `AstroData` instance, as `p.add_color(fitsimage='file_name.fits')`. This method can actually take the same arguments as `AstroData` to specify the data to be plotted as a color map; `**d.todict()` does this indirectly. The command `p.add_scalebar()` can be omitted if the map does not need to show a scale bar. The command `p.set_axis()` (or `p.set_axis_radec()`) is necessary even without any argument.

The class `PlotAstroData` can take more arguments. `veldigit` specifies the number of digits of the velocity label on the channel maps. `channelnumber` specifies which channel is used to make a 2D image; when this is `None` (default), channel maps are made instead of a 2D image. `nrows` and `ncols` specify the grid shape of the channel maps. `fontsize` specifies the basic font size in the figure. `nancolor` specifies which color is used when the value is `nan`. `dpi` specifies the resolution of a raster image file. `figsize` is the same as the argument for `Figure.figure` of `matplotlib`. `fig` and `ax` can be used to input external `Figure` and `Axes` objects. More detailed usage can be found in the `example.py` file and <https://plotastrodata.readthedocs.io/en/latest/#>. The following is the explanation of each method of `PlotAstroData`.

#### 3.1 Maps

The `add_color` method plots the given data in the format of a color map.

```
p.add_color(**d.todict(), stretch='log', show_cbar=True, cblabel=r'mJy beam$^{-1}$',
            cbticks=[0.01, 0.03, 0.1, 0.3], cbticklabels=['10', '30', '100', '300'],
            cblocation='right')
```

The `stretch` argument can be 'linear', 'log', 'asinh', or 'power'. The Arcsinh hyperbolic stretch can be adjusted by another argument of `stretchscale` as `asinh(data / stretchscale)`. The power-law stretch can be adjusted by another argument of `stretchpower` as `((data / vmin)^(1 - stretchpower) - 1) / (1 - stretchpower) / ln(10)`, where `vmin` is a given minimum value. The arguments starting with 'cb' adjust the colorbar. In addition, two arguments, `xskip` and `yskip`, can be used to skip spatial pixels in this method as well as `add_contour`, `add_segment`, and `add_rgb`. Similarly, `show_beam`, `beamcolor`, and `beampos` can be used in these four methods to adjust beam color and position, as well as switch whether to show the beam.

The `add_contour` method plots the given data in the format of a contour map.

```
p.add_contour(**d.todict(), levels=[-3, 3, 6, 9])
```

The `levels` argument specifies the contour levels in the unit of `d.sigma`.

The `add_rgb` method plots the given data in the format of three-color maps. The input three data sets are mixed as Red, Green, and Blue.

```
p.add_rgb(**d.to_dict(), stretch=['linear', 'log', 'linear'])
```

For this method, the input is a combination of three data sets, and thus `d.data` here must be a 1D list (not a numpy array) of three 2D/3D numpy arrays. In the same way as `add_color`, `stretchscale` and `stretchpower` are available in this method.

The `add_segment` method plots the given data in the format of a segment map, as is often used for polarization maps.

```
p.add_segment(Qfits='Qfile_name.fits', Ufits='Ufits_name.fits',
              ampfactor=3.8, angonly=False, rotation=90, cutoff=3.0)
```

The input format of the data is different from that for `add_color` and `add_contour`. One of the following pairs must be given: (`ampfits`, `angfits`), (`Qfits`, `Ufits`), (`amp`, `ang`), or (`stQ`, `stU`). The latter two pairs are supposed to be in the numpy.array format. The `ampfactor` argument can be used to adjust the segment length. When `angonly=True`, the segment length is set to be uniform. The `rotation` can be used to rotate the segments in the unit of degree. The `cutoff` argument specifies the intensity threshold to calculate the amplitude and angle from the Stokes Q and U intensities.

### 3.2 Patches, markers, text, lines, arrows, and scale bar

The class `PlotAstroData` also has methods for plotting regions (patches), markers, text, lines, and arrows. The following is the explanation of each method for this purpose.

The `add_region` method overlays an ellipse or a rectangular. the given data in the format of a segment map, as is often used for polarization maps.

```
p.add_region(patch='ellipse',
             poslist=[[0.5, 0.5], [0.1, 0.2]],
             majlist=[0.3, 1.0],
             minlist=[0.2, 0.8],
             palist=[0, 90])
```

The argument `patch` may be 'ellipse' or 'rectangle'. The patch position can be specified by a 2D list like `[0.1, 0.2]` or a coordinate string like '01h23m45.6s 01d23m45.6s'. The list means a fractional position from left to right and bottom to top: e.g., `[0, 0]`, `[0.5, 0.5]`, and `[1, 1]` are bottom left, center, and top right, respectively. `majlist`, `minlist`, and `palist` specifies the patch size in the unit of arcsec and the orientation in the unit of degree. Other arguments for `matplotlib.patches.Ellipse` or `matplotlib.patches.Rectangle` can be used in this method. Another method `add_beam` uses this method and is executed internally in `add_color`, `add_contour`, `add_segment`, `add_rgb`.

The `add_marker` method overlays markers.

```
p.add_marker(poslist=[[0.5, 0.5], [0.1, 0.2]])
```

Except for the position list `poslist` (same as in `add_region`), the marker properties can be specified by the arguments for `Axes.plot` of `matplotlib`.

The `add_text` method overlays text.

```
p.add_marker(poslist=[[0.5, 0.5], [0.1, 0.2]],
             slist=['abs', 'hoge'])
```

Except for the position list `poslist` (same as in `add_region`) and the list of text `slist`, the text properties can be specified by the arguments for `Axes.text` of matplotlib.

The `add_line` method overlays lines.

```
p.add_marker(poslist=[[0.5, 0.5], [0.1, 0.2]],
             anglelist=[0, 90],
             rlist=[0.4, 1])
```

The position list `poslist` (same as in `add_region`) specifies the start position of the line. `anglelist` and `rlist` specify the position angle in the unit of degree and the length in the unit of arcsec of the line, respectively. Other arguments for `Axes.plot` of matplotlib can be used in this method.

The `add_arrow` method overlays arrows.

```
p.add_marker(poslist=[[0.5, 0.5], [0.1, 0.2]],
             anglelist=[0, 90],
             rlist=[0.4, 1])
```

`poslist`, `anglelist`, and `rlist` are the same in `add_line`. Other arguments for `Axes.quiver` of matplotlib can be used in this method.

The `add_scalebar` method overlays a scale bar.

```
p.add_scalebar(length=0.5,
               label='70 au',
               barpos=[0.8, 0.1])
```

The bar length `length` is in the unit of arcsec. The bar label `label` is located above the bar. `barpos` is a fractional position from left to right and from bottom to top (same as `poslist`). In addition, the arguments of `color`, `fontsize`, `linewidth`, and `bbox` can be used in this method. `bbox` is a dictionary argument for `Axes.text` of matplotlib.

### 3.3 Setting axes and saving figures

The method `set_axis` (or `set_axis_radec`) is necessary even without any argument. This method provides axes of relative coordinates and can also adjust things related to the axes.

```
p.set_axis(title='figure title')
```

The `title` argument can be either string or dictionary; the latter is a set of arguments for `Axes.set_title` or `Figure.suptitle` of matplotlib. This method can also take more arguments related to `Axes.set_*` of matplotlib: `xscale`, `yscale`, `xlim`, `ylim`, `xlabel`, `ylabel`, `xticks`, `yticks`, `xticklabels`, and `yticklabels` are in the same format as in `Axes.set_*` of matplotlib. `xticksminor` and `yticksminor` are either list or integer; the latter means how many times more ticks are needed than the major ticks. Two more dictionary arguments, `grid` and `aspect`, available as for `Axes.grid` and `Axes.set_aspect` of matplotlib.

The method `set_axis_radec` provides axes in the right ascension and declination coordinates.

```
p.set_axis_radec(title='figure title',
                 xlabel='R.A. (ICRS)',
```

```

        ylabel='Dec. (ICRS)',
        nticksminor=2,
        grid=None)

```

`title`, `xlabel`, `ylabel`, and `grid` are the same as in `set_axis`. `nticksminor` specifies how many times more ticks are needed than the major ticks.

The method `savefig` saves the figure as an image file and/or shows it on the screen.

```

p.savefig(filename='hoge.png',
          show=True)

```

In addition to the two arguments, the arguments for `Figure.savefig` of matplotlib can be used for this method.

The method `get_figax` returns the Figure and Axes objects.

```

fig, ax = p.get_figax()

```

### 3.4 Other plotting functions

The function `plot3d` is a function independent of the `PlotAstroData` class. This function provides an HTML file to show a 3D figure that can be interactively rotated in a web browser.

```

plot3d(**d.todict(),
       levels=[3, 6, 9],
       cmap='Jet',
       alpha=0.08,
       xlabel='R.A. (arcsec)',
       ylabel='Dec. (arcsec)',
       vlabel='Velocity (km/s)',
       eye_p=0,
       eye_i=180,
       outname='filename',
       show=True)

```

The data to be plotted can be an instance of `AstroData`. `levels` specifies which surfaces are plotted. `cmap` is an argument (named colorscale) used in the 'mesh3d' type data in `plotly.graph_objs`. `alpha` is also used through the 'mesh3d' type data in `plotly.graph_objs`. `eye_p` and `eye_i` specify the default viewing direction. The output has the extension of `.html` with the file name of `outname`. When `show=True`, a web browser will be executed automatically to show the 3D figure.

The `plot_utils` module has more functions to make other types of figures. `plotprofile` provides a figure of line profiles and `plotslice` provides a 1D slice of a 2D image. These two functions use `AstroData.profile` and `AstroData.slice`, respectively. Hence, it may be more flexible to make figures in one's preferred way using the outputs of these method than using `plotprofile` and `plotslice`.

## 4 Relative and Absolute Coordinates

The relation between relative and absolute coordinates is not trivial on the plane of the sky. For example, the point 30 degrees (= 2h) east of '00h00m00s 60d00m00s' has coordinates of '03h16m25.6s 48d35m25s', rather than '2h00m00s 60d00m00s'. The module `coord_utils` provides useful functions for the coordinate transformation.



```

from plotastrodata.coord_utils import xy2coord
from plotastrodata.coord_utils import coord2xy
s = xy2coord(xy=[[30, 90], [0, 0]], coordorg='00h00m00s 60d00m00s')
print(s)
#['03h16m25.58528421s +48d35m25.36040662s', '06h00m00s +00d00m00s']
a = coord2xy(coords=s, coordorg='00h00m00s 60d00m00s')
print(a)
#[[30, 90], [0, 0]]

```

This example calculates 30 degrees east (and 0 degrees north) and 90 degrees east (and 0 degrees north) of '00h00m00s 60d00m00s' and puts back the resulting coordinates to the relative coordinates in the unit of degree ([offset to the east, offset to the north]).

## 5 Rotation

Comparison of a physical model and an observational result often requires 3D rotation between the model coordinates and the observational coordinates. The `los_utils` module provides a useful coordinate transformation. It starts with a parabolic streamer, as an example, on a coordinate set,  $(x_{\text{sys}}, y_{\text{sys}}, z_{\text{sys}})$ , named system coordinates, as shown in Figure 1(a). The direction of such a streamer is defined with polar and azimuthal angles ( $\theta_0$  and  $\phi_0$ , respectively) in a 3D coordinate,  $(x_{\text{phy}}, y_{\text{phy}}, z_{\text{phy}})$ , named physical coordinates. Figures 1(b) and 1(c) show the relation between  $(x_{\text{sys}}, y_{\text{sys}}, z_{\text{sys}})$  and  $(x_{\text{phy}}, y_{\text{phy}}, z_{\text{phy}})$ , through an intermediate coordinate set,  $(x_{\text{azi}}, y_{\text{azi}}, z_{\text{azi}})$ , named azimuthal coordinates.

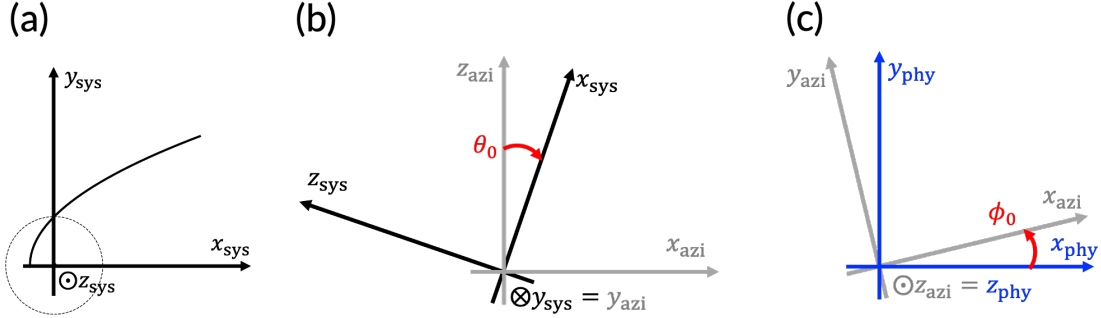


Figure 1: (a) The streamer system. (b) The system and azimuthal coordinates. (c) The azimuthal and physical coordinates.

When a model in the physical coordinates is observed, the relation between the physical and observational coordinates  $(x_{\text{obs}}, y_{\text{obs}}, z_{\text{obs}})$  requires inclination and position (or orientation) angles. Although this relation also requires another azimuthal angle, the  $\phi_0$  defined above will work for the azimuthal rotation. Figures 2(a) and 2(b) show the relation between  $(x_{\text{phy}}, y_{\text{phy}}, z_{\text{phy}})$  and  $(x_{\text{obs}}, y_{\text{obs}}, z_{\text{obs}})$ , through an intermediate coordinate set,  $(x_{\text{ori}}, y_{\text{ori}}, z_{\text{ori}})$ , named oriented coordinates. In this definition, when the zero position angle (P.A.= 0) means a configuration where the  $z_{\text{phy}}$  direction is projected to the  $y_{\text{obs}}$  direction. In other words, *this P.A. is not that of the disk major axis but that of the blueshifted outflow in a typical protostellar system.*

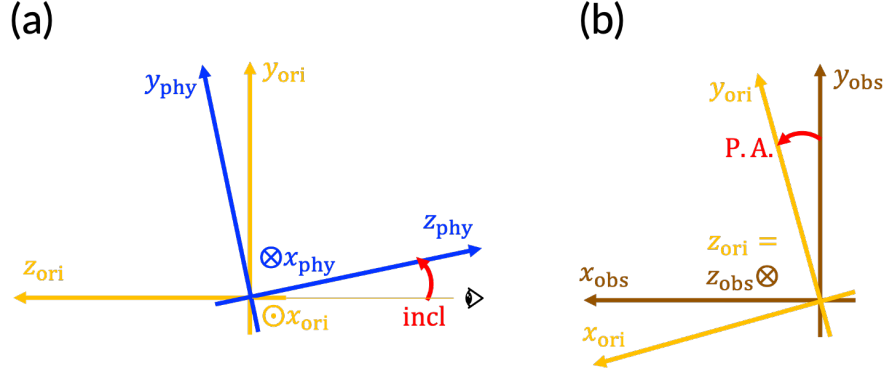


Figure 2: (a) The physical and oriented coordinates. (b) The oriented and observational coordinates.

Figure 3 summarizes the relation between the system and observational coordinates with the four angles ( $\theta_0$ ,  $\phi_0$ , inclination angle, and P.A.) through the physical coordinates. The relation

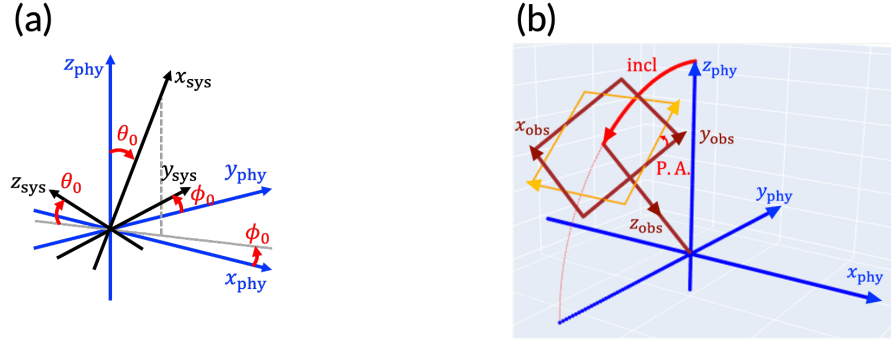


Figure 3: (a) The system and physical coordinates. (b) The physical and observational coordinates.

can be expressed by the rotational matrices  $R_x(\theta)$ ,  $R_y(\theta)$ , and  $R_z(\theta)$  as follows:

$$\mathbf{x}_{\text{sys}} = R_y\left(\frac{\pi}{2} - \theta_0\right)\mathbf{x}_{\text{azi}}, \quad (1)$$

$$\mathbf{x}_{\text{ori}} = R_z(-\phi_0)\mathbf{x}_{\text{phy}}, \quad (2)$$

$$\mathbf{x}_{\text{phy}} = \begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix} R_x(-\text{incl})\mathbf{x}_{\text{ori}}, \quad (3)$$

$$\mathbf{x}_{\text{ori}} = R_z(\text{P.A.})\mathbf{x}_{\text{obs}}. \quad (4)$$

The transformation between  $\mathbf{x}_{\text{obs}}$  and  $\mathbf{x}_{\text{sys}}$  can be done through the functions `obs2sys` and `sys2obs` in `los_utils`.

```

from plotastrodata.los_utils import obs2sys
from plotastrodata.los_utils import sys2obs
import numpy as np

xobs, yobs, zobs = sys2obs(xsys=1/np.sqrt(2), ysys=1/np.sqrt(2), zsys=0,
pa=0, incl=30, phi0=0, theta0=90, polar=False)
print(xobs, yobs, zobs)
#-0.707107 0.612372 0.353553
#-1/sqrt(2) cos(30deg)/sqrt(2) sin(30deg)/sqrt(2)
xsys, ysys, zsys = obs2sys(xobs=xobs, yobs=yobs, zobs=zobs, pa=0, incl=30,
phi0=0, theta0=90, polar=False)
print(xsys, ysys, zsys)
#0.7071077 0.707107 0.000000
#1/sqrt(2) 1/sqrt(2) 0

```

The input coordinate (e.g., `xsys` or `xobs`) may be a numpy array. When `polar=True`, `xsys`, `ysys`, and `zsys` are the radius, polar angle, and azimuthal angle, respectively; the radius is in the unit of arcsec, and the polar and azimuthal angles are in the unit of radian. `xobs`, `yobs`, and `zobs` are the Cartesian coordinates regardless of the `polar` argument. In particular, the combination of `polar=True` and  $\theta_0 = 90$  is useful when a model is defined in the physical coordinates in the polar format.

In addition to the functions for the spatial coordinate transformation, `los_utils` has another function, `polarvel2losvel`, to transform polar velocities ( $v_r, v_\theta, v_\phi$ ) to line-of-sight velocity (i.e.,  $v_{z,\text{obs}}$ ).

```

from plotastrodata.los_utils import polarvel2losvel
import numpy as np

v = polarvel2losvel(v_r=-1/np.sqrt(2), v_theta=0, v_phi=1/np.sqrt(2),
theta=np.pi/2, phi=np.pi/2, incl=30, phi0=0, theta0=90)
print(v)
#-0.353553
#-1/sqrt(2)/2

```

`theta` and `phi` may be numpy arrays and in the unit of radian. `incl`, `phi0`, and `theta0` are the same as in `obs2sys` and `sys2obs`. This velocity transformation is useful for calculating the line-of-sight velocity when the 3D velocity field of a model is written in the polar format as a function of the polar coordinates.