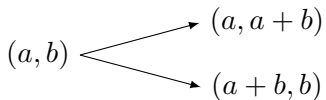
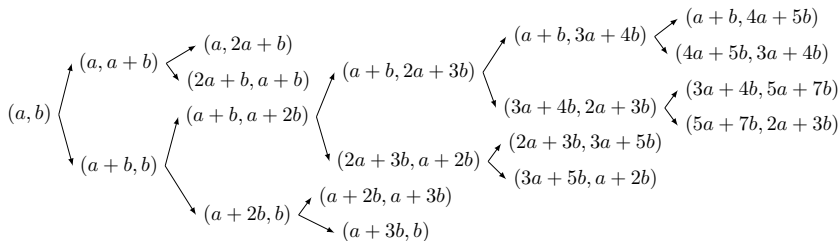


$$(1) \ P = \{p, q, r, s\}, \ N_P(a) = p, \ N_P(b) = q, \ N_P(a + b) = 1.$$



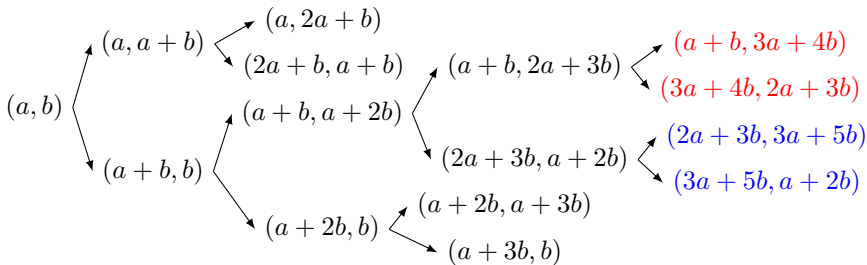
$$\text{APT}_P(a, b) = \{(a, b), (a, a + b), (a + b, b)\}.$$

- (2)  $P = \{p, q, r, s\}$ ,  $N_P(a) = p$ ,  $N_P(b) = q$ ,  $N_P(a + b) = r$ ,  
 $N_P(2a + 3b) = s$ ,  
 (i)  $p = 2$ ,  $q \neq 3, 5$ .



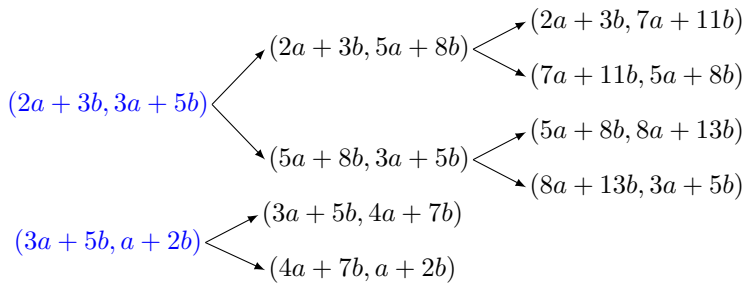
$$\begin{aligned} \text{APT}_P(a, b) = \Big\{ & (a, b), (a, a + b), (a + b, b), (a, 2a + b) \\ & (2a + b, a + b), (a + b, a + 2b), (a + 2b, b), \\ & (a + b, 2a + 3b), (2a + 3b, a + 2b), (a + 2b, a + 3b), \\ & (a + 3b, b), (a + b, 3a + 4b), (3a + 4b, 2a + 3b), \\ & (2a + 3b, 3a + 5b), (3a + 5b, a + 2b), (a + b, 4a + 5b), \\ & (4a + 5b, 3a + 4b), (3a + 4b, 5a + 7b), (5a + 7b, 2a + 3b) \Big\}. \end{aligned}$$

- (2)  $P = \{p, q, r, s\}$ ,  $N_P(a) = p$ ,  $N_P(b) = q$ ,  $N_P(a + b) = r$ ,  
 $N_P(2a + 3b) = s$ ,  
(ii)  $p = 2$ ,  $q = 3$ ,  $r \neq 5$ .



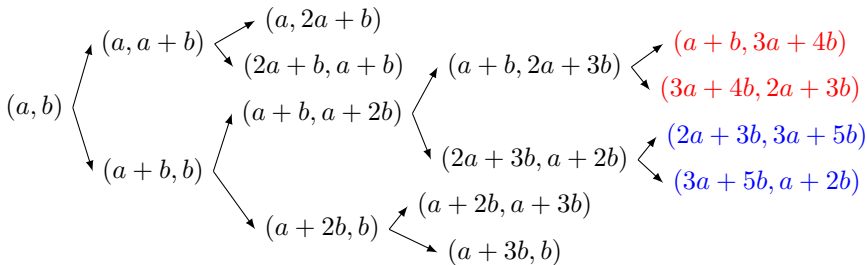
$$(a + b, 3a + 4b) \begin{cases} \rightarrow (a + b, 4a + 5b) \\ \rightarrow (4a + 5b, 3a + 4b) \end{cases}$$

$$(3a + 4b, 2a + 3b) \begin{cases} \rightarrow (3a + 4b, 5a + 7b) \\ \rightarrow (5a + 7b, 2a + 3b) \end{cases}$$



$$\begin{aligned} \text{APT}_P(a, b) = \big\{ & (a, b), (a, a + b), (a + b, b), (a, 2a + b) \\ & (2a + b, a + b), (a + b, a + 2b), (a + 2b, b), \\ & (a + b, 2a + 3b), (2a + 3b, a + 2b), (a + 2b, a + 3b), \\ & (a + 3b, b), (a + b, 3a + 4b), (3a + 4b, 2a + 3b), \\ & (2a + 3b, 3a + 5b), (3a + 5b, a + 2b), (a + b, 4a + 5b), \\ & (4a + 5b, 3a + 4b), (3a + 4b, 5a + 7b), (5a + 7b, 2a + 3b), \\ & (2a + 3b, 5a + 8b), (5a + 8b, 3a + 5b), (3a + 5b, 4a + 7b), \\ & (4a + 7b, a + 2b), (2a + 3b, 7a + 11b), (7a + 11b, 5a + 8b), \\ & (5a + 8b, 8a + 13b), (8a + 13b, 3a + 5b) \big\}. \end{aligned}$$

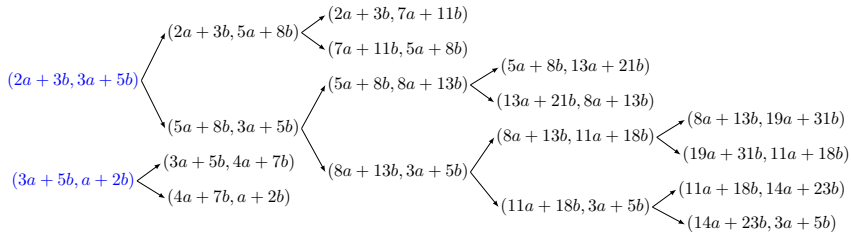
- (2)  $P = \{p, q, r, s\}$ ,  $N_P(a) = p$ ,  $N_P(b) = q$ ,  $N_P(a + b) = r$ ,  
 $N_P(2a + 3b) = s$ ,  
 (iii)  $p = 2$ ,  $q = 3$ ,  $r = 5$ .





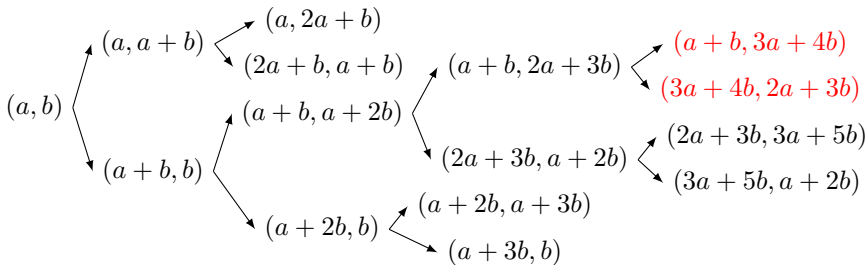
$$(a + b, 3a + 4b) \begin{cases} \rightarrow (a + b, 4a + 5b) \\ \rightarrow (4a + 5b, 3a + 4b) \end{cases}$$

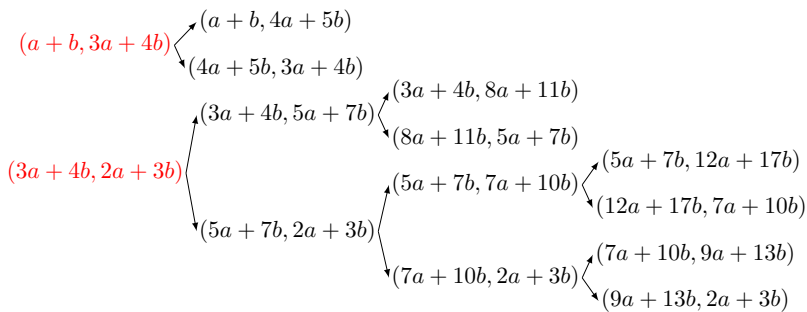
$$(3a + 4b, 2a + 3b) \begin{cases} \rightarrow (3a + 4b, 5a + 7b) \\ \rightarrow (5a + 7b, 2a + 3b) \end{cases}$$



$$\begin{aligned}
\text{APT}_P(a, b) = \Big\{ & (a, b), (a, a + b), (a + b, b), (a, 2a + b) \\
& (2a + b, a + b), (a + b, a + 2b), (a + 2b, b), \\
& (a + b, 2a + 3b), (2a + 3b, a + 2b), (a + 2b, a + 3b), \\
& (a + 3b, b), (a + b, 3a + 4b), (3a + 4b, 2a + 3b), \\
& (2a + 3b, 3a + 5b), (3a + 5b, a + 2b), (a + b, 4a + 5b), \\
& (4a + 5b, 3a + 4b), (3a + 4b, 5a + 7b), (5a + 7b, 2a + 3b), \\
& (2a + 3b, 5a + 8b), (5a + 8b, 3a + 5b), (3a + 5b, 4a + 7b), \\
& (4a + 7b, a + 2b), (2a + 3b, 7a + 11b), (7a + 11b, 5a + 8b), \\
& (5a + 8b, 8a + 13b), (8a + 13b, 3a + 5b), (5a + 8b, 13a + 21b), \\
& (13a + 21b, 8a + 13b), (8a + 13b, 11a + 18b), (11a + 18b, 3a + 5b), \\
& (8a + 13b, 19a + 31b), (19a + 31b, 11a + 18b), (11a + 18b, 14a + 23b), \\
& (14a + 23b, 3a + 5b) \Big\}.
\end{aligned}$$

- (2)  $P = \{p, q, r, s\}$ ,  $N_P(a) = p$ ,  $N_P(b) = q$ ,  $N_P(a + b) = r$ ,  
 $N_P(2a + 3b) = s$ ,  
 (iv)  $p = 2$ ,  $q = 5$ ,  $r \neq 3$ .

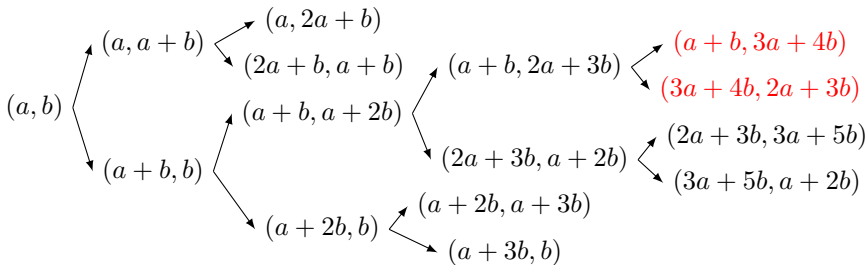


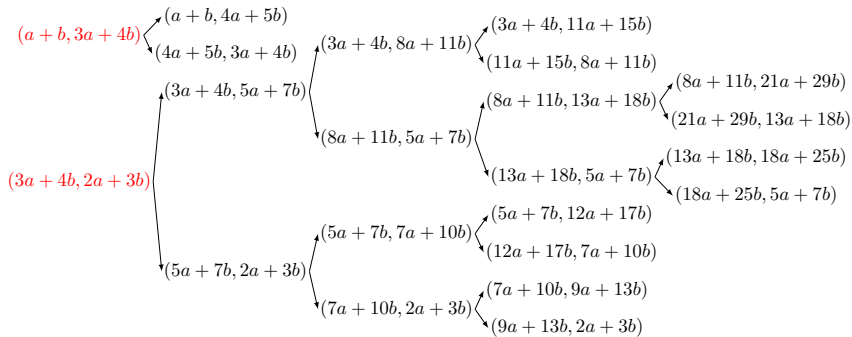


$$\text{APT}_P(a, b) =$$

$$\begin{aligned} & \left\{ (a, b), (a, a + b), (a + b, b), (a, 2a + b) \right. \\ & \quad (2a + b, a + b), (a + b, a + 2b), (a + 2b, b), \\ & \quad (a + b, 2a + 3b), (2a + 3b, a + 2b), (a + 2b, a + 3b), \\ & \quad (a + 3b, b), (a + b, 3a + 4b), (3a + 4b, 2a + 3b), \\ & \quad (2a + 3b, 3a + 5b), (3a + 5b, a + 2b), (a + b, 4a + 5b), \\ & \quad (4a + 5b, 3a + 4b), (3a + 4b, 5a + 7b), (5a + 7b, 2a + 3b), \\ & \quad (3a + 4b, 8a + 11b), (8a + 11b, 5a + 7b), (5a + 7b, 7a + 10b), \\ & \quad (7a + 10b, 2a + 3b), (5a + 7b, 12a + 17b), (12a + 17b, 7a + 10b), \\ & \quad \left. (7a + 10b, 9a + 13b), (9a + 13b, 2a + 3b) \right\}. \end{aligned}$$

- (2)  $P = \{p, q, r, s\}$ ,  $N_P(a) = p$ ,  $N_P(b) = q$ ,  $N_P(a + b) = r$ ,  
 $N_P(2a + 3b) = s$ ,  
 (v)  $p = 2$ ,  $q = 5$ ,  $r = 3$ .



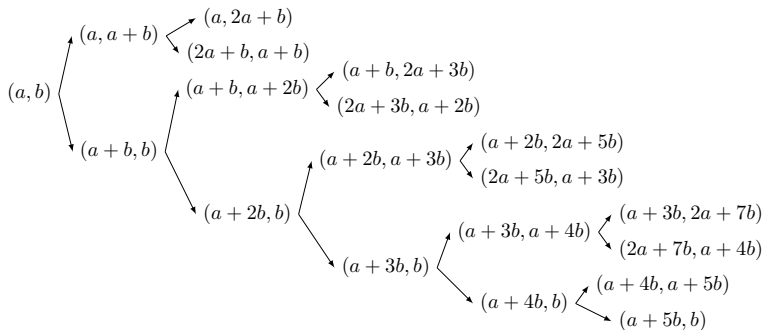




$$\text{APT}_P(a, b) =$$

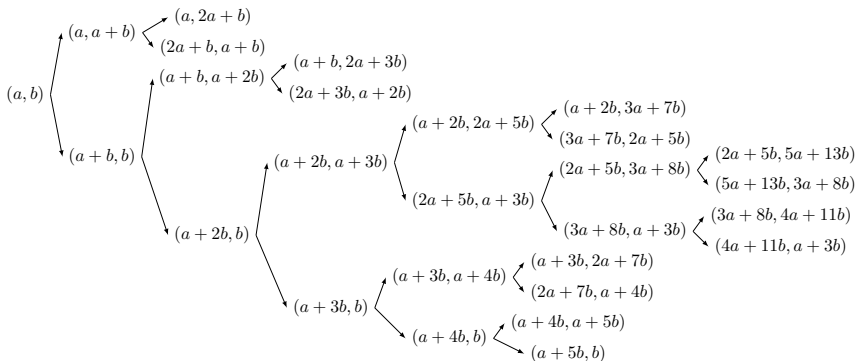
$$\begin{aligned} & \left\{ (a, b), (a, a + b), (a + b, b), (a, 2a + b), \right. \\ & \quad (2a + b, a + b), (a + b, a + 2b), (a + 2b, b), \\ & \quad (a + b, 2a + 3b), (2a + 3b, a + 2b), (a + 2b, a + 3b), \\ & \quad (a + 3b, b), (a + b, 3a + 4b), (3a + 4b, 2a + 3b), \\ & \quad (2a + 3b, 3a + 5b), (3a + 5b, a + 2b), (a + b, 4a + 5b), \\ & \quad (4a + 5b, 3a + 4b), (3a + 4b, 5a + 7b), (5a + 7b, 2a + 3b), \\ & \quad (3a + 4b, 8a + 11b), (8a + 11b, 5a + 7b), (5a + 7b, 7a + 10b), \\ & \quad (7a + 10b, 2a + 3b), (3a + 4b, 11a + 15b), (11a + 15b, 8a + 11b), \\ & \quad (8a + 11b, 13a + 18b), (13a + 18b, 5a + 7b), (5a + 7b, 12a + 17b), \\ & \quad (12a + 17b, 7a + 10b), (7a + 10b, 9a + 13b), (9a + 13b, 2a + 3b), \\ & \quad (8a + 11b, 21a + 29b), (21a + 29b, 13a + 18b), \\ & \quad \left. (13a + 18b, 18a + 25b), (18a + 25b, 5a + 7b) \right\}. \end{aligned}$$

- (3)  $P = \{p, q, r, s\}$ ,  $N_P(a) = p$ ,  $N_P(b) = q$ ,  $N_P(a + b) = r$ ,  
 $N_P(a + 3b) = s$ ,  $N_P(2a + b) = 1$ ,  
 (i)  $p = 2$ ,  $r \neq 3, 5$ .



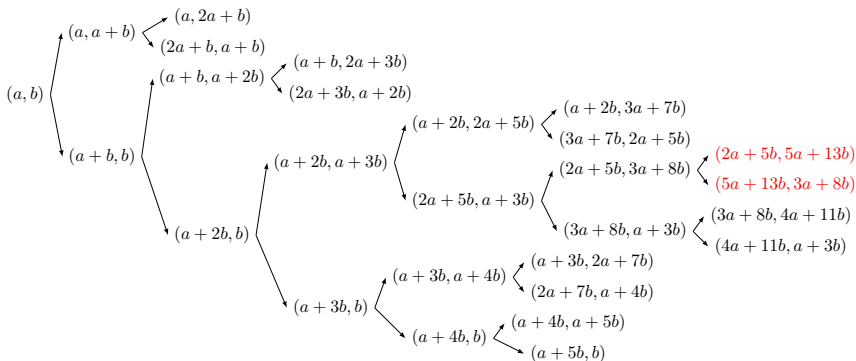
$$\begin{aligned} \text{APT}_P(a, b) = \big\{ & (a, b), (a, a + b), (a + b, b), (a, 2a + b) \\ & (2a + b, a + b), (a + b, a + 2b), (a + 2b, b), \\ & (a + b, 2a + 3b), (2a + 3b, a + 2b), (a + 2b, a + 3b), \\ & (a + 3b, b), (a + 2b, 2a + 5b), (2a + 5b, a + 3b), \\ & (a + 3b, a + 4b), (a + 4b, b), (a + 3b, 2a + 7b), \\ & (2a + 7b, a + 4b), (a + 4b, a + 5b), (a + 5b, b) \big\}. \end{aligned}$$

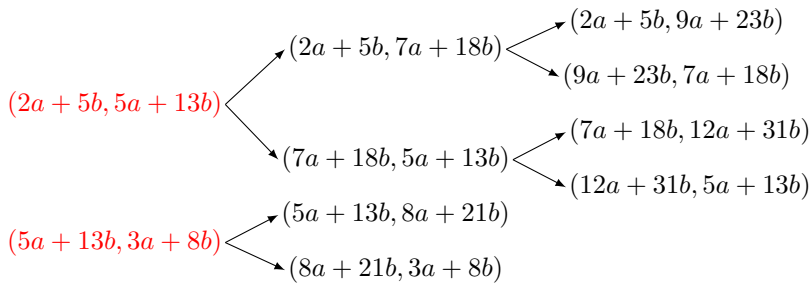
- (3)  $P = \{p, q, r, s\}$ ,  $N_P(a) = p$ ,  $N_P(b) = q$ ,  $N_P(a + b) = r$ ,  
 $N_P(a + 3b) = s$ ,  $N_P(2a + b) = 1$ ,  
(ii)  $p = 2$ ,  $r = 3$ ,  $q \neq 5$ .



$$\begin{aligned} \text{APT}_P(a, b) = \{ & (a, b), (a, a + b), (a + b, b), (a, 2a + b) \\ & (2a + b, a + b), (a + b, a + 2b), (a + 2b, b), \\ & (a + b, 2a + 3b), (2a + 3b, a + 2b), (a + 2b, a + 3b), \\ & (a + 3b, b), (a + 2b, 2a + 5b), (2a + 5b, a + 3b), \\ & (a + 3b, a + 4b), (a + 4b, b), (a + 2b, 3a + 7b), \\ & (3a + 7b, 2a + 5b), (2a + 5b, 3a + 8b), (3a + 8b, a + 3b), \\ & (a + 3b, 2a + 7b), (2a + 7b, a + 4b), (a + 4b, a + 5b) \\ & (a + 5b, b), (2a + 5b, 5a + 13b), (5a + 13b, 3a + 8b), \\ & (3a + 8b, 4a + 11b), (4a + 11b, a + 3b) \}. \end{aligned}$$

- (3)  $P = \{p, q, r, s\}$ ,  $N_P(a) = p$ ,  $N_P(b) = q$ ,  $N_P(a + b) = r$ ,  
 $N_P(a + 3b) = s$ ,  $N_P(2a + b) = 1$ ,  
 (iii)  $p = 2$ ,  $r = 3$ ,  $q = 5$ .

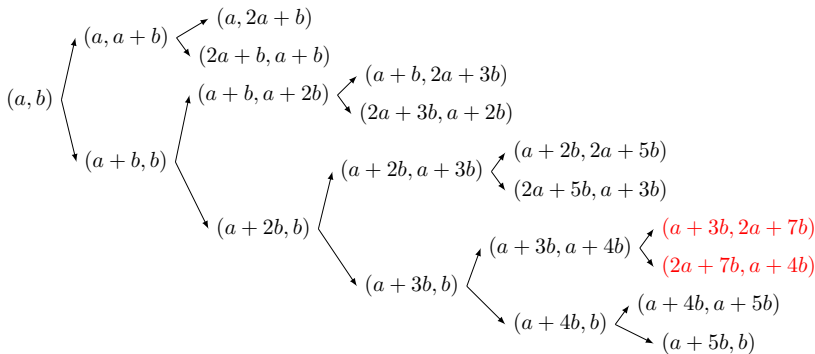


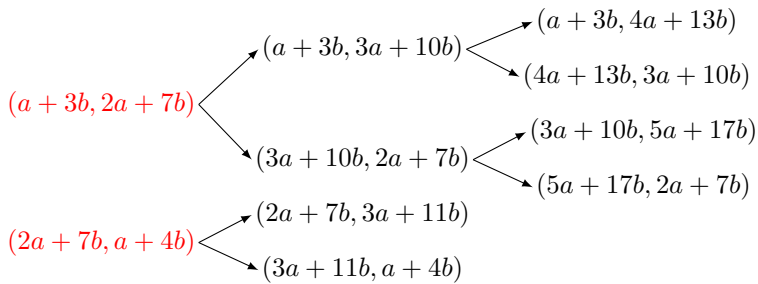


$$\begin{aligned}
\text{APT}_P(a, b) = \big\{ & (a, b), (a, a + b), (a + b, b), (a, 2a + b) \\
& (2a + b, a + b), (a + b, a + 2b), (a + 2b, b), \\
& (a + b, 2a + 3b), (2a + 3b, a + 2b), (a + 2b, a + 3b), \\
& (a + 3b, b), (a + 2b, 2a + 5b), (2a + 5b, a + 3b), \\
& (a + 3b, a + 4b), (a + 4b, b), (a + 2b, 3a + 7b), \\
& (3a + 7b, 2a + 5b), (2a + 5b, 3a + 8b), (3a + 8b, a + 3b), \\
& (a + 3b, 2a + 7b), (2a + 7b, a + 4b), (a + 4b, a + 5b) \\
& (a + 5b, b), (2a + 5b, 5a + 13b), (5a + 13b, 3a + 8b), \\
& (3a + 8b, 4a + 11b), (4a + 11b, a + 3b), \\
& (2a + 5b, 7a + 18b), (7a + 18b, 5a + 13b), \\
& (5a + 13b, 8a + 21b), (8a + 21b, 3a + 8b), \\
& (2a + 5b, 9a + 23b), (9a + 23b, 7a + 18b), \\
& (7a + 18b, 12a + 31b), (12a + 31b, 5a + 13b) \big\}.
\end{aligned}$$



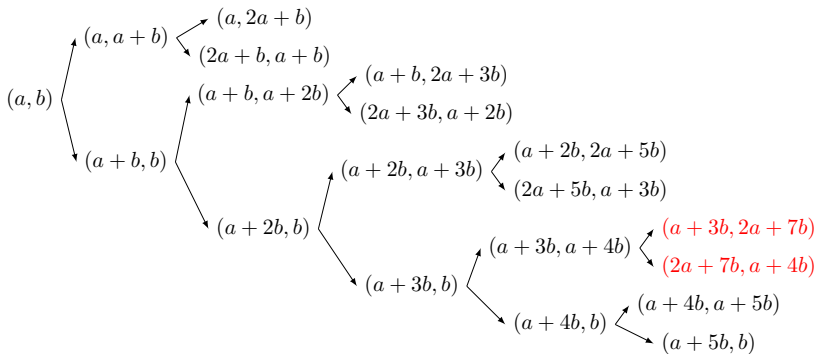
- (3)  $P = \{p, q, r, s\}$ ,  $N_P(a) = p$ ,  $N_P(b) = q$ ,  $N_P(a + b) = r$ ,  
 $N_P(a + 3b) = s$ ,  $N_P(2a + b) = 1$ ,  
 (iv)  $p = 2$ ,  $r = 5$ ,  $q \neq 3$ .

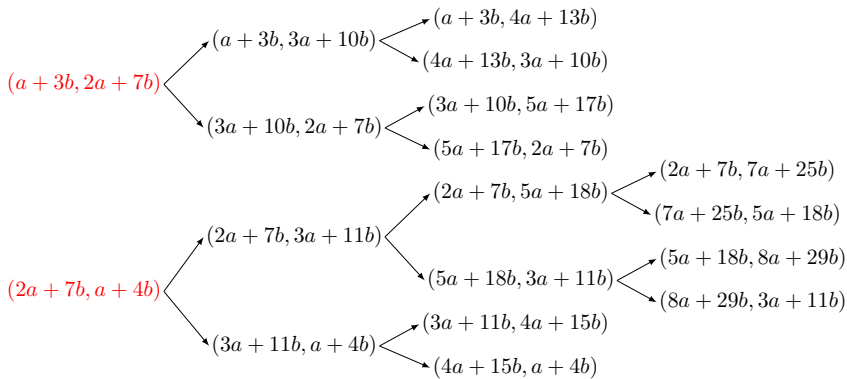




$$\begin{aligned}
\text{APT}_P(a, b) = \big\{ & (a, b), (a, a + b), (a + b, b), (a, 2a + b) \\
& (2a + b, a + b), (a + b, a + 2b), (a + 2b, b), \\
& (a + b, 2a + 3b), (2a + 3b, a + 2b), (a + 2b, a + 3b), \\
& (a + 3b, b), (a + 2b, 2a + 5b), (2a + 5b, a + 3b), \\
& (a + 3b, a + 4b), (a + 4b, b), (a + 3b, 2a + 7b), \\
& (2a + 7b, a + 4b), (a + 4b, a + 5b), (a + 5b, b), \\
& (a + 3b, 3a + 10b), (3a + 10b, 2a + 7b), (2a + 7b, 3a + 11b) \\
& (3a + 11b, a + 4b), (a + 3b, 4a + 13b), \\
& (4a + 13b, 3a + 10b), (3a + 10b, 5a + 17b), \\
& (5a + 17b, 2a + 7b) \big\}.
\end{aligned}$$

- (3)  $P = \{p, q, r, s\}$ ,  $N_P(a) = p$ ,  $N_P(b) = q$ ,  $N_P(a + b) = r$ ,  
 $N_P(a + 3b) = s$ ,  $N_P(2a + b) = 1$ ,  
 (v)  $p = 2$ ,  $r = 5$ ,  $q = 3$ .





$$\begin{aligned}
\text{APT}_P(a, b) = \big\{ & (a, b), (a, a + b), (a + b, b), (a, 2a + b) \\
& (2a + b, a + b), (a + b, a + 2b), (a + 2b, b), \\
& (a + b, 2a + 3b), (2a + 3b, a + 2b), (a + 2b, a + 3b), \\
& (a + 3b, b), (a + 2b, 2a + 5b), (2a + 5b, a + 3b), \\
& (a + 3b, a + 4b), (a + 4b, b), (a + 3b, 2a + 7b), \\
& (2a + 7b, a + 4b), (a + 4b, a + 5b), (a + 5b, b), \\
& (a + 3b, 3a + 10b), (3a + 10b, 2a + 7b), (2a + 7b, 3a + 11b), \\
& (3a + 11b, a + 4b), (a + 3b, 4a + 13b), \\
& (4a + 13b, 3a + 10b), (3a + 10b, 5a + 17b), \\
& (5a + 17b, 2a + 7b), (2a + 7b, 5a + 18b), \\
& (5a + 18b, 3a + 11b), (3a + 11b, 4a + 15b), \\
& (4a + 15b, a + 4b), (2a + 7b, 7a + 25b), \\
& (7a + 25b, 5a + 18b), (5a + 18b, 8a + 29b), \\
& (8a + 29b, 3a + 11b) \big\}.
\end{aligned}$$