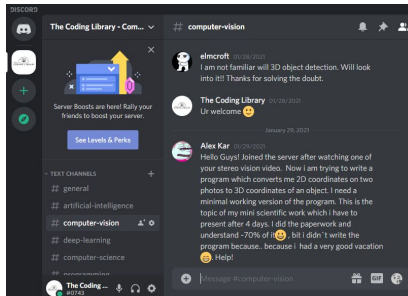


Computer Vision

Corner Detection



Discord Link in Description

Corners in Images

- Features in images
 - Matching points between frames of an environment
 - Relate images to each other and extract information
 - Features are uniquely recognizable
- Types of features in images
 - Edges
 - Corners (interest points)
 - Blobs (regions of interest)
- Corner is an intersection of two edges
 - Point in which the directions of the two edges change
 - Gradients have a high variation



How to Find Corners in Images

- Determine Cornerness values for each pixel
 - Produces a Cornerness map
- Non-maxima suppression
 - Multiple responses
 - Compare to local neighbours
- Threshold the Cornerness map
 - To get the most significant corners



Harris Corner Detector

- Variation of intensity

$$E(u, v) = \sum_{x,y} w(x, y) [I(x + u, y + v) - I(x, y)]^2$$

where:

- $w(x, y)$ is the window at position (x, y)
- $I(x, y)$ is the intensity at (x, y)
- $I(x + u, y + v)$ is the intensity at the moved window $(x + u, y + v)$

- Using Taylor expansion, rearranging and on matrix form

$$M = \sum_{x,y} w(x, y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

$$E(u, v) \approx [u \quad v] M \begin{bmatrix} u \\ v \end{bmatrix}$$

- Calculate a score of the probability that it is a corner

$$R = \det(M) - k(\text{trace}(M))^2$$

where:

- $\det(M) = \lambda_1 \lambda_2$
- $\text{trace}(M) = \lambda_1 + \lambda_2$

a window with a score R greater than a certain value is considered a "corner"

Harris Corner Detector

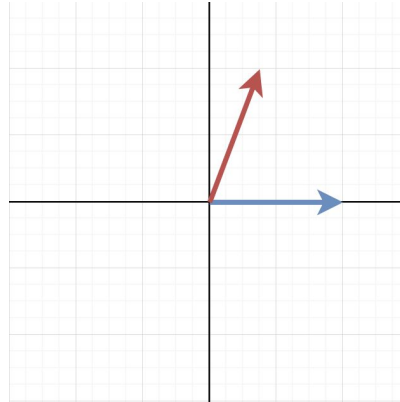
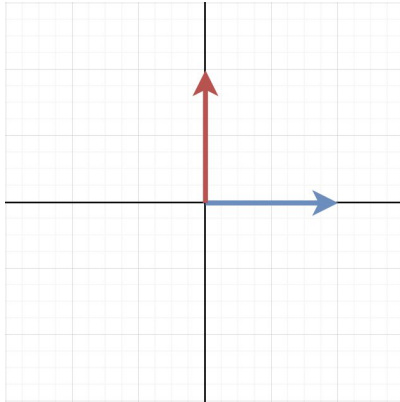
Output Harris



Eigenvalues and Eigenvectors

- Linear Algebra
- An eigenvector changes by a scalar factor when a linear transformation is applied to it
- Eigenvalue is the factor which the eigenvector is scaled

$$A\mathbf{u} = \lambda\mathbf{u}.$$



Shi-Tomasi Corner Detection

- Uses eigenvalues to detect corners and same approach as Harris Corner
 - Calculate the corner quality at every pixel in the image
- Non-maximum suppression
- Corners with minimal eigenvalues less than some threshold are rejected
- Remaining corners are sorted by quality in descending order
- Throws away corners where there is a better corner at a distance less than a maximum distance

Shi-Tomasi Corner Detection



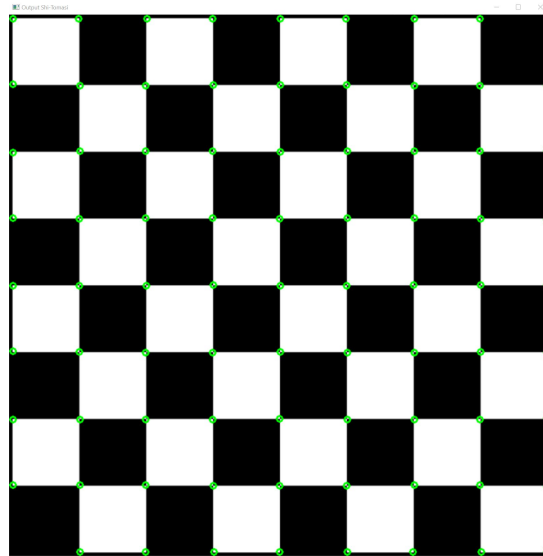
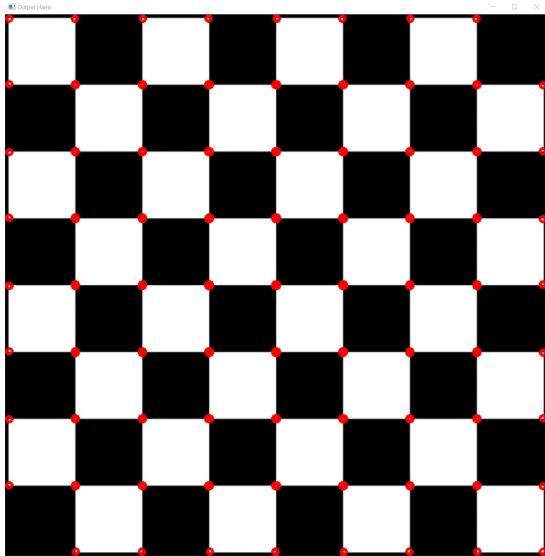
Harris Corner VS Shi-Tomasi

```
cornerHarris(gray, output,  
3,           // Neighborhood size  
3,           // Aperture parameter for the Sobel operator  
0.04);       // Harris detector free parameter
```

```
goodFeaturesToTrack(gray,  
corners,  
100,         // Max corners to detect  
0.01,        // Minimal quality of corners  
10,          // Minimum Euclidean distance between the returned corners  
Mat(),       // Optional region of interest  
3,           // Size of an average block for computing a derivative covariation matrix over each pixel neighborhood  
false,       // Use Harri Detector or cornerMinEigenVal - Like when you create your own  
0.04);       // Free parameter for the Harris detector
```

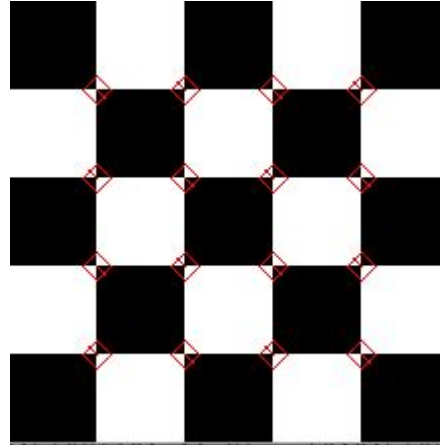
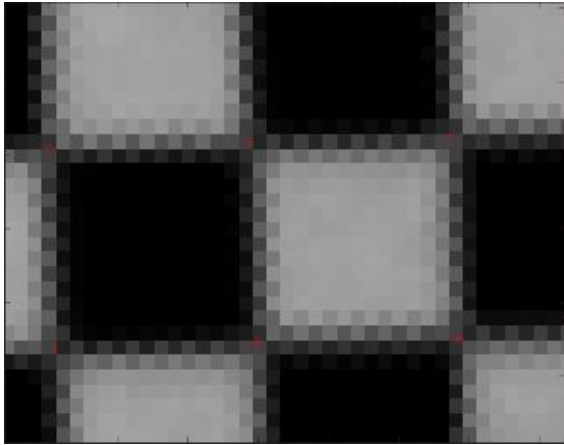


Harris Corner VS Shi-Tomasi



Corner Detection in Subpixels

- A way to find more exact corner positions by using subpixels
 - Normally it is integer pixels



Create Your Own Corner Detector

- Create your own corner detector like the Harris and Shi-Tomasi
- Find the eigenvalues and eigenvectors to determine if a pixel is a corner
- Find the minimum eigenvalues for corner detection

