CSE 415 Autumn 2019 Assignment 4

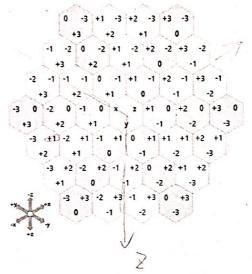
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		day night Octo d on this assign		and the same of th		maximum of one l	ate day
		owing three exe			l to take 20-30	minutes each if yo	ou know
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	1 Effi	ciency of	Search	Algorit	hms		Willey!
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	Suppose a	binary tree-sea	rching algor	ithm needs to	2-	eximum depth of	How-
						tree, $0 \le d \le 4$.	L
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	followi					t be done by each	
	DFS:	22	BFS:	13	IDDFS:	23	
7)		nts) Now for a c s of the worst-c			$_{i}$ g N vertices, $_{i}$	ive Big-Theta cha	racteri-
	DFS:	B(N)	BFS:	b(N)	IDDFS:	6(N)	
		11		1		. ^	
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(c)	(6 points) Now for a general tree having N vertices, and any branching factor, including 1, or even irregular (varying numbers of children, but obviously always non-negative numbers), give Big-Theta characterizations of the worst-case running times:						
	DFS: $\theta(N)$ BFS: $\theta(N)$ IDDFS: $\theta(N^2)$						
(d)	(6 points) Using Big-Theta notation again, describe the amount of memory required by each algorithm for the general tree of N vertices. DFS: $\theta(N)$ BFS: $\theta(N)$ IDDFS: $\theta(N)$						
(e)	(4 points) Suppose we now want to use graph-search versions of these algorithms. What is an important benefit of BFS and IDDFS that DFS does not have?						
	BFS and IDDFS are guaranteed to find the sourcest path. but DFS cannot guaranteed						
	(3 points) What impact does a heuristic function have on the run time of the A* algorithm? Assume that the heuristic is admissible and that we don't consider the cost of computing the heuristic function itself. A good heuristic function can help us to save the run time of A* save it will expand less nodes while finding the						
	shivest puth.						
(g)	(4 points) What does an admissible heuristic do for us in the best and worst cases? (Consider the cost of computing the heuristic function as well as other issues.)						
	Best case = Poes not expand any extra states to find the shortest						
	Worst COME: Does not aoural expand the sterters from UCS and more time to run the hermistic function.						

2 Heuristic Search

Imagine that you are part of a game-design team creating a game that takes place in a hexagonal grid world. Your job is to evaluate some heuristics proposed to help the monsters of the game do path planning.

The figure below shows a general hexagonal grid in which each cell is identifiable by a triple of coordinates: x (which tells how far it is from the origin on an axis that makes an angle of $\pi/6$ with the horizontal axis), y (which tells how far from the origin it is on an axis that makes an angle of $5\pi/6$ with the horizontal axis), and z (which tells how far down from the origin it is on the vertical axis). Note that there is (intentionally) some redundancy here. In particular, x + y + z = 0.



We define the distance between two adjacent cells as follows:

$$d((x_1, y_1, z_1), (x_2, y_2, z_2)) = |x_1 - x_2| + 2 \cdot |y_1 - y_2| + 4 \cdot |z_1 - z_2|$$

The monsters in the game need to perform path planning for two reasons. One is to escape from fighting with the protagonist. The other is to move towards the protagonist to make an attack. (Although the monsters should not be too intelligent, we will assume that they do need to know what the lowest-cost path is between their starting states and destination states.)

Suppose the operators are the following, in the sequence given. Note that only the state-transformation portion of each operator is shown here, but they all have a precondition that monsters are not allowed to go out of the grid or walk through walls. Also note that the order in which the operators are listed has significance during the various searches.

$$\phi_{0}: x \leftarrow x + 1 \text{ and } y \leftarrow y - 1. \qquad \qquad \phi_{3}: y \leftarrow y + 1 \text{ and } x \leftarrow x - 1. \qquad \qquad \downarrow$$

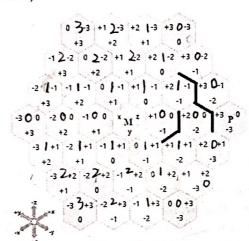
$$\phi_{1}: z \leftarrow z + 1 \text{ and } y \leftarrow y - 1. \qquad \qquad \downarrow$$

$$\phi_{2}: z \leftarrow z + 1 \text{ and } x \leftarrow x - 1. \qquad \searrow$$

$$\phi_{5}: x \leftarrow x + 1 \text{ and } z \leftarrow z - 1. \qquad \searrow$$

The cost of going from one cell to a neighbor depend on the operator. For example, applying ϕ_3 to state M leads to state (-1, +1, 0), so that the distance value, by the formula above, is 3. The cost of a path is, as usual, the sum of its edge costs.

(a) (6 points) Consider the problem of finding a lowest-cost path from M to P in the example game situation below. The thick black walls in the diagram represent barriers through which the monsters must not pass. (Therefore, the precondition for operator ϕ_0 is not satisfied at state (+1, -1, 0), and neither is the precondition for operator ϕ_1 , so that this state has only 4 successors.)



What is the cost of the shortest path? (i.e., total distance for all its edges)

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(b) (6 points) What is the number of states that would be expanded by UCS to find a lowest-cost path from M to P?

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(c) (4 points) Consider the heuristic $h_x((x, y, z)) = \min(|x - x_g|, |y - y_g|, |z - z_g|)$, where (x_g, y_g, z_g) refer to the coordinates of the goal cell.

Determine whether or not h_x is admissible and explain why it is or why it is not.

the is admissible.

The distance between a cell and goal cell is 1x-xy1+21y-yy1
+412-2y1 > hx(x,y,z). It is never overestimated.

(d) (6 points) Determine how many states would be expanded by A^* using h_x to find a shortest path from M to P.

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(e) (5 points) Explain how the use of the heuristic is affecting the search (compared with UCS).

for mis ha, ha value is smaller on the right side which means states prefer to expend to right side. Therefore, A* with he will assider less states of right side.

(f) (5 points) Propose another heuristic that you believe will outperform h_x . (Do not propose the exact distance defined above or function that includes it.) Give a formula to define your function. Also give an argument for or against its admissibility. Why do you believe it will outperform h_x ?

hx is admissible since it never overestimated.

1x-xg1+z1y-yg1+412-zg1>hx.

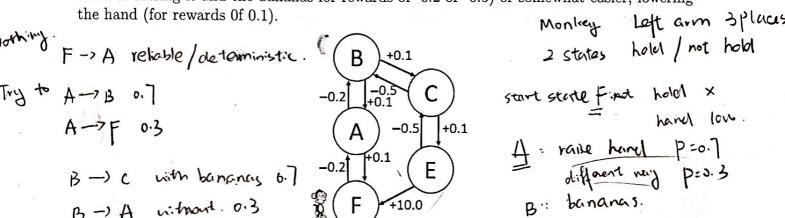
hx=1x-xg1 win help us conside less expanded state-left

(g) (3 points) How many states will be expanded by A* using your heuristic to find a shortest path from M to P?

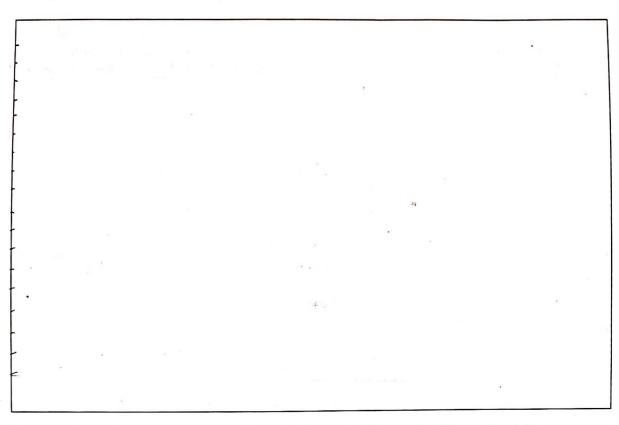
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3 Markov Decision Processes

Consider a situation in which a robot monkey is in a room in which some bananas are hanging from the ceiling. The monkey can move its left arm to any one of 3 different places, and it might be holding or not holding bananas in either of two states. The monkey starts out not holding bananas with left hand low (state F). It can try to raise its hand, and so it can transition to state A. However, this monkey has a somewhat unreliable body, and most actions are only effective with probability 0.7. (Then, with probability 0.3, the arm goes a different way. But there is 0 probability of staying in the same state.) The action of raising the hand from state F, however, is the one completely reliable and deterministic action, so the next state after that action is guaranteed to be state A If the monkey again tries to raise his hand from state A, there is a 0.7 probability of arriving in state B, which is roughly where the bananas are. There is a probability of 0.3 that the action will cause the monkeys hand to move back down to state F. From state B, the monkey has a choice of action: (G) grab the bananas and go down to state C, or (D) leave the bananas and go down to state A. (These again are nondeterministic, so action G in state B goes to C with probability 0.7 and to state A with probability 0.3; action D in state B goes to A with probability 0.7 and to C with probability 0.3.) From state C, the monkey can go to state E or back up to state B. From state E, the monkey can finally get the bananas all the way down and consume them, for a reward of +10. Note that the other rewards are either effort-consuming (raising the hand or raising it and the bananas for rewards of -0.2 or -0.5) or somewhat easier, lowering



(a) (10 points) Create a table representing the function T(s, a, s') for this MDP. Assume that there are three possible actions: U, D and G. U means try to go up, and D means try to go down. G means try to grab the bananas (and go down from B to C). Action U is applicable only at states A, C, E, and F. Action D is applicable only at states A, B, C, and E. Action G is only applicable at state B. In this table you do not have to provide an explicit entry for any T(s, a, s') whose value is 0. Hint: there should be 17 entries in your table.

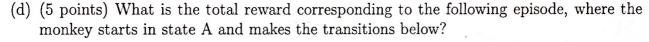


(b) (5 points) Create a table representing the function R(s, a, s'). There should be one explicit entry here for each explicit entry you gave in part (a).

B-1-9.

(c) (10 points) Create a table representing the expected reward for taking action a in state s. Call this function $Q_1(s,a)$. Note: if action a is not allowed in state s then $S_1(s,a) = 0$. The expected reward is the *expectation* of the reward from state s given that the action

is s. Because of the nondeterminism in the actions, this is normally a weighted sum of the possible rewards out of s, and the weight corresponding to action a is usually the largest of the weights. Hint: there should be 9 entries in your table.



A-D-F-U-A-U-B-D-A-U-B-G-C-D-B-G-C-D-E-D-C-D-E-D-F-U-A

(Add up all the actual rewards here; do not use expected rewards.)

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