#### 311306435

#### 2023-07-18

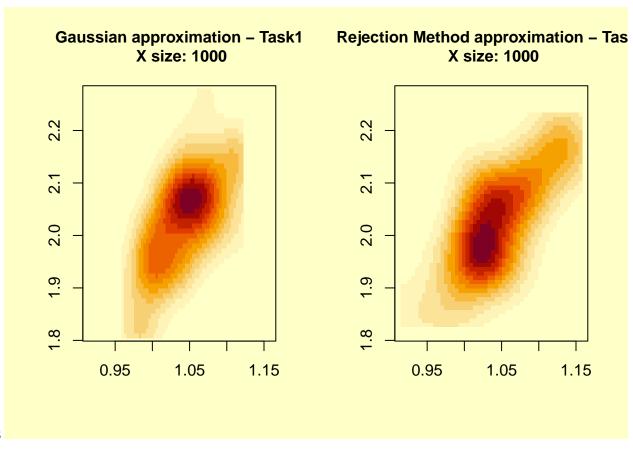
```
r = getOption("repos")
r["CRAN"] = "http://cran.us.r-project.org"
options(repos = r)
install.packages("DirichletReg")
## Installing package into 'C:/Users/Yuval-PC/AppData/Local/R/win-library/4.3'
## (as 'lib' is unspecified)
## package 'DirichletReg' successfully unpacked and MD5 sums checked
## Warning: cannot remove prior installation of package 'DirichletReg'
## Warning in file.copy(savedcopy, lib, recursive = TRUE): problem copying
## C:\Users\Yuval-PC\AppData\Local\R\win-library\4.3\00L0CK\DirichletReg\libs\x64\DirichletReg.dll
## C:\Users\Yuval-PC\AppData\Local\R\win-library\4.3\DirichletReg\libs\x64\DirichletReg.dll:
## Permission denied
## Warning: restored 'DirichletReg'
##
## The downloaded binary packages are in
## C:\Users\Yuval-PC\AppData\Local\Temp\RtmpArAAVq\downloaded_packages
install.packages("scatterplot3d") # Install
## Installing package into 'C:/Users/Yuval-PC/AppData/Local/R/win-library/4.3'
## (as 'lib' is unspecified)
## package 'scatterplot3d' successfully unpacked and MD5 sums checked
##
## The downloaded binary packages are in
## C:\Users\Yuval-PC\AppData\Local\Temp\RtmpArAAVq\downloaded_packages
install.packages("MASS")
## Installing package into 'C:/Users/Yuval-PC/AppData/Local/R/win-library/4.3'
## (as 'lib' is unspecified)
## package 'MASS' successfully unpacked and MD5 sums checked
## Warning: cannot remove prior installation of package 'MASS'
## Warning in file.copy(savedcopy, lib, recursive = TRUE): problem copying
## C:\Users\Yuval-PC\AppData\Local\R\win-library\4.3\00L0CK\MASS\libs\x64\MASS.dll
## to C:\Users\Yuval-PC\AppData\Local\R\win-library\4.3\MASS\libs\x64\MASS.dll:
## Permission denied
## Warning: restored 'MASS'
```

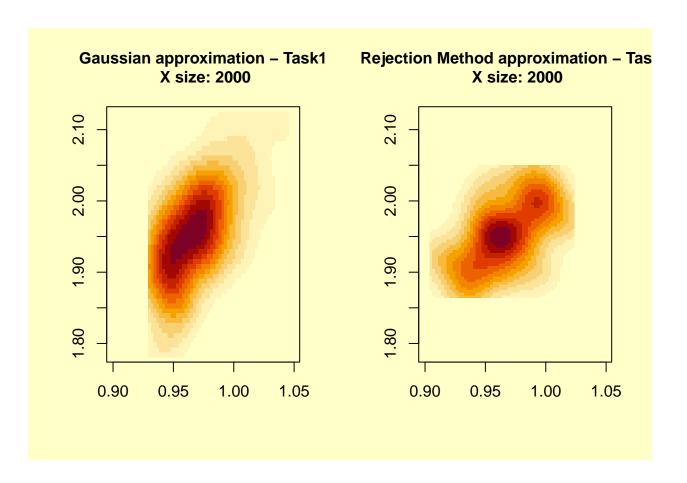
```
##
## The downloaded binary packages are in
## C:\Users\Yuval-PC\AppData\Local\Temp\RtmpArAAVq\downloaded_packages
install.packages("MCMCprecision")
## Installing package into 'C:/Users/Yuval-PC/AppData/Local/R/win-library/4.3'
## (as 'lib' is unspecified)
## package 'MCMCprecision' successfully unpacked and MD5 sums checked
## Warning: cannot remove prior installation of package 'MCMCprecision'
## Warning in file.copy(savedcopy, lib, recursive = TRUE): problem copying
## C:\Users\Yuval-PC\AppData\Local\R\win-library\4.3\00L0CK\MCMCprecision\libs\x64\MCMCprecision.dll
## C:\Users\Yuval-PC\AppData\Local\R\win-library\4.3\MCMCprecision\libs\x64\MCMCprecision.dll:
## Permission denied
## Warning: restored 'MCMCprecision'
##
## The downloaded binary packages are in
## C:\Users\Yuval-PC\AppData\Local\Temp\RtmpArAAVq\downloaded_packages
install.packages("ggpubr")
## Installing package into 'C:/Users/Yuval-PC/AppData/Local/R/win-library/4.3'
## (as 'lib' is unspecified)
## package 'ggpubr' successfully unpacked and MD5 sums checked
## The downloaded binary packages are in
## C:\Users\Yuval-PC\AppData\Local\Temp\RtmpArAAVq\downloaded_packages
library(gridExtra)
library(ggpubr)
## Loading required package: ggplot2
library(cowplot)
## Attaching package: 'cowplot'
## The following object is masked from 'package:ggpubr':
##
##
       get_legend
require(MCMCprecision)
## Loading required package: MCMCprecision
library(Formula)
library(DirichletReg)
##
## Attaching package: 'DirichletReg'
## The following object is masked from 'package: MCMCprecision':
##
##
       rdirichlet
```

library("scatterplot3d") # load
library(MASS)

Question 1

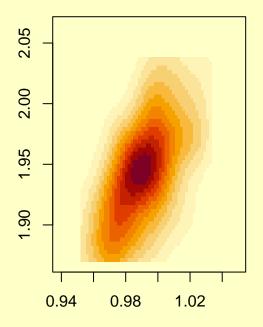
Question 2



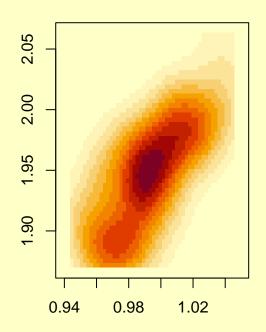


### Gaussian approximation – Task1 X size: 4000

## Rejection Method approximation – Tas X size: 4000

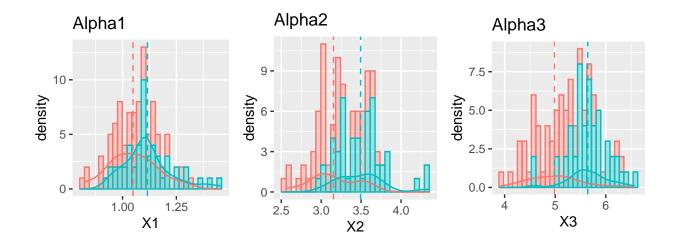


rates <-c(1,3,5)

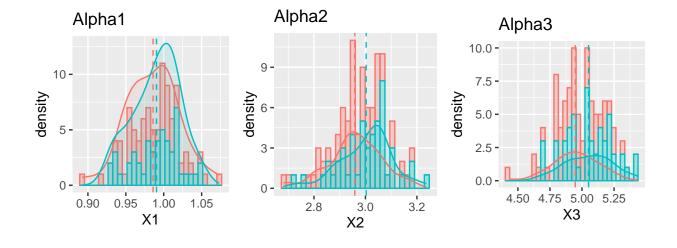


```
X <- rdirichlet(1000, rates)</pre>
q1_alphas \leftarrow q1(50, X, rates)
q2_alphas <- q2(50, X, rates)$Alpha
q1_df <- data.frame(q1_alphas)</pre>
q1 df$approximation <- "Guassian Task1"
q2_df <- data.frame(q2_alphas)</pre>
q2_df$approximation <- "Rejection_Task2"
df <- rbind(q1_df, q2_df)</pre>
## Warning: package 'ggplot2' is in use and will not be installed
## Warning: package 'gridExtra' is in use and will not be installed
## Installing package into 'C:/Users/Yuval-PC/AppData/Local/R/win-library/4.3'
## (as 'lib' is unspecified)
## package 'plyr' successfully unpacked and MD5 sums checked
## Warning: cannot remove prior installation of package 'plyr'
## Warning in file.copy(savedcopy, lib, recursive = TRUE): problem copying
## C:\Users\Yuval-PC\AppData\Local\R\win-library\4.3\00L0CK\plyr\libs\x64\plyr.dll
## to C:\Users\Yuval-PC\AppData\Local\R\win-library\4.3\plyr\libs\x64\plyr.dll:
## Permission denied
## Warning: restored 'plyr'
##
## The downloaded binary packages are in
```

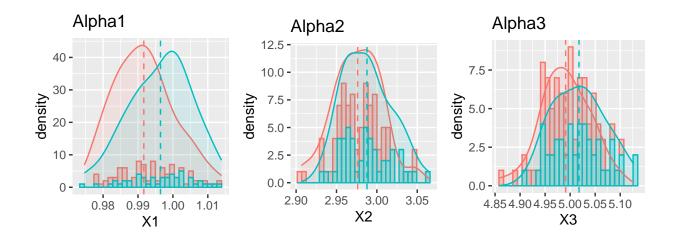
```
C:\Users\Yuval-PC\AppData\Local\Temp\RtmpArAAVq\downloaded_packages
##
## Attaching package: 'plyr'
##
  The following object is masked from 'package:ggpubr':
##
##
       mutate
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```







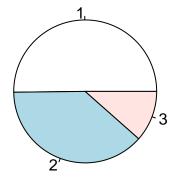
```
approximation Guassian_Task1 Rejection_Task2
```

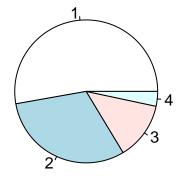
#### Question 4

```
Q3_non_zeros <- rowSums(Q3 >= 0.001)
Q4_non_zeros <- rowSums(Q4 >= 0.001)
par(mfrow=c(1,2))
pie(table(Q3_non_zeros), main="Q3 non zero elements count")
pie(table(Q4_non_zeros), main="Q4 non zero elements count")
```

## Q3 non zero elements count

#### Q4 non zero elements count



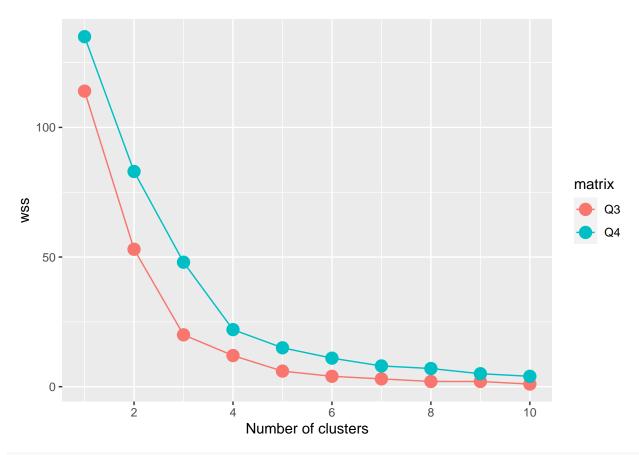


```
# Decide how many clusters to look at
n_clusters <- 10</pre>
# Initialize total within sum of squares error: wss
wss_Q3 <- matrix(nrow=n_clusters, ncol=3)</pre>
wss_Q4 <- matrix(nrow=n_clusters, ncol=3)</pre>
set.seed(123)
# Look over 1 to n possible clusters
for (i in 1:n_clusters) {
  print(i)
  # Fit the model: km.out
  km_out_Q3 <- kmeans(Q3, centers = i, nstart = 100)</pre>
  km_out_Q4 <- kmeans(Q4, centers = i, nstart = 100)</pre>
  # Save the within cluster sum of squares
  wss_Q3[i,1] <- i
  wss_Q4[i,1] <- i
  wss_Q3[i,2] <- km_out_Q3$tot.withinss</pre>
  wss_Q4[i,2] <- km_out_Q4$tot.withinss</pre>
  wss_Q3[i,3] <- "Q3"
  wss_Q4[i,3] <- "Q4"
```

```
## [1] 2
## [1] 3
```

## [1] 1

```
## [1] 4
## [1] 5
## [1] 6
## [1] 7
## [1] 8
## [1] 9
## [1] 10
# Produce a scree plot
concated_matrix <- rbind(wss_Q3, wss_Q4)</pre>
wss_df <- data.frame(clusters = as.integer(concated_matrix[,1]),</pre>
                     wss = as.integer(concated_matrix[,2]),
                     matrix = concated_matrix[,3])
print(wss_df)
##
      clusters wss matrix
## 1
             1 114
                        QЗ
## 2
             2 53
                        QЗ
             3 20
## 3
                        QЗ
## 4
             4
                12
                        QЗ
## 5
             5
                 6
                        QЗ
## 6
                 4
                        QЗ
             6
## 7
             7
                 3
                        QЗ
## 8
             8
                 2
                        QЗ
## 9
             9
                2
                        QЗ
## 10
            10
                1
                        QЗ
             1 135
## 11
                        Q4
## 12
             2 83
                        Q4
## 13
             3 48
                        Q4
             4 22
## 14
                        Q4
## 15
             5 15
                        Q4
## 16
             6 11
                        Q4
## 17
             7
                 8
                        Q4
## 18
                 7
                        Q4
             8
## 19
             9
                 5
                        04
## 20
            10
                        Q4
scree_plot <- ggplot(wss_df, aes(x = clusters, y = wss, color = matrix)) +</pre>
    geom_point(size = 4)+
    geom_line() +
    scale_x_continuous(breaks = c(2, 4, 6, 8, 10)) +
    xlab('Number of clusters')
scree_plot
```



#### install.packages('ggtern')

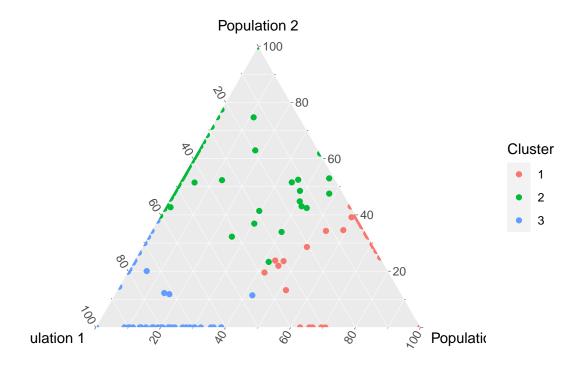
```
## Installing package into 'C:/Users/Yuval-PC/AppData/Local/R/win-library/4.3'
## (as 'lib' is unspecified)
## package 'ggtern' successfully unpacked and MD5 sums checked
##
## The downloaded binary packages are in
## C:\Users\Yuval-PC\AppData\Local\Temp\RtmpArAAVq\downloaded_packages
```

## library('ggtern')

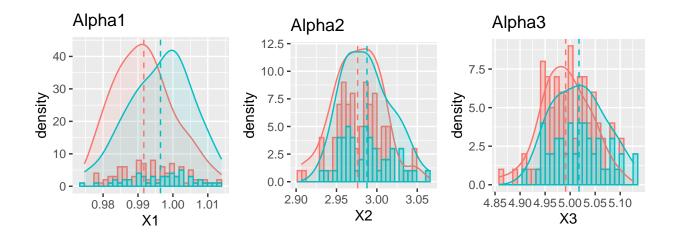
```
## Registered S3 methods overwritten by 'ggtern':
##
     method
                      from
##
     grid.draw.ggplot ggplot2
                      ggplot2
##
     plot.ggplot
##
     print.ggplot
                      ggplot2
## --
## Remember to cite, run citation(package = 'ggtern') for further info.
## --
##
## Attaching package: 'ggtern'
## The following objects are masked from 'package:ggplot2':
##
##
       aes, annotate, ggplot, ggplot_build, ggplot_gtable, ggplotGrob,
##
       ggsave, layer_data, theme_bw, theme_classic, theme_dark,
```

```
##
       theme_gray, theme_light, theme_linedraw, theme_minimal, theme_void
## The following objects are masked from 'package:gridExtra':
##
       arrangeGrob, grid.arrange
##
clusters <- kmeans(Q3, centers = 3, nstart = 100)$cluster
clusters <- as.factor(clusters)</pre>
Q3_clusters_df <- data.frame(Q3, clusters)
\# p1 <- ggplot(Q3_clusters_df, aes(x = V1, color=clusters)) +
  geom\ density(alpha=0.1)+
#
    theme(aspect.ratio = 1) +
  labs(title = "Alpha1 clusters")
\# p2 \leftarrow ggplot(Q3\_clusters\_df, aes(x = V2, color=clusters)) +
# geom density(alpha=0.1)+
    theme(aspect.ratio = 1) +
# labs(title = "Alpha2 clusters")
\# p3 \leftarrow ggplot(Q3\_clusters\_df, aes(x = V3, color=clusters)) +
  geom_density(alpha=0.1)+
    theme(aspect.ratio = 1) +
# labs(title = "Alpha2 clusters")
# combined <- ggarrange(p1, p2, p3, ncol=3, nrow=1, common.legend = TRUE, legend="bottom")
ggtern(data = Q3_clusters_df, aes(x = V1, y = V2, z = V3, color = clusters)) +
 geom_point() +
  labs(title = "K-means clustering with 3 clusters and k=3",
       x = "Population 1",
      y = "Population 2",
      z = "Population 3",
      color = "Cluster")
```

# K-means clustering with 3 clusters and k=3



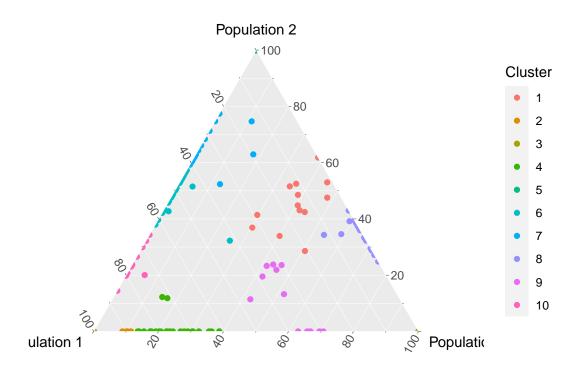
print(combined)



```
approximation Guassian_Task1 Rejection_Task2
```

```
clusters <- kmeans(Q3, centers = 10, nstart = 100)$cluster
clusters <- as.factor(clusters)
Q3_clusters_df <- data.frame(Q3, clusters)
ggtern(data = Q3_clusters_df, aes(x = V1, y = V2, z = V3, color = clusters)) +
    geom_point() +
    labs(title = "K-means clustering with 10 clusters and k=3",
        x = "Population 1",
        y = "Population 2",
        z = "Population 3",
        color = "Cluster")</pre>
```

## K-means clustering with 10 clusters and k=3



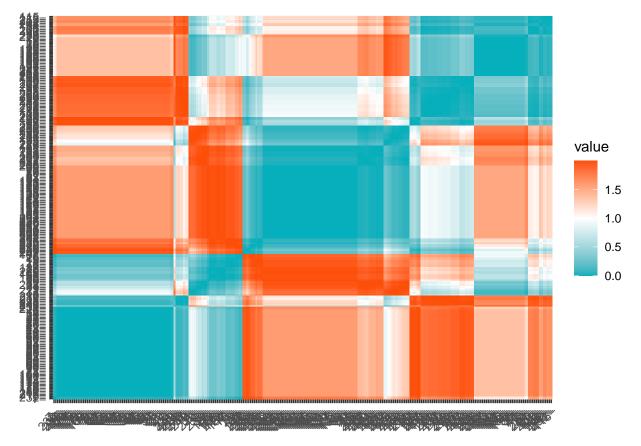
```
install.packages("factoextra")
## Installing package into 'C:/Users/Yuval-PC/AppData/Local/R/win-library/4.3'
## (as 'lib' is unspecified)
## package 'factoextra' successfully unpacked and MD5 sums checked
##
## The downloaded binary packages are in
  C:\Users\Yuval-PC\AppData\Local\Temp\RtmpArAAVq\downloaded_packages
install.packages("cluster")
## Installing package into 'C:/Users/Yuval-PC/AppData/Local/R/win-library/4.3'
## (as 'lib' is unspecified)
## package 'cluster' successfully unpacked and MD5 sums checked
## The downloaded binary packages are in
## C:\Users\Yuval-PC\AppData\Local\Temp\RtmpArAAVq\downloaded_packages
install.packages("magrittr")
## Installing package into 'C:/Users/Yuval-PC/AppData/Local/R/win-library/4.3'
## (as 'lib' is unspecified)
## package 'magrittr' successfully unpacked and MD5 sums checked
## Warning: cannot remove prior installation of package 'magrittr'
```

## Warning in file.copy(savedcopy, lib, recursive = TRUE): problem copying

```
## C:\Users\Yuval-PC\AppData\Local\R\win-library\4.3\00L0CK\magrittr\libs\x64\magrittr.dll
## t.o
## C:\Users\Yuval-PC\AppData\Local\R\win-library\4.3\magrittr\libs\x64\magrittr.dll:
## Permission denied
## Warning: restored 'magrittr'
## The downloaded binary packages are in
## C:\Users\Yuval-PC\AppData\Local\Temp\RtmpArAAVq\downloaded_packages
install.packages("dendextend")
## Installing package into 'C:/Users/Yuval-PC/AppData/Local/R/win-library/4.3'
## (as 'lib' is unspecified)
## package 'dendextend' successfully unpacked and MD5 sums checked
##
## The downloaded binary packages are in
## C:\Users\Yuval-PC\AppData\Local\Temp\RtmpArAAVq\downloaded_packages
library("cluster")
library("factoextra")
## Welcome! Want to learn more? See two factoextra-related books at https://goo.gl/ve3WBa
library("magrittr")
##
## Attaching package: 'magrittr'
## The following object is masked from 'package:tidyr':
##
##
       extract
library("dendextend")
##
## -----
## Welcome to dendextend version 1.17.1
## Type citation('dendextend') for how to cite the package.
##
## Type browseVignettes(package = 'dendextend') for the package vignette.
## The github page is: https://github.com/talgalili/dendextend/
##
## Suggestions and bug-reports can be submitted at: https://github.com/talgalili/dendextend/issues
## You may ask questions at stackoverflow, use the r and dendextend tags:
    https://stackoverflow.com/questions/tagged/dendextend
##
  To suppress this message use: suppressPackageStartupMessages(library(dendextend))
##
##
## Attaching package: 'dendextend'
## The following object is masked from 'package:ggpubr':
##
##
      rotate
## The following object is masked from 'package:stats':
```

```
##
## cutree
res.dist <- get_dist(Q3, stand = TRUE, method = "pearson")

fviz_dist(res.dist,
    gradient = list(low = "#00AFBB", mid = "white", high = "#FC4E07"))</pre>
```



## Warning: The `<scale>` argument of `guides()` cannot be `FALSE`. Use "none" instead as
## of ggplot2 3.3.4.

## i The deprecated feature was likely used in the factoextra package.

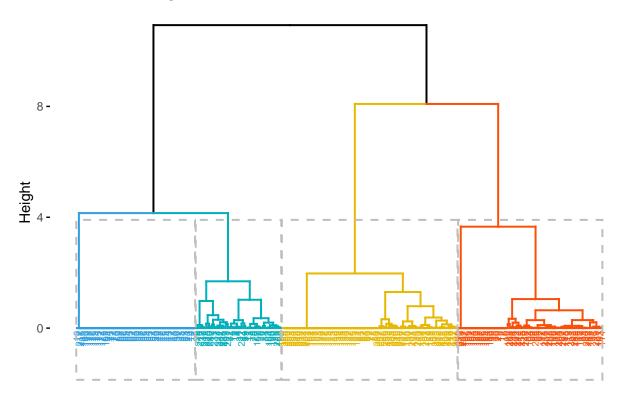
## Please report the issue at <a href="https://github.com/kassambara/factoextra/issues">https://github.com/kassambara/factoextra/issues</a>.

## This warning is displayed once every 8 hours.

## Call `lifecycle::last\_lifecycle\_warnings()` to see where this warning was

#### ## generated.

# Cluster Dendrogram



```
install.packages("fpc")
## Installing package into 'C:/Users/Yuval-PC/AppData/Local/R/win-library/4.3'
## (as 'lib' is unspecified)
## package 'fpc' successfully unpacked and MD5 sums checked
##
## The downloaded binary packages are in
   C:\Users\Yuval-PC\AppData\Local\Temp\RtmpArAAVq\downloaded_packages
install.packages("dbscan")
## Installing package into 'C:/Users/Yuval-PC/AppData/Local/R/win-library/4.3'
## (as 'lib' is unspecified)
## package 'dbscan' successfully unpacked and MD5 sums checked
##
## The downloaded binary packages are in
  C:\Users\Yuval-PC\AppData\Local\Temp\RtmpArAAVq\downloaded_packages
library("fpc")
library("dbscan")
##
## Attaching package: 'dbscan'
## The following object is masked from 'package:fpc':
##
```

```
##
       dbscan
## The following object is masked from 'package:stats':
##
##
       as.dendrogram
set.seed(123)
db <- fpc::dbscan(Q3, eps = 0.08, MinPts = 5)
# Plot DBSCAN results
library("factoextra")
fviz_cluster(db, data = Q3, stand = FALSE,
             ellipse = FALSE, show.clust.cent = FALSE,
             geom = "point",palette = "jco", ggtheme = theme_classic())
         Cluster plot
                                                                                         2
                                                                                         3
                                                                                         5
     0.5
                                                                                         8
Dim2 (34.4%)
                                                                                    cluster
```

#### install.packages("kernlab")

-0.8

-0.7

0.0

-0.5

```
## Installing package into 'C:/Users/Yuval-PC/AppData/Local/R/win-library/4.3'
## (as 'lib' is unspecified)
## package 'kernlab' successfully unpacked and MD5 sums checked
## Warning: cannot remove prior installation of package 'kernlab'
## Warning in file.copy(savedcopy, lib, recursive = TRUE): problem copying
## C:\Users\Yuval-PC\AppData\Local\R\win-library\4.3\00L0CK\kernlab\libs\x64\kernlab.dl1
## C:\Users\Yuval-PC\AppData\Local\R\win-library\4.3\kernlab\libs\x64\kernlab.dll:
## Permission denied
```

-0.6

Dim1 (46.2%)

-0.5

1 2 3

5

6

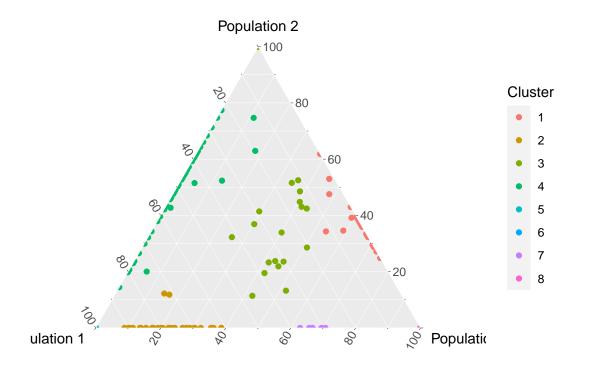
7

-0.3

-0.4

```
## Warning: restored 'kernlab'
##
## The downloaded binary packages are in
## C:\Users\Yuval-PC\AppData\Local\Temp\RtmpArAAVq\downloaded_packages
library(kernlab)
##
## Attaching package: 'kernlab'
## The following object is masked from 'package:ggplot2':
##
##
       alpha
set.seed(127)
clusters <- specc(Q3, centers = 8, scale=TRUE, kernel="splinedot")</pre>
clusters <- as.factor(clusters)</pre>
Q3_clusters_df <- data.frame(Q3, clusters)
g \leftarrow ggtern(data = Q3\_clusters\_df, aes(x = V1, y = V2, z = V3, color = clusters)) +
  geom_point() +
 labs(title = "Spectral clustering with splinedot kernel",
       x = "Population 1",
       y = "Population 2",
       z = "Population 3",
       color = "Cluster")
print(g)
```

# Spectral clustering with splinedot kernel



```
install.packages("GGally")
## Installing package into 'C:/Users/Yuval-PC/AppData/Local/R/win-library/4.3'
## (as 'lib' is unspecified)
## package 'GGally' successfully unpacked and MD5 sums checked
## The downloaded binary packages are in
## C:\Users\Yuval-PC\AppData\Local\Temp\RtmpArAAVq\downloaded_packages
library(GGally)
## Registered S3 method overwritten by 'GGally':
    method from
   +.gg ggplot2
# Generate some sample data with four variables
set.seed(123)
n <- 100
data <- data.frame(</pre>
 var1 = rnorm(n),
 var2 = rnorm(n),
 var3 = rnorm(n),
 var4 = rnorm(n)
)
# Create the scatterplot matrix
ggpairs(data)
```

```
var1
                                   var2
                                                         var3
                                                                               var4
 0.4 -
 0.3 -
                                  Corr:
                                                        Corr:
                                                                              Corr:
                                                                                            var1
 0.2 -
                                 -0.050
                                                       -0.129
                                                                             -0.044
 0.1
 0.0
  3 -
  2 -
                                                        Corr:
                                                                              Corr:
                                                                                            var2
                                                        0.031
                                                                              0.044
  2
                                                                              Corr:
                                                                                            var3
                                                                             -0.045
  2
                                                                                            var4
                                                                                Ö
# clusters <- as.factor(clusters)</pre>
# Q4_clusters_df <- data.frame(Q4, clusters)</pre>
install.packages(c("klaR", "scatterplot3d"))
## Warning: package 'scatterplot3d' is in use and will not be installed
## Installing package into 'C:/Users/Yuval-PC/AppData/Local/R/win-library/4.3'
## (as 'lib' is unspecified)
## package 'klaR' successfully unpacked and MD5 sums checked
##
## The downloaded binary packages are in
    \verb|C:\Users\Yuval-PC\AppData\Local\Temp\RtmpArAAVq\downloaded\_packages| \\
install.packages("haven")
## Installing package into 'C:/Users/Yuval-PC/AppData/Local/R/win-library/4.3'
## (as 'lib' is unspecified)
## package 'haven' successfully unpacked and MD5 sums checked
##
## The downloaded binary packages are in
   C:\Users\Yuval-PC\AppData\Local\Temp\RtmpArAAVq\downloaded_packages
library(haven)
library(klaR)
library(kernlab)
```

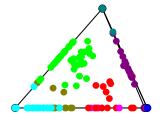
```
set.seed(132)
clusters <- specc(Q4, centers = 8, scale=TRUE, kernel="splinedot")</pre>
colors = c("#FF0000", "#808000", "#00FF00", "#00FFFF", "#008080", "#0000FF", "#FF00FF", "#800080")
par(mfrow=c(2,3))
for (angle in seq(0,150,30)){
  print(angle)
  quadplot(Q4,
           main=paste("spectral clustering angle:",toString(angle)),
           angle = angle,
           labelcol = "black",
           col=colors[c(clusters)],
           pch=19,
           lwd=2,
           cex=1,
           legend.control = list(plot=FALSE))
}
## [1] 0
## [1] 30
## [1] 60
## [1] 90
## [1] 120
```

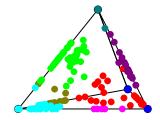
#### spectral clustering angle: 0

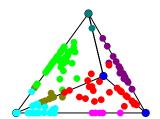
## [1] 150

## spectral clustering angle: 30

#### spectral clustering angle: 60







#### spectral clustering angle: 90

spectral clustering angle: 120

spectral clustering angle: 150

