

Hamming code receiver

- S \rightarrow HC \rightarrow 101001001111 \rightarrow there was some error
- R received was 101011001111

R 101011001111

$n=12$

$m=8$

$r=4$

1 0 1 0 1 1 0 0 1 1 1 1

- c1 c2 m c4 m m m c8 m m m m

- let counter = 0
- calculate check bits

$$3 = 1 + 2$$

$$5 = 1 + 4$$

$$6 = 2 + 4$$

$$7 = 1 + 2 + 4$$

$$9 = 1 + 8$$

$$10 = 2 + 8$$

$$11 = 1 + 2 + 8$$

$$12 = 4 + 8$$

calculated $c1=0, c2=0, c4=1, c8=0$

received $c1=1, c2=0, c4=0, c8=0$
counter = sum of all the check bit positions that have discrepancy
 $= 1 + 4 = 5$ i.e. 5th bit was in error

1 0 1 0 0 1 0 0 1 1 1 1

Ques A 12-bit hamming code whose hexadecimal value is 0xE4F arrives at a receiver. What was the original value in hexadecimal? Assume that not more than 1 bit is in the error.

$n=12$, $m=8$, $r=4$

received msg = 1110 0100 1111

calculations

$c1=1$

$c2=0$

$c3=0$

$c4=0$

counter = 2 i.e. 2nd bit is in error

invert 2nd bit

so, corrected codeword = 1010 0100 1111 = 0xA4F

what is the value of msg ? 1010 1111 = 0xAF

Ques Construct hamming code for BCD 0110.

ans 1100110

Two-dimensional parity check.

- In this method, the dataword is organized in a table (rows and columns).
- The data to be sent is five 7-bit bytes, are put in separate rows.
- For each row and each column, 1 parity-check bit is calculated. The whole table is then sent to the receiver, which finds the **syndrome for each row and each column**.
- The two-dimensional parity check can detect up to three errors that occur anywhere in the table (arrows point to the locations of the created nonzero syndromes). However, **errors affecting 4 bits** may not be detected.

Two-dimensional parity-check code

1	1	0	0	1	1	1	1	
1	0	1	1	1	0	1	1	
0	1	1	1	0	0	1	0	
0	1	0	1	0	0	1	1	
0	1	0	1	0	1	0	1	1
								Row parities
								Column parities

a. Design of row and column parities

1	1	0	0	1	1	1	1
1	0	1	1	1	0	1	1
0	1	1	1	0	0	1	0
0	1	0	1	0	0	1	1
<hr/>							
0	1	0	1	0	1	0	1



b. One error affects two parities

1	1	0	0	1	1	1	1
1	0	1	1	1	0	1	1
0	1	1	1	0	0	1	0
0	1	0	1	0	0	1	1
<hr/>							
0	1	0	1	0	1	0	1



c. Two errors affect two parities

1	1	0	0	1	1	1	1	←
1	0	1	1	1	0	1	1	←
0	1	1	1	0	0	1	0	←
0	1	0	1	0	0	1	1	
<hr/>								
0	1	0	1	0	1	0	1	↑

d. Three errors affect four parities

1	1	0	0	1	1	1	1	
1	0	1	1	1	0	1	1	
0	1	1	1	0	0	1	0	
0	1	0	1	0	0	1	1	
<hr/>								
0	1	0	1	0	1	0	1	

e. Four errors cannot be detected

c1 10001
c2 00001
c3 10101

sender will send all the codewords in a matrix format i.e.,
3x5

10001
00001
10101

