

# ELIMINATION OF LEFT RECURSION AND LEFT FACTORING

EX. NO. 3

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**AIM:** To write a program Elimination of Left recursion and Left factoring.

## ALGORITHM:

### (i) Algorithm for elimination of left recursion:

Suppose we have a grammar which contains left recursion:

$S \rightarrow S a / S b / c / d$

1. Check if the given grammar contains left recursion, if present then separate the production and start working on it.

In our example,

$S \rightarrow S a / S b / c / d$

2. Introduce a new nonterminal and write it at the last of every terminal. We produce a new nonterminal  $S'$  and write new production as,

$S \rightarrow cS' / dS'$

3. Write newly produced nonterminal in LHS and in RHS it can either produce or it can produce new production in which the terminals or non terminals which followed the previous LHS will be replaced by new nonterminal at last.

$S' \rightarrow ? / aS' / bS'$

So after conversion the new equivalent production is

$S \rightarrow cS' / dS'$

$S' \rightarrow ? / aS' / bS'$

### (ii) Algorithm for elimination of left factoring:

1. For each non terminal  $A$  find the longest prefix  $\alpha$  common to two or more of its alternatives.

2. If  $\alpha \neq \epsilon$ , i.e., there is a non trivial common prefix, replace all the  $A$  productions

$A \rightarrow \alpha\beta_1 | \alpha\beta_2 | \dots | \alpha\beta_n | \gamma$

where  $\gamma$  represents all alternatives that do not begin with  $\alpha$  by

$A \Rightarrow \alpha A' | \gamma$

$A' \Rightarrow \beta_1 | \beta_2 | \dots | \beta_n$

Here  $A'$  is new non terminal. Repeatedly apply this transformation until no two alternatives for a non-terminal have a common prefix.

EX: Perform left factoring on following grammar,

$A \rightarrow xByA \mid xByAzA \mid a$   $B \rightarrow b$

Left factored, the grammar becomes

$A \rightarrow xByAA' \mid a$   $A' \rightarrow zA \mid \epsilon$   $B \rightarrow b$

## PROGRAM :

### (i) Left Recursion:

```
gram = {  
    "E":["E+T","T"],  
    "T":["T*F","F"],  
    "F":["(E)","i"]  
}
```

```
def removeDirectLR(gramA, A):  
    temp = gramA[A]  
    tempCr = []  
    tempInCr = []  
    for i in temp:  
        if i[0] == A:  
            tempInCr.append(i[1:]+[A+""])  
        else:  
            tempCr.append(i+[A+""])  
    tempInCr.append(["e"])  
    gramA[A] = tempCr  
    gramA[A+""] = tempInCr  
    return gramA
```

```
def checkForIndirect(gramA, a, ai):  
    if ai not in gramA:  
        return False  
    if a == ai:  
        return True  
    for i in gramA[ai]:  
        if i[0] == ai:  
            return False  
        if i[0] in gramA:  
            return checkForIndirect(gramA, a, i[0])
```

```
return False
```

```
def rep(gramA, A):  
    temp = gramA[A]  
    newTemp = []  
    for i in temp:  
        if checkForIndirect(gramA, A, i[0]):  
            t = []  
            for k in gramA[i[0]]:  
                t=[]  
                t+=k  
                t+=i[1:]  
                newTemp.append(t)  
  
        else:  
            newTemp.append(i)  
    gramA[A] = newTemp  
    return gramA
```

```
def rem(gram):  
    c = 1  
    conv = {}  
    gramA = {}  
    revconv = {}  
    for j in gram:  
        conv[j] = "A"+str(c)  
        gramA["A"+str(c)] = []  
        c+=1  
  
    for i in gram:  
        for j in gram[i]:  
            temp = []  
            for k in j:  
                if k in conv:  
                    temp.append(conv[k])  
                else:  
                    temp.append(k)  
            gramA[conv[i]].append(temp)  
  
    for i in range(c-1,0,-1):
```

```

    ai = "A"+str(i)
    for j in range(0,i):
        aj = gramA[ai][0][0]
        if ai!=aj :
            if aj in gramA and checkForIndirect(gramA,ai,aj):
                gramA = rep(gramA, ai)

for i in range(1,c):
    ai = "A"+str(i)
    for j in gramA[ai]:
        if ai==j[0]:
            gramA = removeDirectLR(gramA, ai)
            break

op = {}
for i in gramA:
    a = str(i)
    for j in conv:
        a = a.replace(conv[j],j)
    revconv[i] = a

for i in gramA:
    l = []
    for j in gramA[i]:
        k = []
        for m in j:
            if m in revconv:
                k.append(m.replace(m,revconv[m]))
            else:
                k.append(m)
        l.append(k)
    op[revconv[i]] = l

return op

result = rem(gram)

for i in result:
    print(f'{i}->{result[i]}')

```

## OUTPUT :

```
T->[['F', 'T']]
F->[['(', 'E', ')'], ['i']]
E->[['+', 'T', 'E'], ['e']]
T->[['*', 'F', 'T'], ['e']]
```

### (ii) Left Factoring:

```
from itertools import takewhile
```

```
def groupby(ls):
```

```
    d = {}
```

```
    ls = [ y[0] for y in rules ]
```

```
    initial = list(set(ls))
```

```
    for y in initial:
```

```
        for i in rules:
```

```
            if i.startswith(y):
```

```
                if y not in d:
```

```
                    d[y] = []
```

```
                    d[y].append(i)
```

```
    return d
```

```
def prefix(x):
```

```
    return len(set(x)) == 1
```

```
starting=""
```

```
rules=[]
```

```
common=[]
```

```
alphabetset=["A","B","C","D","E","F","G","H","I","J","K","L","M","N","O","P","Q","R","S","T","U","V","W","X","Y","Z"]
```

```
s= "S->iEtS|iEtSeS|a"
```

```
while(True):
```

```
    rules=[]
```

```
    common=[]
```

```
    split=s.split("->")
```

```
    starting=split[0]
```

```
    for i in split[1].split("|"):
```

```
        rules.append(i)
```

```

for k, l in groupby(rules).items():
    r = [l[0] for l in takewhile(prefix, zip(*l))]
    common.append("".join(r))
for i in common:
    newalphabet=alphabetset.pop()
    print(starting+"->" +i+newalphabet)
    index=[]
    for k in rules:
        if(k.startswith(i)):
            index.append(k)
    print(newalphabet+"->",end="")
    for j in index[:-1]:
        stringtoprint=j.replace(i,"", 1)+"|"
        if stringtoprint=="|":
            print("\u03B5","|",end="")
        else:
            print(j.replace(i,"", 1)+"|",end="")
    stringtoprint=index[-1].replace(i,"", 1)+"|"
    if stringtoprint=="|":
        print("\u03B5","",end="")
    else:
        print(index[-1].replace(i,"", 1)+"" ,end="")
    print("")
break

```

#### OUTPUT:

```

S->iEtSZ'
Z' ->ε |eS
S->aY'
Y' ->ε

```

#### RESULT :

The program to Eliminate Left recursion and Left factoring has been executed successfully.