Generic Hash Dictionaries

Hash Dictionaries so far

The Hash Dictionary Library

```
// Implementation-side types
typedef struct chain_node chain;
struct chain node {
                     // data != NULL
 entry data;
 chain* next;
struct hdict header {
 int size:
                     // size >= 0
 int capacity;
                    // capacity > 0
                    // \length(table) == capacity
 chain*[] table:
typedef struct hdict_header hdict;
// Representation invariant
bool is_hdict (hdict* H) {
return H != NULL
    && H->size >= 0
    && H->capacity > 0
    && is array expected length(H->table, H->capacity)
    && is_valid_hashtable(H);
// Implementation of interface functions
int index of key(hdict* H, key k)
//@requires is_hdict(H);
//@ensures 0 <= \result && \result < H->capacity:
return abs(key_hash(k) % H->capacity);
entry hdict_lookup(hdict* H, key k)
//@requires is_hdict(H);
//@ensures \result == NULL
          || key_equiv(entry_key(\result), k);
int i = index_of_key(H, k);
```

```
for (chain* p = H->table[i]; p != NULL; p = p->next)
   if (key_equiv(entry_key(p->data), k))
     return p->data:
 return NULL:
void hdict insert(hdict* H, entry e)
//@requires is hdict(H) && e != NULL;
//@ensures hdict_lookup(H, entry_key(e)) == e;
//@ensures is_hdict(H);
 key k = entry key(e);
 int i = index of key(H, k);
 for (chain* p = H->table[i]; p != NULL; p = p->next) {
   if (key_equiv(entry_key(p->data), k)) {
      p->data = e;
      return;
 chain* p = alloc(chain);
 p->data = e:
 p->next = H->table[i];
 H->table[i] = p;
 (H->size)++;
hdict* hdict_new(int capacity)
//@requires capacity > 0:
//@ensures is hdict(\result);
 hdict^* H = alloc(hdict):
 H->size = 0:
 H->capacity = capacity;
 H->table = alloc_array(chain*, capacity);
 return H;
// Client type
typedef hdict* hdict_t;
```

```
Client Interface

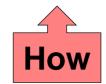
// typedef _____* entry;
// typedef _____* key;

key entry_key(entry e)
/*@requires e != NULL; @*/;

int key_hash(key k);

bool key_equiv(key k1, key k2);
```

```
Library Interface
// typedef
                * hdict_t;
hdict_t hdict_new(int capacity)
/*@requires capacity > 0;
                                                  @*/
 /*@ensures \result != NULL:
                                                  @*/:
entry hdict_lookup(hdict_t D, key k)
/*@requires D != NULL:
                                                  @*/
/*@ensures \result != NULL
           || key_equiv(entry_key(\result), k);
                                                  @*/:
void hdict insert(hdict t D, entry e)
/*@requires D != NULL && e != NULL;
                                                  @*/
 /*@ensures hdict_lookup(D, entry_key(e)) == e; @*/
```





- Generic data structures
 - work the same way no matter the type of their data
 - Dictionaries are intrinsically generic
 - they map keys to entries
 - they work the same for any type of key and entry
 - Hash dictionaries should be generic
 - they abstract key manipulations into client functions
 - key_entry, key_hash and key_equiv

Generic libraries

- a single implementation that
 - > lets the clients choose the type of their data
 - allows multiple instances of the data structure with different data types in the same application

- A single implementation that
 - lets the clients choose the type of their data
 - > Yes!
 - ➤ the client interface mandates that the client define the types key and entry

```
Client Interface

// typedef _____* entry;
// typedef _____* key;

key entry_key(entry e)
/*@requires e != NULL; @*/;

int key_hash(key k);

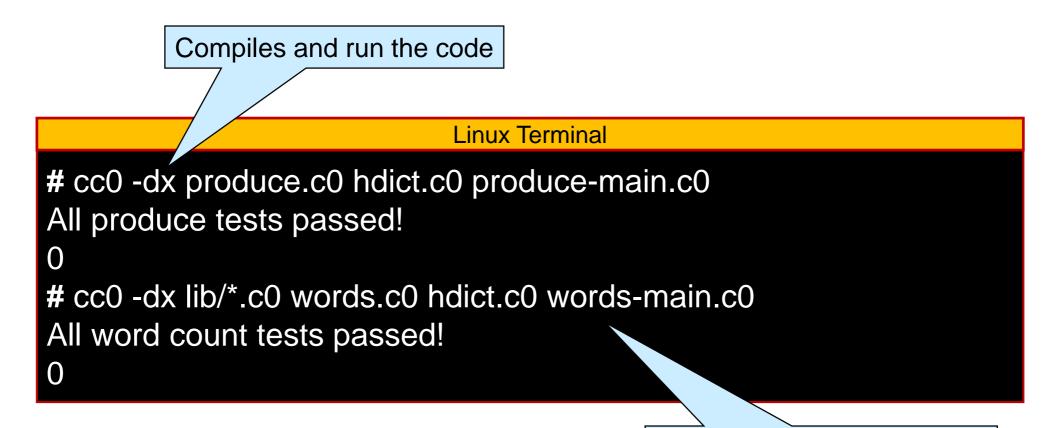
bool key_equiv(key k1, key k2);
```

- > the client does so in the client definition file
- > Let's try it out to be sure

```
Client definition file
 return h:
// What the client wants to store in the dictionary
struct inventory item {
 string fruit;
                  // key
 int quantity;
      * Fulfilling the library interface ******/
typedef struct inventory item* entry;
typedef string key;
key entry_key(entry e)
//@requires e != NULL;
 return e->fruit;
bool key equiv(key k1, key k2) {
 return string_equal(k1, k2);
int key_hash(key k) {
 return lcg_hash_string(k);
```

- A single implementation that
 - lets the clients to chose the type of their data





Another client application that uses the hash dictionary to count the occurrences of each word in a file

- A single implementation that
 - lets the clients to chose the type of their data



 allows multiple instances of the data structure with different data types in the same application

cc0 -dx produce.c0 lib/*.c0 words.c0 hdict.c0 combined-main.c0 words.c0:29.1-29.30:error:type name 'entry' defined more than once previous definition at produce.c0:28.1-28.38 typedef struct wcount* entry; Compilation failed

> there can be at most one definition of the types key and entry



- A single implementation that
 - lets the clients choose the type of their data

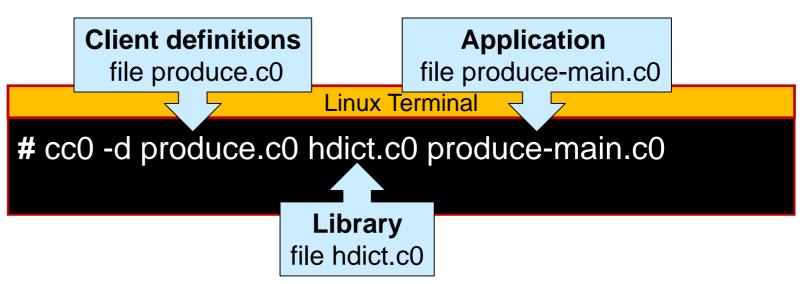


 allows multiple instances of the data structure with different data types in the same application



This approach also forced clients to split their application

code into two files



- This is an unnatural compilation pattern
 - ➤ We would like to compile the hash dictionary library just the way we compile a stack library

Making this Library Generic

 With the stack library, setting the element type to void* solved both problems

typedef void* elem;

> This was now C1 code

Let's do the same with the hash dictionary library

void* to the Rescue

Upgrading the Library

 The only changes we need to make to the library are defining key and entry as void*

```
Client Interface

// typedef _____* entry;
// typedef _____* key;

key entry_key(entry e)
/*@requires e != NULL; @*/;

int key_hash(key k);

bool key_equiv(key k1, key k2);

Client Interface

typedef void* entry;
typedef void* key;

key entry_key(entry e)
/*@requires e != NULL; @*/;

int key_hash(key k);

bool key_equiv(key k1, key k2);
```

This only affects the client interface

We should not add NULL-check on keys since the client could have • chosen key to be a pointer type • chosen NULL to be a valid key



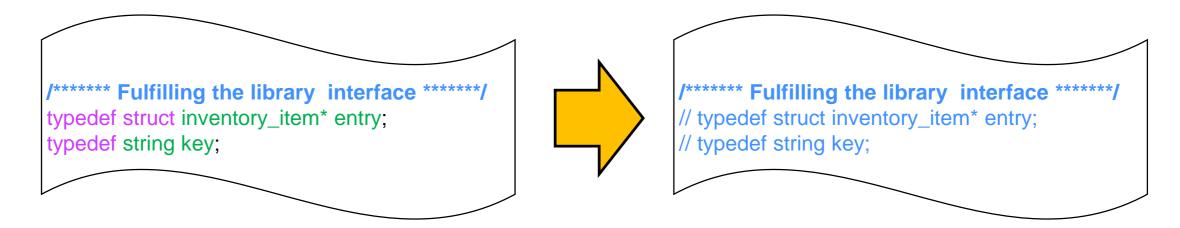
```
typedef void* entry;
typedef void* key;

key entry_key(entry e)
/*@requires e != NULL; @*/;

int key_hash(key k);

bool key_equiv(key k1, key k2);
```

- The client does not need to define key and entry
 - the library defines both to void*



- For the client
 - an entry is still a struct inventory_item*
 - a key is now a string* —

It's got to be a pointer

- > "lime" must now live in a cell in allocated memory to be used as a key
- > NULL does not correspond to any valid key

```
typedef void* entry;
typedef void* key;

key entry_key(entry e)
/*@requires e != NULL; @*/;

int key_hash(key k);

bool key_equiv(key k1, key k2);
```

- For the client
 - an entry is still a struct inventory_item*
 - a key is now a string*
- So,
 - every value of type entry must have tag struct inventory_item*
 - every value of type key must have tag string*

```
int key_hash(key k) {
    return lcg_hash_string(k);
}

NULL is not a
    valid fruit name

int key_hash(key k)

//@requires k != NULL && \hastag(string*, k);

{
    ...
}

Every key is in
    reality a string*
```

```
typedef void* entry;
typedef void* key;

key entry_key(entry e)
/*@requires e != NULL; @*/;

int key_hash(key k);

bool key_equiv(key k1, key k2);
```

- For the client, a key is now a string*
- Before using a value of type key, we need to
 - cast it to string*
 - dereference the result to a string

```
int key_hash(key k) {
    return lcg_hash_string(k);
}

lcg_hash_string takes
    a string as input

| int key_hash(key k) //@requires k != NULL && \hastag(string*, k);
| return lcg_hash_string(*(string*)k);
| A void* cast to a string* and dereferenced to a string*
```

```
typedef void* entry;
typedef void* key;

key entry_key(entry e)
/*@requires e != NULL; @*/;

int key_hash(key k);

bool key_equiv(key k1, key k2);
```

- For the client
 - an entry is still a struct inventory_item*
 - a key is now a string*
 - > "lime" must now live in a cell in allocated memory to be used as a key
 - > NULL does not correspond to any valid key

 When extracting a key from an entry, we must put it in a cell in allocated memory

```
key entry_key(entry e)
//@requires e != NULL;
{
  return e->fruit;
}
```

```
key entry_key(entry e)

//@requires e != NULL && \hastag(struct inventory_item*, e);

//@ensures \result != NULL && \hastag(string*, \result);

{

struct inventory_item* E = (struct inventory_item*)e;

string* K = alloc(string);

*K = E->fruit;

return (key)K;

}

Auxiliary variables can help make those casts
```

more readable

```
typedef void* entry;
typedef void* key;

key entry_key(entry e)
/*@requires e != NULL; @*/;

int key_hash(key k);

bool key_equiv(key k1, key k2);
```

- When extracting a key from an entry, we must put it in a cell in allocated memory
 - add a helper function that turns a string to a string* for even better readability

```
string* to_string_ptr(string s)
//@ensures \result != NULL;
{
    string* s_ptr = alloc(string);
    *s_ptr = s;
    return s_ptr;
}

key entry_key(entry e)
//@requires e != NULL && \hastag(struct inventory_item*, e);
//@ensures \result != NULL && \hastag(string*, \result);
{
    return e->fruit;
}

return e->fruit;
}
```

We could write it in one line as return (key) to_string_ptr(((struct inventory_item*)e)->fruit); but that's unreadable

```
Client Interface
typedef void* entry:
typedef void* key;
key entry_key(entry e)
/*@requires e != NULL; @*/;
int key_hash(key k);
bool key_equiv(key k1, key k2);
```

```
What the client wants
                                  Similar to key hash
struct inventory item {
 string fruit;
                 // key
 int quantity;
/***** Fulfilling the library interface ******/
typedef struct inventory item* entry;
typedef string key;
key entry_key(entry e)
//@requires e != NULL;
 return e->fruit:
bool key_equiv(key k1, key k2) {
 return string_equal(k1, k2);
int key_hash(key k) {
 return lcg_hash_string(k);
```

```
// What the client wants to store
struct inventory item {
 string fruit;
                 // key
 int quantity;
/****** Fulfilling the library interface ******/
key entry_key(entry e)
//@requires e != NULL && \hastag(struct inventory item*, e);
//@ensures \result != NULL && \hastag(string*, \result);
 struct inventory_item* E = (struct inventory_item*)e;
 string* K = to_string_ptr(E->fruit);
 return (key)K;
bool key equiv(key k1, key k2)
//@requires k1 != NULL && \hastag(string*, k1);
//@requires k2 != NULL && \hastag(string*, k2);
 return string_equal(*(string*)k1, *(string*)k2);
int key hash(key k)
//@requires k != NULL && \hastag(string*, k);
 return lcg_hash_string(*(string*)k);
```

Upgrading the Client Application

- Cast entries and keys before calling the library operations
- Turn values of type string to string* before using them as keys

```
int main () {
    struct inventory_item* A = make_inventory_item("apple", 20);
    struct inventory_item* B = make_inventory_item("banana", 10);
    struct inventory_item* C = make_inventory_item("pumpkin", 50);
    struct inventory_item* D = make_inventory_item("banana", 20);

hdict_t H = hdict_new(10);
    hdict_insert(H, A);
    hdict_insert(H, B);
    hdict_insert(H, C);
    assert(hdict_lookup(H, "apple") != NULL);
    assert(hdict_lookup(H, "lime") == NULL);
    hdict_insert(H, D);

return 0;
}
```



```
int main () {
    struct inventory_item* A = make_inventory_item("apple", 20);
    struct inventory_item* B = make_inventory_item("banana", 10);
    struct inventory_item* C = make_inventory_item("pumpkin", 50);
    struct inventory_item* D = make_inventory_item("banana", 20);

    hdict_t H = hdict_new(10);
    hdict_insert(H, (entry)A);
    hdict_insert(H, (entry)B);
    hdict_insert(H, (entry)C);
    assert(hdict_lookup(H, (key)to_string_ptr("apple")) != NULL);
    assert(hdict_lookup(H, (key)to_string_ptr("apple")) == NULL);
    hdict_insert(H, (entry)D);

return 0;
}
```

Generic Hash Dictionaries

Let's try it on our examples

```
# cc0 -dx hdict.c1 produce.c1 produce-main.c1
All produce tests passed!

# cc0 -dx hdict.c1 lib/*.c0 words.c1 words-main.c1
All word count tests passed!

O
```

- we can now put the library before all client files
- this means we could merge produce.c1 and produce-main.c1 into a single file
 - > same thing for word.c1 and words-main.c1

Generic Hash Dictionaries

Let's try it on our examples

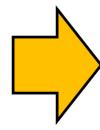


- This still doesn't work!
 - both produce.c1 and words.c1 define entry_key
 - and key_equiv and key_hash
 - This is not allowed in C0/C1
 - Even if it were, the library wouldn't know which version to use with what data

Function Pointers to the Rescue

Renaming the Client Functions

- We avoid having duplicate client definition function names by renaming them
 - key_hash to key_hash_produceetc
 - and similarly for the word count application

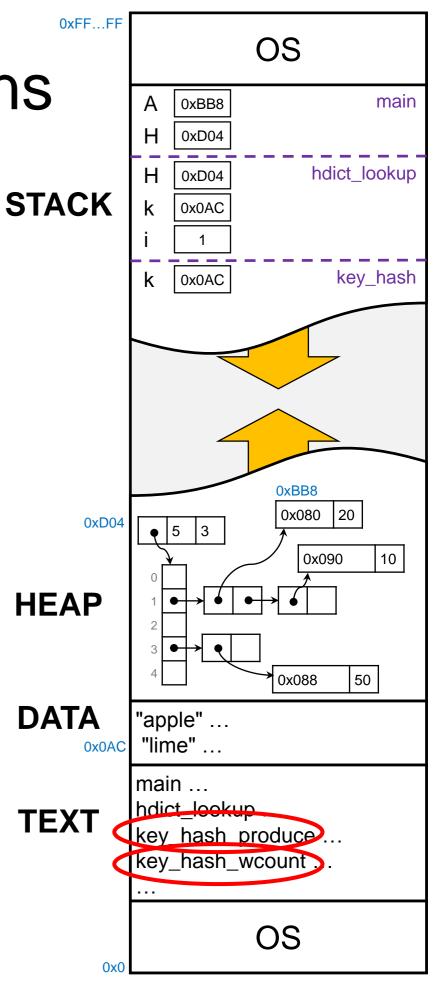


 But how to tell the library which function to use?

```
This is all we need to do
                                 in the client definition file
// What the client wants to store
struct inventory item {
 string fruit;
                 // kev
 int quantity;
/***** Fulfilling the library interface ******/
key entry_key_produce(entry e)
//@requires e != NULL && \hastag(struct inventory_item*, e);
//@ensures \result != NULL && \hastag(string*, \result);
 struct inventory_item* E = (struct inventory_item*)e;
 string* K = to_string_ptr(E->fruit);
 return (key)K;
bool key_equiv_produce(key k1, key k2)
//@requires k1 != NULL && \hastag(string*, k1);
//@requires k2 != NULL && \hastag(string*, k2);
 return string_equal(*(string*)k1, *(string*)k2);
in key hash produce ky
//@requires k != NULL && \hastag(string*, k);
 return lcg_hash_string(*(string*)k);
```

Accessing the Right Functions

- During execution, functions live in the TEXT segment of memory
 - & allows us to obtain their address and pass it around as a function pointer
 - we can call a function through a pointer to it
- Idea: make pointers to the appropriate client function available to the library
 - o but how to do so?



Accessing the Right Functions – I

 One option is to pass the right client functions to the library functions that use them

```
entry A = make_inventory_item("apple", 20);
hdict_insert(H, A);

entry A = make_inventory_item("apple", 20);
hdict_insert(H, A, &entry_key_produce,
&key_hash_produce,
&key_equiv_produce):
```

- Then do this for every use of hdict_insert and hdict_lookup
 - We will make mistakes
 - This is also a poor way of thinking about dictionaries
 - > H is a dictionary where we want to store produce
 - > every insertion and lookup on H will need these client functions
 - not others

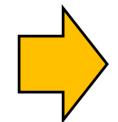


Accessing the Right Functions – II

 A better option is to pass the right client functions when we create a dictionary This is all we need to do in the client application file

o in hdict_new

```
hdict_t H = hdict_new(10);
```



```
hdict_t H = hdict_new(H, &entry_key_produce
&key_hash_produce,
&key_equiv_produce);
```

- hdict_new needs to store the client functions in H itself
 - we need to modify the internal representation
 - but first we need to give types to the client functions

Client Function Types

- We need to define types for the client functions
 - > entry_key_fn
 - > key_hash_fn
 - > key_equiv_fn

since

- hdict_new takes them as arguments
- we will store them in the concrete implementation type
- These definitions go in the client interface

```
Client Interface

typedef void* entry;
typedef void* key;

key entry_key(entry e)
/*@requires e != NULL; @*/;
int key_hash(key k);
bool key_equiv(key k1, key k2);

Client Interface

typedef void* entry;
typedef void* key;

typedef void* key;

typedef void* entry;
typedef void* key;

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typedef void* entry;
typedef void* entry;
typedef void* key;

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typedef void* entry;
typedef void* entry;
typedef void* key;

typedef void* entry;
typedef void* entry;
typedef void* key;

typedef void* entry;
typedef void* key;
typ
```

Upgrading the Concrete Type

- We store the client definitions in the data structure itself
 - extend struct hdict_header with three additional fields

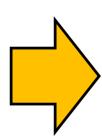
- Storing both data and functions in a struct is a fundamental concept in object-oriented programming
 - these structs are called objects
 - the functions are called methods

There is a lot more to object-oriented programming however

Upgrading the Representation Invariant

A valid hdict cannot have NULL in the added fields

```
bool is_hdict (hdict* H) {
  return H != NULL
    && H->size >= 0
    && H->capacity > 0
    && is_array_expected_length(H->table, H->capacity)
    && is_valid_hashtable(H);
}
```



```
bool is_hdict (hdict* H) {
  return H != NULL
    && H->size >= 0
    && H->capacity > 0
    && is_array_expected_length(H->table, H->capacity)
    && H->key != NULL
    && H->hash != NULL
    && H->equiv != NULL
    && Is_valid_hashtable(H);
}
```

Upgrading hdict_new

- hdict_new
 - takes the client functions as inputs
 - expects them to be non-NULL
 - stores them in the added fields of the concrete type

```
hdict* hdict_new(int capacity)

//@requires capacity > 0;

//@ensures is_hdict(\result);

{
   hdict* H = alloc(hdict);
   H->size = 0;
   H->capacity = capacity;
   H->table = alloc_array(chain*, capacity);
   return H;
}
```



Calling the Client Functions

Whenever we need a client function,
 we call the function pointer in the data structure

Here, H->hash

For example,

```
int index_of_key(hdict* H, key k)

//@requires is_hdict(H);

//@ensures 0 <= \result && \result < H->capacity;
{
    return abs(key_hash(k) % H->capacity);
}

This is the same as
    (*(H->hash))(...)
```

Upgrading hdict_lookup

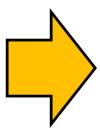
- Proceed in the same way
 - change client function calls to function pointer calls



- The function pointer syntax is hard to read
 - factor it out in helper functions similar to index_of_key

Upgrading hdict_lookup

- The function pointer syntax is hard to read
 - factor it out in helper functions similar to index_of_key



```
int index of key(hdict* H, key k)
   //@requires is_hdict(H);
   //@ensures 0 <= \result && \result < H->capacity;
    return abs((*H->hash)(k) % H->capacity);
   key entry key(hdict* H, entry x)
   //@requires is_hdict(H) && x != NULL;
    return (*H->key)(x);
   bool key_equiv(hdict* H, key k1, key k2)
   //@requires is_hdict(H);
    veturn (*H->equiv)(k1, k2);
entry hdict lookup(hdict* H, key k)
//@requires is hdict(H);
//@ensures \result == NULL
          || key equiv(entry key(\result), k);
 int i = index of key(H, k);
 for (chain* p - H > table[i]; p !- NULL; p = p->next) {
  if (key_equiv(H, entry_key(H, p->data), k))
```

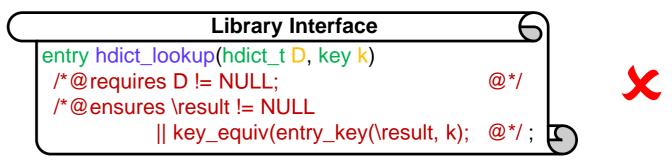
return p->uata,

return NULL;

hdict_insert is similar

Updating the Library Interface

- The client interface does not contain entry_key and key_equiv any more
 - We cannot call them in the library interface



Using the fields of the implementation type would violate the interface

```
Library Interface

entry hdict_lookup(hdict_t D, key k)

/*@requires D != NULL;

/*@ensures \result != NULL

|| (*H->equiv)((*H->key)(\result, k); @*/;
```

 We must give up on this refined postcondition

```
Library Interface

entry hdict_lookup(hdict_t D, key k)
/*@requires D != NULL;

@*/;
```

The Hash Dictionary Library

```
// Implementation-side types
                                                           bool key_equiv(hdict* H, key k1, key k2)
                                                                                                                 Implementation
typedef struct chain node chain:
                                                           //@requires is hdict(H);
struct chain_node {
                     // data != NULL
 entry data;
                                                            return (*H->equiv)(k1, k2);
 chain* next;
struct hdict header {
                                                           entry hdict lookup(hdict* H, key k)
 int size;
                       // size >= 0
                                                           //@requires is hdict(H);
 int capacity;
                       // capacity > 0
                                                           //@ensures \result == NULL
 chain*[] table:
                       // \length(table) == capacity
                                                                      || key_equiv(entry_key(\result), k);
                      // != NULL
 entry_key_fn* key;
 key hash fn* hash; // != NULL
                                                            int i = index of key(H, k);
 key equiv fn* equiv; // != NULL
                                                            for (chain* p = H->table[i]; p != NULL; p = p->next) {
                                                               if (key_equiv(H, entry_key(H, p->data), k))
typedef struct hdict header hdict:
                                                                 return p->data;
// Representation invariant
                                                            return NULL;
bool is hdict (hdict* H) {
return H != NULL
                                                           void hdict_insert(hdict* H, entry e) // left as exercise
    && H->size >= 0
    && H->capacity > 0
                                                           hdict* hdict new(int capacity,
    && is array expected length(H->table, H->capacity)
                                                               entry_key_fn* entry_key, key_hash_fn* hash,
    && H->key != NULL
                                                               key equiv fn* equiv)
    && H->hash != NULL
                                                           //@requires capacity > 0 && entry key != NULL;
    && H->equiv != NULL
                                                           //@requires hash != NULL && equiv != NULL;
    && is_valid_hashtable(H);
                                                           //@ensures is_hdict(\result);
                                                            hdict* H = alloc(hdict);
// Implementation of interface functions
                                                             H->size = 0;
int index_of_key(hdict* H, key k)
                                                             H->capacity = capacity:
//@requires is_hdict(H);
                                                             H->table = alloc array(chain*, capacity):
//@ensures 0 <= \result && \result < H->capacity:
                                                             H->key = entry_key;
                                                             H->hash = hash;
 return abs((*H->hash)(k) % H->capacity);
                                                            H->equiv = equiv;
                                                            return H:
key entry_key(hdict* H, entry x)
//@requires is_hdict(H) && x != NULL;
                                                           // Client type
return (*H->key)(x);
                                                           typedef hdict* hdict t;
```

```
typedef void* entry;
typedef void* key;

typedef key entry_key_fn(entry e)
    /*@requires e != NULL; @*/;
typedef int key_hash_fn(key k);
typedef bool key_equiv_fn(key k1, key k2);
```

```
Library Interface
// typedef
                 * hdict t:
hdict_t hdict_new(int capacity,
                   entry key fn* entry key,
                   key hash fn* hash,
                  key equiv fn* equiv)
 /*@requires capacity > 0 && entry_key != NULL;@*/
 /*@requires hash != NULL && equiv != NULL;
                                                 @*/
 /*@ensures \result != NULL:
                                                 @*/:
entry hdict_lookup(hdict_t D, key k)
/*@requires D != NULL;
                                                 @*/:
void hdict_insert(hdict_t D, entry e)
 /*@requires D != NULL && e != NULL;
```

Is it Generic?

Linux Terminal

cc0 -dx hdict.c1 produce.c1 lib/*.c0 words.c1 combined-main.c1 All word count tests passed!
All produce tests passed!

• Yes!



Harmony

Experimenting with Client Definitions

- Now that we have an easy way to specify which client definition functions to use, we can test a few things
 - Let's consider alternatives versions of key_hash and key_equiv
 - > they look at the length of the key

This is a bad hash function. Let's use it anyway for simplicity

```
int key_hash_produce(key k)
//@requires k != NULL && \hastag(string*, k);
{
   return lcg_hash_string(*(string*)k);
}
```

```
bool key_equiv_produce(key k1, key k2)
//@requires k1 != NULL && \hastag(string*, k1);
//@requires k2 != NULL && \hastag(string*, k2);
{
   return string_equal(*(string*)k1, *(string*)k2);
}
```

```
This are our original functions
```

```
int key_hash_produce_alt(key k)
//@requires k != NULL && \hastag(string*, k);
{
   return string_length(*(string*)k);
}
```

```
bool key_equiv_produce_alt(key k1, key k2)
//@requires k1 != NULL && \hastag(string*, k1);
//@requires k2 != NULL && \hastag(string*, k2);
{
    return string_length(*(string*)k1) == string_length(*(string*)k2);
}
```

This are our alternative functions

Mixing and Matching

 key_hash_produce and key_equiv_produce are meant to be used together

```
hdict_t H hdict_new(H, &entry key_produce, &key_equiv_produce);
```

Same for key_hash_produce_alt and key_equiv_produce_alt

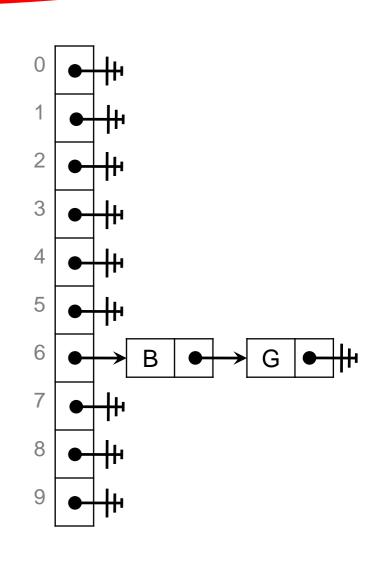
• But what if we mix and match them?

Mixing and Matching

- But what if we mix and match them?
 - key_hash_produce_alt with key_equiv_produce

```
hdict_t H hdict_new(H, &entry_key_produce,
&key_hash_produce_alt, &key_equiv_produce);
```

- Let's use the dictionary
 - ✓ new dictionary
 ✓ insert B = ("banana", 10)
 ✓ insert G = ("grapes", 30)
 - □ key_hash_produce_alt returns 6 on both
 - both "banana" and "grapes" have length 6
 - □ both end up in the same bucket
 - but key_hash_produce would have sent them in different buckets
 - > This is not as **efficient** as using key_hash_produce
 - ☐ the dictionary works correctly, but not is not as fast



Mixing and Matching

That's the other way around • But what if we mix and match them? key_hash_produce with key_equiv_produce_alt hdict_t H hdict_new(H, &entry_key_produce &key_hash_produce, &key_equiv_produce_alt); Let's use the dictionary key_hash_produce returns 7 on "banana" new dictionary √ insert B = ("banana", 10) look up "grapes" □ key_hash_produce returns 2 on "grapes" □ there is nothing in bucket 2 □ lookup "grapes" returns NULL > This is incorrect! "grapes" and "banana" have length 6 key_equiv_produce_alt treats them as equal

□ What look up "grapes" asks is find an entry whose key has length 6

B fits the bill, but it is not found

Harmony

- The key hash and equivalence functions are in harmony when equivalent entries have the same hash value
 - key_hash_produce and key_equiv_produce_alt are not in harmony
 - □ "banana" and "grapes" are equal according to key_equiv_produce_alt
 - □ but, according to key_hash_produce"banana" hashes to index 7 while "grapes" hashes to index 2
 - > the other combinations are in harmony
 - When they are not in harmony, the hash dictionary does not work correctly
 - it may return the wrong answer
 - Harmony does not guarantee efficiency