Monoid $M = \langle a, b \mid ba = aa \rangle$: Upho Lattice with Core M_2 The following diagram represents the upho lattice for the monoid $M = \langle a, b \mid ba = aa \rangle$, corresponding to the case r = 2 of thm:rank_two.ThecoreofthislatticeisM₂.

aa

bb

ab

Figure 1: Upho lattice for $M = \langle a, b \mid ba = aa \rangle$ with core M_2 .