

figureSketch for the construction of a short odd cycle containing v, in the case d=2, when both v and its blue neighbour v' lie outside  $Q_{2r}$ . The highlighted cells are used to construct paths from v and v' to  $q'_{t'}$ , where an application of

claim:paths allows to close them into a cycle.