$U(x,y) = y \left[ -2 \frac{\ln(\cosh x)}{x^2} + \frac{x - \tanh x}{x^2} y + \frac{\tanh x}{x} (2 - y \tanh x) \right]$ 

 $= y \left[ 1 + \frac{2}{9} x^4 - \left( \frac{2}{3} x - \frac{8}{15} x^3 \right) y \right] + [5]$ 

 $= x \left[ 1 - \frac{1}{3}x^2 - \left( \frac{2}{3}x - \frac{4}{15}x^3 \right) y \right] + [5]$ 

 $V(x,y) = 2\frac{\ln(\cosh x)}{2} + 2\frac{\tanh x - x}{2}u$