$$\mathcal{I}(X)$$

$$\downarrow^{\phi_{I}} \qquad \downarrow^{\phi_{I}H}$$

$$\mathcal{P}(X) \xrightarrow{\phi_{PH}\phi_{H}} \mathcal{H}(X)$$