shown below. [scale = 0.8](0,0)circle(0.5); at(0,0) $\rho_i$ ; [-i., bend left=45] (0,-0.5) to node[above]  $\mathcal{E}(\rho_i)$  (4,0);

A visual representation of the protocol in the case of two iterations is

(6,0) rectangle (8,2); at (7,1) 
$$\mathcal{S}$$
, '...';  
[- $\dot{\iota}$ , bend left=45] (10,1) to node[above]  $C_{-}(\mathcal{E}(\rho_{j}))$  (8,1);  
[- $\dot{\iota}$ , bend left=45] (-1,-0.5) to node[above]  $\mathcal{E}(\rho_{j})$  (-3,0);  
[- $\dot{\iota}$ , bend left=45] (-5,-0.5) to node[above]  $\mathcal{E}(\rho_{j})$  (-9,0);

[-, dashed] (-4,0) - (6,0); at (-4,0) :;[-i, bend left=45] (-11,-0.5) to node[above]  $\mathcal{E}(\rho_i)$  (-13,0);

pair of operations and measurements.

[-
$$\dot{\epsilon}$$
, bend left=45] (-17,-0.5) to node[above]  $\mathcal{E}(\rho_j)$  (-13,0), [- $\dot{\epsilon}$ , bend left=45] (-17,-0.5) to node[above]  $\mathcal{E}(\rho_j)$  (-19,0); [- $\dot{\epsilon}$ , dashed] (-12,0) - (4,0); at (-12,0) :; [- $\dot{\epsilon}$ , bend left=45] (-11,-3) to node[above]  $\mathcal{E}(\rho_j)$  (-13,-2);

[- $\dot{\epsilon}$ , bend left=45] (-17,-3) to node[above]  $\mathcal{E}(\rho_i)$  (-19,-2); (11,-2) circle (0.5); at (11,-2) S; [- $\dot{c}$ , bend left=45] (13.5,-2) to node[above]  $C_{+}(C_{-}(\mathcal{E}(\rho_{i})))$  (14.5,-1); [- $\dot{c}$ , bend left=45] (8.5,-2.3) to node[right] '+' (11,-3); [-¿, bend left=45] (16.5,-

2) to node[below] '-' (17.5,-3); [-¿, bend left=45] (11,-2.3) to node[below]  $C_{-}(C_{-}(\mathcal{E}(\rho_{i})))$  (8,-3);

Description:

In this figure, noisy copies of the states  $\rho_i$  are first combined pairwise with the controlled unitary operation in the quantum switch. The measure-

ments are performed on the ancilla qubits, followed by the recombination of the pairs depending on the outcomes. Specifically, when the measurement

outcomes result in a pair of '-', it leads to the effective state  $C_{-}(\mathcal{E}(\rho_{i}))$ . This process is repeated for another iteration, as indicated by the additional