$$\underbrace{U(1)_k}^{X,\tilde{X}}\underbrace{U(1)_{-k}}^{Y,\tilde{Y}}\underbrace{U(1)_k}^{Z,\tilde{Z}}\underbrace{U(1)_{-k}}$$