The partition, 
$$\sum_{k=1}^{R} (\beta_k + m_{k-1} + 1)(R - k + 1) - R.$$

$$\beta_1$$

$$\beta_2 + m_1 + 1$$

$$\beta_R + m_R - 1 + 1$$