



figure The SIRV Compartmental Model for COVID-19 disease dynamics (similar to the one in Abou-Ismaïl et al [?]), consisting Susceptible ( $S$ ), Exposed ( $E$ ), Quarantined ( $U$ ), Recovered ( $R$ ), and Vaccinated ( $V$ ) compartments. Three doses of vaccination are assumed, the second and the third being administered 28 and 208 days after the first. The transmission rate is  $\beta$ , recovery rate is  $\delta$ , the rate of becoming susceptible after disease is  $\gamma$ , the vaccination rates are  $\alpha_i$  for  $i^{th}$  vaccination, calculated as a proportion of people who took the previous vaccine, and the rate of vaccination immunity wearing off from  $i^{th}$  vaccination is  $\phi_i$ .