$$ar{u}_{t+1}$$
  $u_t - P_t^n g_t \ u_t - g_t$ 

Figure 1: Illustration of the proposed algorithm: based on an iterate  $u_t \in \mathcal{M}$  and the choice of a linear space  $\mathcal{T}_t$ , an approximation  $P_t^n g_t \in \mathcal{T}_t$  of the true gradient  $g_t$  is first obtained via a random operator  $P_t^n$ . Then an update  $\bar{u}_{t+1} = u_t - s_t P_t^n g_t$  is obtained given a step size  $s_t$ . Then, the next iterate  $u_{t+1} \in \mathcal{M}$  is obtained

through application of the retraction map  $R_t$ .