The monoid $M = \langle a, b \mid ba = aa \rangle$ from the case $r = 2$ of thm:rank$_t$wo, an uphol lattice with core M_2.