

CS521 hw3

Name: Yuxiao Wu

No collaborators, no late days

Source: Textbook

Problem 1:

1. factorial(5)

```
n = 5, n != 0
return 5 * factorial(4)
factorial(4)
n = 4, n != 0
return 4 * factorial(3)
.....
```

Factorial(1) = $1 * \text{factorial}(0) = 1 * 1 = 1$

Factorial(5) = $5 * 4 * 3 * 2 * 1 * 1 = 120$

```
def factorial(n):
    if n == 0:
        return 1
    else:
        return n * factorial(n-1)
```

2. factorial(8)

Same as above

Factorial(8) = $8 * \text{factorial}(7)$

Factorial(7) = $7 * \text{factorial}(6)$

.....

Factorial(2) = $2 * \text{factorial}(1)$

Factorial(1) = $1 * \text{factorial}(0) = 1$

Factorial(8) = $8 * 7 * 6 * \dots * 2 * 1 = 40320$

3. y(8)

m = 8

n = x(8-1) = x(7)

x(7) -> $7 * 6 * x(6)$

x(6) -> $6 * 5 * x(5)$

x(5) -> $5 * 4 * x(4)$

x(4) -> $4 * 3 * x(3)$

x(3) -> $3 * 2 * x(2)$

x(2) -> $2 * 1 * x(1)$

x(1) = 1

x(7) = $2 * 6 * 12 * 20 * 30 * 42 = 3628800$

```
def x(n):
    if n <= 1:
        return 1
    else:
        return n*(n-1)*x(n-1)
def y(m):
    if m == 1:
        return 1
    else:
        n = x(m - 1)
```

4. tribonacci(4)

```
# Function that finds the nth tribonacci number
def tribonacci(n):
    if n == 1:
        return 0
    elif n == 2:
        return 1
    elif n == 3:
        return 2
    else:
        return tribonacci(n-1) + tribonacci(n-2) + tribonacci(n-3)
```

tribonacci(4) -> tribonacci(4-1) + tribonacci(4-2) + tribonacci(4-3)

tribonacci(4) -> tribonacci(3) + tribonacci(2) + tribonacci(1)

tribonacci(4) -> 2 + 1 + 0 = 3

5. tribonacci(7)

tribonacci(7) -> tribonacci(6) + tribonacci(5) + tribonacci(4)

tribonacci(5) -> tribonacci(4) + tribonacci(3) + tribonacci(2) -> 3 + 2 + 1 = 6

tribonacci(6) -> tribonacci(5) + tribonacci(4) + tribonacci(3) -> 6 + 3 + 2 = 11

tribonacci(7) -> tribonacci(6) + tribonacci(5) + tribonacci(4) -> 11 + 6 + 3 = 20

Problem 2

Find the expected result of the two list comprehension by hand (show your work):

```
list_1 = [10-thing for thing in range(20,1,-1)]
list_2 = [val**3 for val in [1,1,2,2,3,3,4,4] if val!=2]
```

1. range(20,1,-1) = [20,19,18,17,....., 4,3,2]

for every thing in range(20,1,-1)

10 - thing -> [10 - 20, 10-19,, 10 - 3, 10 - 2]

List_1 = [-10, -9, -8, -7, -6, -5, -4,-3,-2,-1,0,1,2,3,1,4,5,6,7,8]

2. cubic every val in [1,1,2,2,3,3,4,4] except val == 2

list_2 = [1**3, 1**3, 3**3, 3**3, 4**3, 4**3]

list_2 = [1,1,27,27,64,64]